

# CS1110

## Lecture 23: **Prelim 2 Review Session**

### Announcements

All regrade requests for prelim 1 and A2 have been processed and the hardcopies are back in the homework handback room, Gates 216 (open noon-4pm on weekdays; bring ID).

No change in CMS grade means that we elected not to change your grade.



KEEP  
CALM  
AND  
READ the SPECS  
AGAIN

# Notes

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1. Always carefully read the specs (**and class invariants, and ...**), and re-read them after finishing a problem.  
In doubt? *Ask!*
2. Check your code against any examples we give you.
3. When ask you to solve a problem a certain way (i.e., recursively), the intent is for us to see if you understand that implementation method.  
(Ex: don't use a loop if we ask for recursion.)
4. If we don't ask for an invariant, you do not need to provide one.

# Provide a *recursive* implementation

---

```
def merge(s1,s2):
```

```
    """Given s1 & s2 strings with characters in alphabetical order,  
        return a string equivalent to the sorted concatenation.
```

```
    Examples: merge('ab', '') → 'ab'
```

```
              merge('abbce', 'cdg') → 'abbccdeg' """
```

```
# Compare characters with =, >, and <.
```

# Provide a *recursive* implementation

---

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def merge(s1,s2):
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    """Given s1 & s2 strings with characters in alphabetical order,  
        return a string equivalent to the sorted concatenation.
```

```
    Examples: merge('ab', '') → 'ab'
```

```
              merge('abbce', 'cdg') → 'abbccdeg' """
```

```
    # Compare characters with =, >, and <.
```

```
    if s1 == '' or s2 == '':
```

```
        return s1 + s2
```

```
    if s1[0] <= s2[0]:      # Pick first from s1 and merge the rest
```

```
        return s1[0]+merge(s1[1:],s2)
```

```
    else:                  # Pick first from s2 and merge the rest
```

```
        return s2[0]+merge(s1,s2[1:])
```

# Provide a recursive implementation

---

**def** skip(s):

"""Returns: copy of string s, odd letters (i.e., 1<sup>st</sup>, 3<sup>rd</sup>, 5<sup>th</sup>) dropped.

Example: 'abcd' -> 'bd'. '' -> '' 'abc' -> 'b', 'zzz' -> 'z' """

# Provide a recursive implementation

---

**def** skip(s):

"""Returns: copy of string s, odd letters (i.e., 1<sup>st</sup>, 3<sup>rd</sup>, 5<sup>th</sup>) dropped.

Example: 'abcd' -> 'bd'. '' -> '' 'abc' -> 'b', 'zzz' -> 'z' """

if len(s) <= 1: # One base case

return ''

else: # s >= 2 characters (if exactly 2, another base case)

return s[1] + (skip(s[2:]) if len(s) > 2 else '')

# Provide a for-loop implementation

---

**def** skip(s):

"""Returns: copy of string s, odd letters (i.e., 1<sup>st</sup>, 3<sup>rd</sup>, 5<sup>th</sup>) dropped.

Example: 'abcd' -> 'bd'. '' -> '' 'abc' -> 'b', 'zzz' -> 'z' """



# Provide a for-loop implementation

---

**def** skip(s):

"""Returns: copy of string s, odd letters (i.e., 1<sup>st</sup>, 3<sup>rd</sup>, 5<sup>th</sup>) dropped.

Example: 'abcd' -> 'bd'. '' -> '' 'abc' -> 'b', 'zzz' -> 'z' """

out = '' # progress towards output

# Inv: chars s[0..i-1] have been processed, s[i] is next to check

for i in range(len(s)): # i in 0..len(s) - 1

if i % 2 == 1:

out += s[i]

return out

# Provide a while-loop implementation

---

**def** skip(s):

"""Returns: copy of string s, odd letters (i.e., 1<sup>st</sup>, 3<sup>rd</sup>, 5<sup>th</sup>) dropped.

Example: 'abcd' -> 'bd'. '' -> '' 'abc' -> 'b', 'zzz' -> 'z' """

# Inv: chars s[0..i-1] have been processed. Done when i is len(s)

# Provide a while-loop implementation

---

**def** skip(s):

"""Returns: copy of string s, odd letters (i.e., 1<sup>st</sup>, 3<sup>rd</sup>, 5<sup>th</sup>) dropped.

Example: 'abcd' -> 'bd'.    '' -> ''    'abc' -> 'b', 'zzz' -> 'z'    """

out = "" # progress towards output

~~if len(s) <= 1:~~ # these two lines are optional

~~return out~~

i = 1

# Inv: chars s[0..i-1] have been processed. Done when i is len(s)

while i < len(s): # don't need parens around loop condition

    out += s[i]

    i += 2

return out

# Defining a class

---

```
class Paper(object):
```

```
    """An instance is a scientific paper.
```

```
    Class variables:
```

```
    number [int]: number of papers that have been created. >= 0
```

```
    Instance variables:
```

```
    title [string]: title of this paper. At least one char long.
```

```
    cites [list of Papers]: papers that this paper cites
```

```
    cited_by [list of Papers]: papers that this paper is cited by
```

```
    """
```

```
    number = 0 # initial value is 0
```

```
def __init__(self, title, cites=None):
```

```
    """Initializer. A new paper with title <title>, citing the papers in list  
    <cites> (set to [] if <cites> is None, and should be a copy of <cites>  
    otherwise), and with cited_by set to []. This initializer should also  
    update the relevant attributes of any papers in the list <cites>. Pre:  
    arg values as in class specification."""
```

```
    # Don't forget to update the class variable.
```

# Write the body of `__init__`

---

```
def __init__(self, title, cites=None):
```

```
    # spec on previous slide
```

```
    self.title = title
```

```
    self.cites = ([] if cites is None else cites[:])
```

```
    for p in self.cites:
```

```
        p.cited_by.append(self)
```

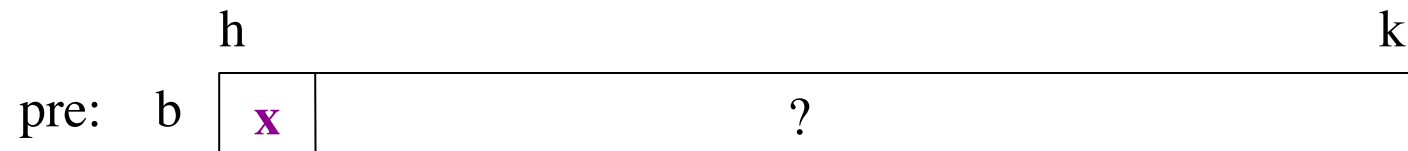
```
    self.cited_by = []
```

```
    Paper.number += 1 # note how to reference the class variable.
```

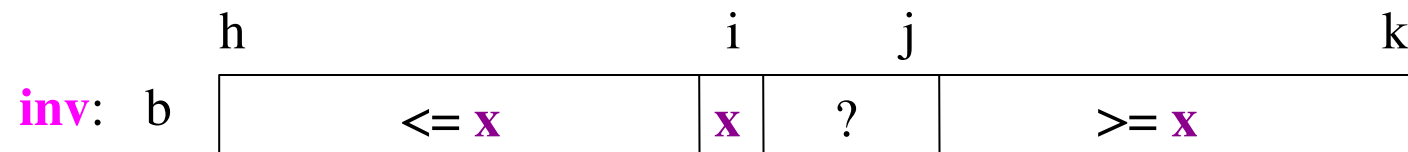
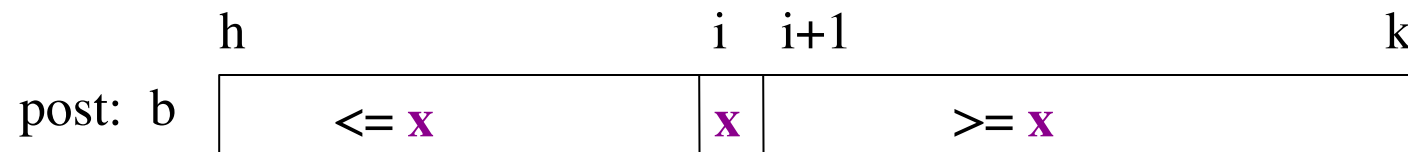
# Implement according to invariant

---

- Given a sequence  $b[h..k]$  with some value  $x$  in  $b[h]$ :



- Swap elements of  $b[h..k]$  and store in  $i$  to truthify post:



# Partition Algorithm Implementation

---

```
def partition(b, h, k):
```

```
    """Partition list b[h..k] around a pivot x = b[h]. Return i s.t. b[i] is x."""
```

```
    # invariant: b[h..i-1] <= b[i], b[j+1..k] >= b[i], b[i] is x
```



# Partition Algorithm Implementation

---

```
1. def partition(b, h, k):
2.     """Partition list b[h..k] around a pivot x = b[h]. . Return i s.t. b[i] is x"""
3.     i = h; j = k
4.     # inv: b[h..i-1] <= b[i], b[j+1..k] >= b[i], b[i] is x
5.     while i < j:
6.         if b[i+1] >= b[i]:
7.             # Move to end of block.
8.             b[i+1], b[j] = b[j], b[i+1]
9.             j = j - 1
10.        else: # b[i+1] < b[i]
11.            b[i], b[i+1] = b[i+1], b[i]
12.            i = i + 1
13.        # post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= x
14.    return i
```



**def** evaluate(p, x): """Returns: The evaluated polynomial p(x).

We represent polynomials as a list of **coefficients** (as floats):

[1.5, -2.2, 3.1, 0, -1.0] is  $1.5 - 2.2x + 3.1x^2 + 0x^3 - x^4$

We evaluate by substituting in for the value x. For example

$\text{evaluate}([1.5, -2.2, 3.1, 0, -1.0], 2) = 1.5 - 2.2(2) + 3.1(4) - 1(16) = -6.5$

$\text{evaluate}([2], 4) = 2$

Precondition: p is a list (len > 0) of floats, x is a float"""

# One implementation

---

```
def evaluate(p, x):  
    """(spec on previous slide)"""  
    sum = 0    # sum of all the coeffs*x**y for coeffs seen so far  
    xval = 1   #  $x^{*0} == 1$ ; value to multiply with next coeff yet unseen  
    for c in p: # c is next unseen coefficient  
        sum = sum + c*xval  
        xval = xval * x  
    return sum
```

# Alternate implementation

---

```
def evaluate(p, x):
```

```
    """(spec on previous slide)"""
```

```
    i=0; sum=0
```

```
    # Inv: sum is eval of p[0..i-1], i is next power to do
```

```
    while i < len(p):
```

```
        sum += p[i]*(x**i)
```

```
        i += 1
```

```
    return sum
```

# Alternate implementation

---

```
def evaluate(p, x):
```

```
    """(spec on previous slide)"""
```

```
    i=0; xval = 1; sum = p[i] # no point in multiplying by 1; showing
                             # i for clarity; it's not really necessary here
```

```
    i = 1
```

```
    while i < len(p):
```

```
        # Invariant: xval = x**(i-1); sum = eval(p[..i-1], x)
```

```
        xval *= x                # or, xval = xval*x
```

```
        sum += p[i]*xval        # or, sum = sum + p[i]*xval
```

```
        i += 1                  # or, i = i + 1
```

```
    return sum
```