#### 11. More on While and Boolean-Valued Functions

Topics:

Reasoning about While Loops Designing Boolean-Valued Functions

#### Four Examples

- 1. Random Walk
- 2. Fibonacci numbers and the Golden Ratio
- 3. A Spiral Problem
- 4. Detecting streaks in a coin toss sequence



#### Random Walk

```
from random import randint as randi
x = 0
while abs(x)<=5:
    r = randi(1,2)
    if r == 1:
        x = x+1
    else:
        x = x-1</pre>
```



















































# 2. Fibonacci Numbers and the Golden Ratio

#### Fibonacci Numbers and the Golden Ratio

Here are the first 12 Fibonacci Numbers

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144

The Fibonacci ratios 1/1, 2/1, 3/2, 5/3, 8/5 get closer and closer to the "golden ratio"

phi = (1 + sqrt(5))/2



### Generating Fibonacci Numbers

Here are the first 12 Fibonacci Numbers 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144 Starting here, each one is the sum of its two predecessors

















## Generating Fibonacci Numbers



#### Generating Fibonacci Numbers

	$\mathbf{x} = 0$
$\mathbf{x} = 0$	print x
print x	y = 1
y = 1	print y
print y	$\mathbf{k} = 0$
<pre>for k in range(6):</pre>	while k<6:
z = x+y	z = x+y
$\mathbf{x} = \mathbf{y}$	х = у
y = z	$\mathbf{y} = \mathbf{z}$
print z	print z
	$\mathbf{k} = \mathbf{k} + 1$
L	















3. A Spiral Problem



A Spiral Problem

Recall:

DrawSpiral(N,t,c1,c2,c3)

draws a spiral and

SpiralRadius(N,t)

computes its radius.

#### The Gist of SpiralRadius

```
xc = 0; yc = 0; r = 0
for k in range(N):
    theta = (k*t)*math.pi/180
    L = k+1
    # (xc,yc) = end of the kth edge
    xc = xc + L*math.cos(theta)
    yc = yc + L*math.sin(theta)
    dist = math.sqrt(xc**2+yc**2)
    r = max(r,dist)
return r
```













#### A Reverse Problem

Given the turn angle  ${\tt t}$  and a radius  ${\tt r},$  what is the largest  ${\tt N}$  so that

DrawSpiral(N,t,c1,c2,c3)

fits inside the circle

x\*\*2 + y\*\*2 = r\*\*2









```
k = 0
xc = 1
yc = 0
d = math.sqrt(xc**2 + yc**2)
while d<=r:
    k = k+1
    theta = (k*t)*math.pi/180
    xc = xc + (k+1)*math.cos(theta)
    yc = yc + (k+1)*math.sin(theta)
    d = math.sqrt(xc**2 + yc**2)
return k-1</pre>
```











s[k:k+n] is a length-n streakif
(1) k+n <= len(s)
and
(2) It is either all T's or all H's
and
(3) If there is a character before
 s[k], it is different from s[k].
and
(4) If there is a character after
 s[k+n], it is different from s[k+n].</pre>











## Using isStreak to Find Streaks s = `HHTHTTTHTHHHTHTT' k isSTreak(s,k,3) 0 False 1 False 2 False 3 False

#### Using isStreak to Find Streaks

#### s = `HHTHTTTHTHHHHTHTT'

#### k isSTreak(s,k,3)

0	False

- False False
- 3 False 4 True

1

2

#### Using isStreak to Find Streaks

```
def FindStreak(s,n):
    k=0
    while k<len(s) and (not isStreak(s,k,n)):
        # s[k:k+n] is not a streak
        k = k+1
    if k<len(s):
        # isStreak(s,k,n) is True
        return k
else:
        # k==len(s) is True
        return -1</pre>
```