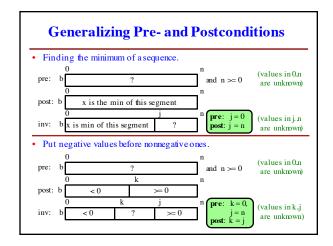
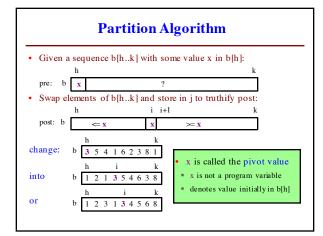


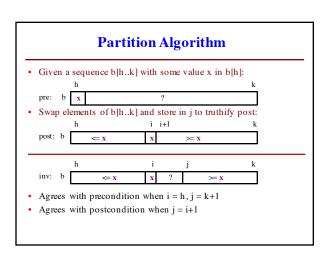
## **Developing Algorithms on Sequences**

- Specify the algorithm by giving its precondition and postcondition as pictures.
- Draw the invariant by drawing another picture that "generalizes" the precondition and postcondition
  - The invariant is true at the beginning and at the end
- The four loop design questions (memorize them)
  - 1. How does loop start (how to make the invariant true)?
  - 2. How does it stop (is the postcondition true)?
  - 3. How does the body make progress toward termination?
  - 4. How does the body keep the invariant true?

# 







#### **Partition Algorithm Implementation** def partition(b,h,k): """Partition list b[h..k] around apivot x = b[h]""" i = h; j = k+1; x = b[h]# invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= x while i < j-1: if b[i+1] >= x: partition(b,h,k), not partition(b[h:k+1]) #Move to end of block Remember, slicing always copies the list! \_swap(b,i+1,j-1) We want to partition the original list j=j-1 else: #b[i+1] < x \_swap(b,i,i+1) i = i + 1post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= x

### **Partition Algorithm Implementation** def partition(b,h,k): """Partition list b[h..k] around apivot x = b[h]"" i = h; j = k+1; x = b[h]1 2 3 1 5 0 6 3 8 # invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= x while i < j-1: if b[i+1] >= x: # Move to end of block \_swap(b,i+1,j-1) j=j-1 else: # b[i+1] < x \_swap(b,i,i+1) i = i + 1post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= xreturn i

#### **Partition Algorithm Implementation** def partition(b,h,k): """Partition list b[h..k] around apivot x = b[h]"" i = h; j = k+1; x = b[h]1 2 3 1 5 0 6 3 8 # invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= xwhile i < j-1: i⊬l if b[i+1] >= x: 1 3 5 0 6 3 8 $\#\operatorname{Move}$ to end of block \_swap(b,i+1,j-1) j=j-1 se: #b[i+1] < x 1 2 1 3 0 5 6 3 8 \_swap(b,i,i+1) i = i + 1post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= x1 0 3 5 6 3 8

