# 9. Random Simulations

Topi cs:

The class random Estimating probabilities Estimating averages More occasions to practice iteration

#### The random Module

Contains functions that can be used in the design of random simulations.

We will practice with these:

random.randint(a,b)
random.uniform(a,b)

random.normalvariate(mu,sigma)

And as a fringe benefit, more practice with for-loops

## Generating Random Integers

If a and  $\mathbf{b}$  are initialized integers with a <  $\mathbf{b}$  then

i = random.randint(a,b)

assigns to i a "random" integer that satisfies

a <= i <= b

That is, we randomly select an element from the set {a,a+1,...,b} and assign it to n

## What Does "Random" Mean?

import random
for k in range(1000000):
 i = random.randint(1,6)
 print i

The output would "look like" you rolled a dice one million times and recorded the outcomes.

No discernible pattern.

Roughly equal numbers of 1's, 2's, 3's, 4's, 5's, and 6's.



# **Random Simulation**

We can use randint to simulate genuinely random events, e.g.,

Flip a coin one million times and record the number of heads and tails.







Sample Outputs		
N = 1000000		
Heads = 500636	Different runs produce	
Tails = 499364	different results.	
	This is consistent with	
N = 1000000	what would happen if	
Heads = 499354	coin one million times.	
Tails = 500646		



#### Dice Roll

```
from random import randint as randi
N = 6000000
count = 0
for k in range(N):
    i = randi(1,6)
    if i==5:
        count+=1
prob = float(count)/float(N)
print N, count, prob
```









Sample Output		
k	count/k	
100000 200000 300000 400000 500000 600000 700000 800000 900000	0.554080 0.555125 0.555443 0.555512 0.555882 0.555750 0.555901 0.555912 0.555841	Note how we say "sample output" because if the script is run again, then we will get different results. Educated guess true prob = 5/9









# Estimating Pi Using random.uniform(a,b)

Idea:

Set up a game whose outcome tells us something about pi.

This problem solving strategy is called Monte Carlo. It is widely used in certain areas of science and engineering









# Repeatability of Experiments

In science, whenever you make a discovery through experimentation, you must provide enough details for others to repeat the experiment.

We have "discovered" pi through random simulation. How can others repeat our computation?





#### An Example that Uses Both randi and randu

Repeat:

- 1. Position a square randomly in the figure window.
- 2. Choose its side length randomly.
- 3. Determine its tilt randomly
- 4. Color it cyan, magenta, or, yellow randomly.















# Developing For-Loop Solutions Illustrate the thinking associated with the design of for-loops Again we illustrate the methodology of <u>stepwise refinement</u>. An example...

## A Game: TriStick

Pick three sticks each having a random length between zero and one.

You win if you can form a triangle whose sides are the sticks. Otherwise you lose.



#### Problem

Estimate the probability of winning a game of TriStick by simulating a million games and counting the number of wins.





# Key Problem-Solving Strategy

Progress from pseudocode to Python through a sequence of refinements.

Comments have an essential role during the transitions. They remain all the way to the finished code.



# Generating floats from the Normal Distribution

If mu and sigma (positive) are floats, then

x = random.normalvariate(mu,sigma)

assigns to  ${\bf x}$  a "random" float sampled from the normal distribution with mean mu and standard deviation sigma



#### Typical Situation: Test Scores

from random import normalvariate as randn for k in range(450): x = randn(70,7)print round(x)

This would look like a report of test scores from a class of 450 students.

The mean is approximately 70 and the standard deviation is approximately 7.









70.007824 6.998934

ApproxSTD = sqrt(float(sum2)/float(N))

Sample Output:

# Final Reminder

randi, randu, and randn are RENAMED
versions of

random.randint
random.uniform
random.normalvariate