

16. More On Lists

Topics:

- References
- Alias
- More on Slicing
- Merging Sorted Lists

Comparing Lists

You can use `==` to compare two lists

```
>>> x = [10,20,30,40]
>>> y = [10,20,30,40]
>>> x==y
True
```

Comparing Lists

You can use `==` to compare two lists

x -->	0	----	10		y -->	0	----	10
	1	----	20			1	----	20
	2	----	30			2	----	30
	3	----	40			3	----	40

The Boolean expression `x==y` is True because x and y have the same length and identical values in each element

Comparing Lists

You can use `==` to compare two lists

```
>>> x = [1,2,3]
>>> y = [1.0,2.0,3.0]
>>> x==y
True
```

If there are ints and floats, convert everything to float then compare

Comparing Lists

Do not use `<`, `<=`, `>`, `>=` to compare two lists

```
>>> x = [10,20,30,40]
>>> y = [11,21,31,41]
>>> x<y
True
>>> y<x
True
```

Unpredictable

Aliasing

This:

```
x = [10,20,30,40]
y = x
```

Results in this:

x -->	0	----	10
	1	----	20
y -->	2	----	30
	3	----	40

Aliasing

```
x --> 0 ----> 10
      1 ----> 20
y --> 2 ----> 30
      3 ----> 40
```

Things to say:

x and y are variables that refer to the same list object.

The object is aliased because it has more than one name.

Tracking Changes

```
● x = [10,20,30,40]   x --> 0 ----> 10
  y = x              1 ----> 20
  y = [1,2,3]        2 ----> 30
                    3 ----> 40
```

Tracking Changes

```
x = [10,20,30,40]   x --> 0 ----> 10
● y = x             1 ----> 20
y = [1,2,3]         2 ----> 30
                    3 ----> 40
```

Tracking Changes

```
x = [10,20,30,40]   x --> 0 ----> 10
  y = x             1 ----> 20
● y = [1,2,3]      2 ----> 30
                    3 ----> 40

y --> 0 ----> 1
      1 ----> 2
      2 ----> 3
```

The is Operator

```
>>> x = [10,20,30,40]
>>> y = [10,20,30,40]
>>> x is y
False
```

```
x --> 0 ----> 10   y --> 0 ----> 10
      1 ----> 20   1 ----> 20
      2 ----> 30   2 ----> 30
      3 ----> 40   3 ----> 40
```

Even though the two lists have the same component values, x and y do not refer to the same object.

The is Operator

```
>>> x = [10,20,30,40]
>>> y = x
>>> x is y
True
```

```
x --> 0 ----> 10
      1 ----> 20
y --> 2 ----> 30
      3 ----> 40
```

x and y refer to the same object

Making a Copy of a List

```
● x = [10,20,30,40]   x --> 0 ----> 10  
  y = list(x)         1 ----> 20  
                      2 ----> 30  
                      3 ----> 40
```

Making a Copy of a List

```
● x = [10,20,30,40]   x --> 0 ----> 10  
  y = list(x)         1 ----> 20  
                      2 ----> 30  
                      3 ----> 40  
  
y --> 0 ----> 10  
      1 ----> 20  
      2 ----> 30  
      3 ----> 40
```

Slices Create new Objects

```
● x = [10,20,30,40]   x --> 0 ----> 10  
  y = x[1:]           1 ----> 20  
                      2 ----> 30  
                      3 ----> 40
```

Slices Create New Objects

```
● x = [10,20,30,40]   x --> 0 ----> 10  
  y = x[1:]           1 ----> 20  
                      2 ----> 30  
                      3 ----> 40  
  
y --> 0 ----> 20  
      1 ----> 30  
      2 ----> 40
```

Careful!

```
● x = [10,20,30,40]   x --> 0 ----> 10  
  y = x               1 ----> 20  
  y = x[1:]          2 ----> 30  
                    3 ----> 40
```

Careful!

```
● x = [10,20,30,40]   x --> 0 ----> 10  
  y = x               1 ----> 20  
  y = x[1:]          2 ----> 30  
                    3 ----> 40
```

Careful!

```
x = [10,20,30,40]   x --> 0 ----> 10
y = x              1 ----> 20
● y = x[1:]        2 ----> 30
                  3 ----> 40

y --> 0 ----> 20
      1 ----> 30
      2 ----> 40
```

Void Functions

```
● x = [40,20,10,30] x --> 0 ----> 40
y = x.sort()        1 ----> 20
                   2 ----> 10
                   3 ----> 30

y -->
```

Void Functions

```
x = [40,20,10,30]   x --> 0 ----> 10
● y = x.sort()      1 ----> 20
                   2 ----> 30
                   3 ----> 40

y --> None
```

Void Functions return None, a special type

Void Functions

```
x = [40,20,10,30]   x --> 0 ----> 40
● y = list(x)        1 ----> 20
y.sort()             2 ----> 10
                   3 ----> 30

y --> 0 ----> 40
      1 ----> 20
      2 ----> 10
      3 ----> 30
```

Void Functions return None, a special type

Void Functions

```
x = [40,20,10,30]   x --> 0 ----> 40
y = list(x)         1 ----> 20
● y.sort()          2 ----> 10
                   3 ----> 30

y --> 0 ----> 10
      1 ----> 20
      2 ----> 30
      3 ----> 40
```

Void Functions return None, a special type

Understanding Function Calls

```
def f(x):
    x = x[1:]
    print x

if __name__ == '__main__':
    u = [1,2,3,4]
    f(u)
    print u
```

Looks like f deletes the 0-th character in x

Understanding Function Calls

```
def f(x):  
    x = x[1:]  
    print x  
  
if __name__ == '__main__':  
    u = [1,2,3,4]  
    f(u)  
    print u
```

```
u --> 0 ---> 1  
      1 ---> 2  
      2 ---> 3  
      3 ---> 4
```

Follow the red dot and watch for impact...

Understanding Function Calls

```
def f(x):  
    x = x[1:]  
    print x  
  
if __name__ == '__main__':  
    u = [1,2,3,4]  
    f(u)  
    print u
```

```
u --> 0 ---> 1  
      1 ---> 2  
      2 ---> 3  
      3 ---> 4
```

```
x
```

Parameter x initially refers to the same object as u

Understanding Function Calls

```
def f(x):  
    x = x[1:]  
    print x  
  
if __name__ == '__main__':  
    u = [1,2,3,4]  
    f(u)  
    print u
```

```
u --> 0 ---> 1  
      1 ---> 2  
      2 ---> 3  
      3 ---> 4
```

```
x --> 0 ---> 2  
      1 ---> 3  
      2 ---> 4
```

x[1:] creates a new object and x will refer to it

Understanding Function Calls

```
def f(x):  
    x = x[1:]  
    print x  
  
if __name__ == '__main__':  
    u = [1,2,3,4]  
    f(u)  
    print u
```

```
u --> 0 ---> 1  
      1 ---> 2  
      2 ---> 3  
      3 ---> 4
```

```
x --> 0 ---> 2  
      1 ---> 3  
      2 ---> 4
```

2 3 4 is printed

Understanding Function Calls

```
def f(x):  
    x = x[1:]  
    print x  
  
if __name__ == '__main__':  
    u = [1,2,3,4]  
    f(u)  
    print u
```

```
u --> 0 ---> 1  
      1 ---> 2  
      2 ---> 3  
      3 ---> 4
```

```
x --> 0 ---> 2  
      1 ---> 3  
      2 ---> 4
```

1 2 3 4 is printed

Some Inadvertent Errors

```
>>> x = [10,20,30]  
>>> y = [11,21,31]  
>>> z = x+y  
>>> print z  
[10,20,30,11,21,31]
```

Some Inadvertent Errors

```
>>> x = [10,20,30]
>>> y = 3*x
>>>Print y
[10,20,30,10,20,30,10,20,3]
```

List Comprehensions

A short cut for setting up "simple" lists

```
>>> x = [i for i in range(5)]
>>> print x
[0,1,2,3,4]
```

List Comprehensions

A short cut for setting up "simple" lists

```
>>> x = [1 for i in range(5)]
>>> print x
[1,1,1,1,1]
```

List Comprehensions

A short cut for setting up "simple" lists

```
>>> x = [math.sqrt(i) for i in range(5)]
>>> print x
[0,1,1.414,1.732,2.0]
```

Quickly: Lists of Strings

```
>>> x = ['Maine', 'Vermont', 'New York']
>>> a = x[1]
>>> print a
'Vermont'
>>> c = a[2]
>>> print c
'r'
>>> x[1][2]
'r'
```

Next Problem

Merging Two Sorted Arrays
Into a
Single Sorted Array

Example

x-> 12 33 35 45

y-> 15 42 55 65 75

z-> 12 15 33 35 42 45 55 65 75

x and y are input
They are sorted
z is the output

Merging Two Sorted Lists

x-> 12 33 35 45

y-> 15 42 55 65 75

z-> []

ix and iy
keep track
of where
we are in x
and y

ix: 0

iy: 0

Merging Two Sorted Lists

x-> 12 33 35 45

y-> 15 42 55 65 75

z-> []

ix: 0

iy: 0

Do we pick from x? $x[ix] \leq y[iy]$???

Merge

x-> 12 33 35 45

y-> 15 42 55 65 75

z-> 12

ix: 0

iy: 0

Yes. So update ix

Merge

x-> 12 33 35 45

y-> 15 42 55 65 75

z-> 12

ix: 1

iy: 0

Do we pick from x? $x[ix] \leq y[iy]$???

Merge

x-> 12 33 35 45

y-> 15 42 55 65 75

z-> 12 15

ix: 1

iy: 0

iz:

No. So update iy

Merge

x-> 12 33 35 45 ix: 1

↓

y-> 15 42 55 65 75 iy: 1

↓

z-> 12 15

Do we pick from x ?

$x[ix] \leq y[iy]$???

Merge

x-> 12 33 35 45 ix: 1

↓

y-> 15 42 55 65 75 iy: 1

↓

z-> 12 15 33

Yes. So update ix

Merge

x-> 12 33 35 45 ix: 2

↓

y-> 15 42 55 65 75 iy: 1

↓

z-> 12 15 33

Do we pick from x ?

$x[ix] \leq y[iy]$???

Merge

x-> 12 33 35 45 ix: 2

↓

y-> 15 42 55 65 75 iy: 1

↓

z-> 12 15 33 35

Yes. So update ix

Merge

x-> 12 33 35 45 ix: 3

↓

y-> 15 42 55 65 75 iy: 1

↓

z-> 12 15 33 35

Do we pick from x ?

$x[ix] \leq y[iy]$???

Merge

x-> 12 33 35 45 ix: 3

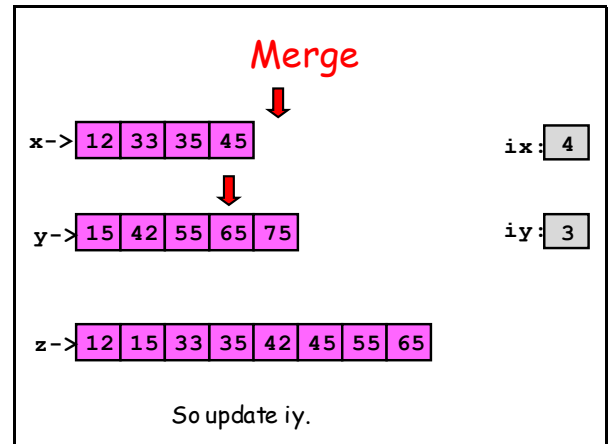
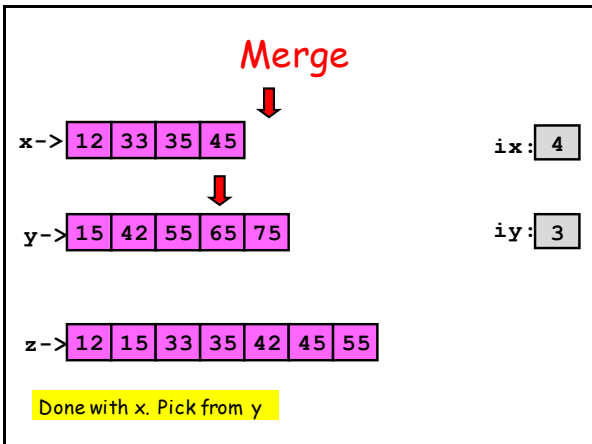
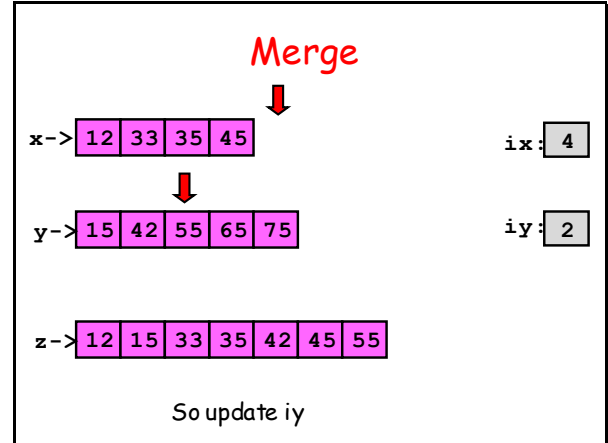
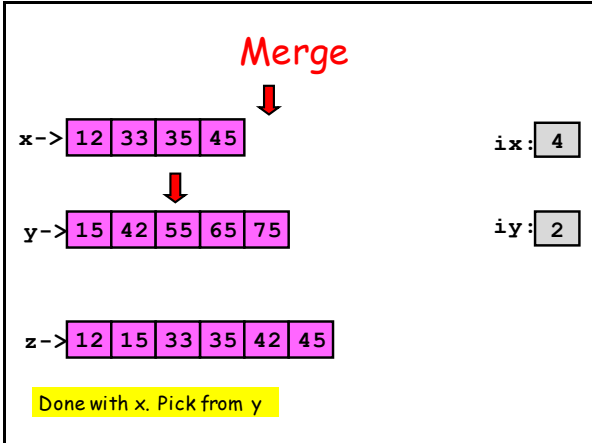
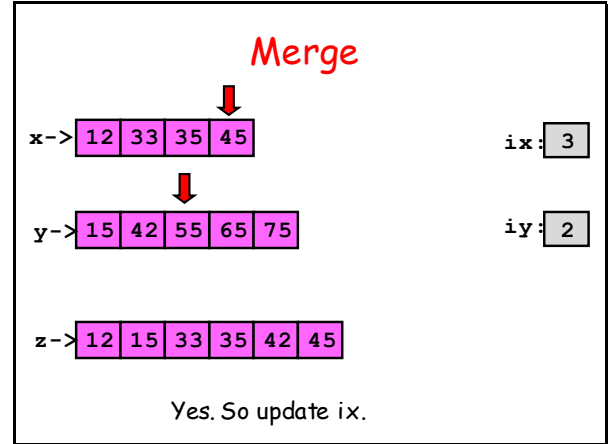
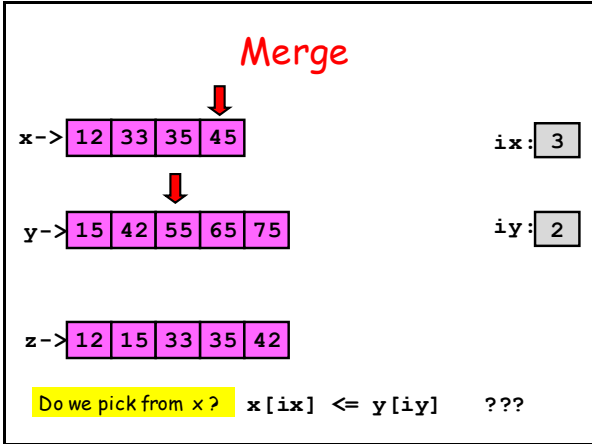
↓

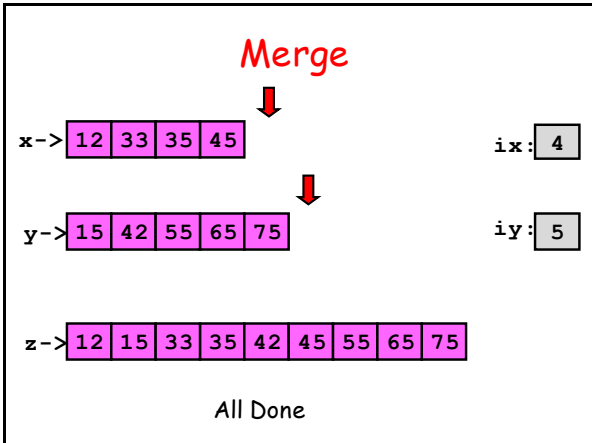
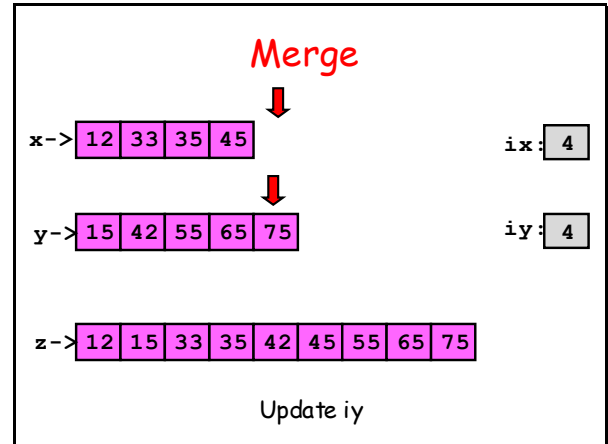
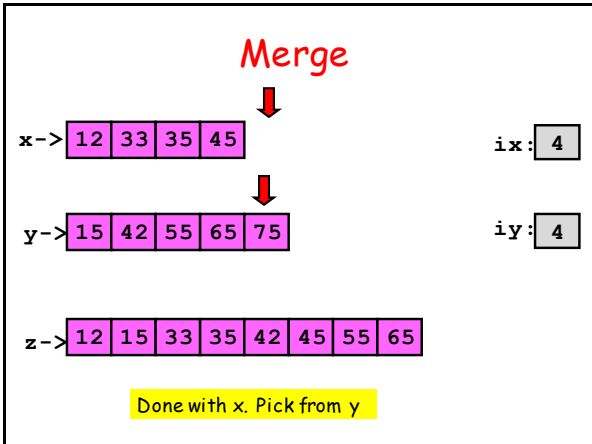
y-> 15 42 55 65 75 iy: 1

↓

z-> 12 15 33 35 42

No. So update iy...





The Python Implementation...

```
def Merge(x,y):
    n = len(x); m = len(y);
    ix = 0; iy = 0; z = []
    for iz in range(n+m):
        if ix >= n:
            z.append(y[iy]); iy+=1
        elif iy >= m:
            z.append(x[ix]); ix+=1
        elif x[ix] <= y[iy]:
            z.append(x[ix]); ix+=1
        elif x[ix] > y[iy]:
            z.append(y[iy]); iy+=1
    return z
```

Build z up via repeated appending

x-list exhausted

y-list exhausted

x-value smaller

y-value smaller

```
def Merge(x,y):
    n = len(x); m = len(y);
    ix = 0; iy = 0; z = []
    for iz in range(n+m):
        if ix >= n:
            z.append(y[iy]); iy+=1
        elif iy >= m:
            z.append(x[ix]); ix+=1
        elif x[ix] <= y[iy]:
            z.append(x[ix]); ix+=1
        elif x[ix] > y[iy]:
            z.append(y[iy]); iy+=1
    return z
```

len(x)+len(y) is the total length of the merged list

x-list exhausted

y-list exhausted

x-value smaller

y-value smaller

Implementation Using Pop

```
def Merge(x, y):  
    u = list(x)      Make copies of the  
    v = list(y)      Incoming lists  
    z = []  
    while len(u)>0 and len(v)>0 :  
        if u[0]<= v[0]:  
            g = u.pop(0)  
        else:  
            g = v.pop(0)  
        z.append(g)  
    z.extend(u)  
    z.extend(v)  
    return z
```

Implementation Using Pop

```
def Merge(x, y):  
    u = list(x)      Build z up via  
    v = list(y)      repeated appending  
    z = []  
    while len(u)>0 and len(v)>0 :  
        if u[0]<= v[0]:  
            g = u.pop(0)  
        else:  
            g = v.pop(0)  
        z.append(g)  
    z.extend(u)  
    z.extend(v)  
    return z
```

Implementation Using Pop

```
def Merge(x, y):  
    u = list(x)      Every "pop" reduces the  
    v = list(y)      length by 1. The loop shuts  
    z = []           down when one of u or v is  
                    exhausted  
    while len(u)>0 and len(v)>0 :  
        if u[0]<= v[0]:  
            g = u.pop(0)  
        else:  
            g = v.pop(0)  
        z.append(g)  
    z.extend(u)  
    z.extend(v)  
    return z
```

Implementation Using Pop

```
def Merge(x, y):  
    u = list(x)  
    v = list(y)      g gets the popped value  
    z = []           and it is appended to z  
    while len(u)>0 and len(v)>0 :  
        if u[0]<= v[0]:  
            g = u.pop(0)  
        else:  
            g = v.pop(0)  
        z.append(g)  
    z.extend(u)  
    z.extend(v)  
    return z
```

Implementation Using Pop

```
def Merge(x, y):  
    u = list(x)  
    v = list(y)  
    z = []  
    while len(u)>0 and len(v)>0 :  
        if u[0]<= v[0]:  
            g = u.pop(0)  
        else:  
            g = v.pop(0)  
        z.append(g)  
    z.extend(u)      Add what is left in u.  
    z.extend(v)      OK if u is the empty list  
    return z
```

Implementation Using Pop

```
def Merge(x, y):  
    u = list(x)  
    v = list(y)  
    z = []  
    while len(u)>0 and len(v)>0 :  
        if u[0]<= v[0]:  
            g = u.pop(0)  
        else:  
            g = v.pop(0)  
        z.append(g)  
    z.extend(u)      Add what is left in v  
    z.extend(v)      OK if v is the empty list  
    return z
```