

Review 5

Recursion

What We Will Do today

- Practice recursive specifications and functions
 - Given a recursive problem definition
 - Determine a proper specification (note preconditions)
 - Given a problem description and specification:
 - Write the recursive base case
 - Write the recursive call
 - Verify that it is correct

Questions?

Important Steps

1. Precise Specification

- What does the function do?
- What are the preconditions?

2. Write the base case

- What is the most basic case?
- What causes termination of the recursive function?

3. Write the recursive case

- How do we make progress toward termination?
- Is your computation correct?

Writing Specifications

Write a specification for a function that:

- Computes the complement of a positive integer.
i.e. The complement of 12345 is 98765.

- Reduce the positive input integer to a single digit.
i.e. $472 \rightarrow 47+2 = 49 \rightarrow 4+9 = 13 \rightarrow 1+3 = 4$

Writing Specifications

Write a specification for a function that:

- Computes the complement of a positive integer.
i.e. The complement of 12345 is 98765.

"""Returns: complement of n, by replacing each decimal digit of n by 10-n. ie. the result for 93723 is 17387.
Precondition: n > 0 an int, and no digit of n is 0"""

- Reduce the positive input integer to a single digit.
i.e. $472 \rightarrow 47+2 = 49 \rightarrow 4+9 = 13 \rightarrow 1+3 = 4$

"""Returns: n reduced to a single digit (summing its digits)
Precondition: n > 0 an int"""

Writing Specifications

Write a specification for a function that:

- Compresses a String so that duplicate are replaced with counts
i.e. aaabbbbbbbccd -> a3b6c2d1

- Converts an integer to a string representation with commas
i.e. 5923821 is converted to 5,923,821.

Writing Specifications

Write a specification for a function that:

- Compresses a String so that duplicate are replaced with counts
i.e. aaabbbbbbbccd -> a3b6c2d1

"""Returns: s compressed so that duplicates are replaced with count of how many occurrences that character has in a row.
Precondition: s a string"""

- Converts an integer to a string representation with commas
i.e. 5923821 is converted to 5,923,821.

"""Returns: String representation of n with commas added
Precondition: n an int (positive or negative)"""

Complement of an Integer

```
def complement(int n) {  
    """Returns: the complement of n, formed by replacing  
    each decimal digit of n by 10-n.  
    i.e. the result for the integer 93723 is 17387.  
    Precondition: n > 0 and int, and no digit of n is 0"""  
    # Base Case  
  
    # Recursive Case
```


Complement of an Integer

```
def complement(int n) {  
    """Returns: the complement of n, formed by replacing  
    each decimal digit of n by 10-n.  
    i.e. the result for the integer 93723 is 17387.  
    Precondition: n > 0 and int, and no digit of n is 0"""  
    # Base Case  
    if n < 10:  
        | return 10 - n  
  
    # Recursive Case  
    return complement(n/10) * 10 + (10 - n%10)
```

Adding Commas to an Integer

```
def add_commas(n):
```

```
    """Returns: string representation of n with commas added
```

```
    Precondition: n is an int (positive or negative)"""
```

```
    # Base case
```

```
    # Recursive Case
```

Adding Commas to an Integer

```
def add_commas(n):  
    """Returns: string representation of n with commas added  
    Precondition: n is an int (positive or negative)"""  
    # Base case  
    if n < 1000:  
        | return str(n)  
    # Recursive Case  
    number = str(n)  
    return add_commas(n/1000) + ',' + number[-3:0]
```

Is something wrong?

Adding Commas to an Integer

```
def add_commas(n):  
    """Returns: n with commas added. Precondition: n is an int (positive or negative)"""  
    if n < 0:  
        return '-' + add_commas_helper(-n)  
    else:  
        return add_commas_helper(n)
```

```
def add_commas_helper(n):  
    """Returns: n with commas added. Precondition: n > 0 is an int"""  
    # Base case  
    if n < 1000:  
        return str(n)  
    # Recursive Case  
    number = str(n)  
    return add_commas_helper(n/1000) + ',' + number[-3:]
```

An extra problem...

```
class FacebookProfile(object):
    name = '' # String, name of this profile
    friends = [] # Friends lists; contents are FacebookProfile objects
```

We want to answer the question:

- Is this profile at most 6 degrees away from Kevin Bacon?
- In other words, is Kevin Bacon a friend of a friend of a friend of a friend of a friend of a friend of a friend?

Specification (Method inside class FacebookProfile):

```
def sixDegreesOfBacon(self):
    """Returns: True if this FacebookProfile is at most 6
    degrees away from Kevin Bacon; False otherwise"""
```

6-Degrees of Kevin Bacon

```
class FacebookProfile(object):
    ...
    def sixDegreesOfBacon(self):
        """Returns: True if this FacebookProfile is at most 6 degrees away from Kevin Bacon"""
        return _sixDegreesHelper(6)

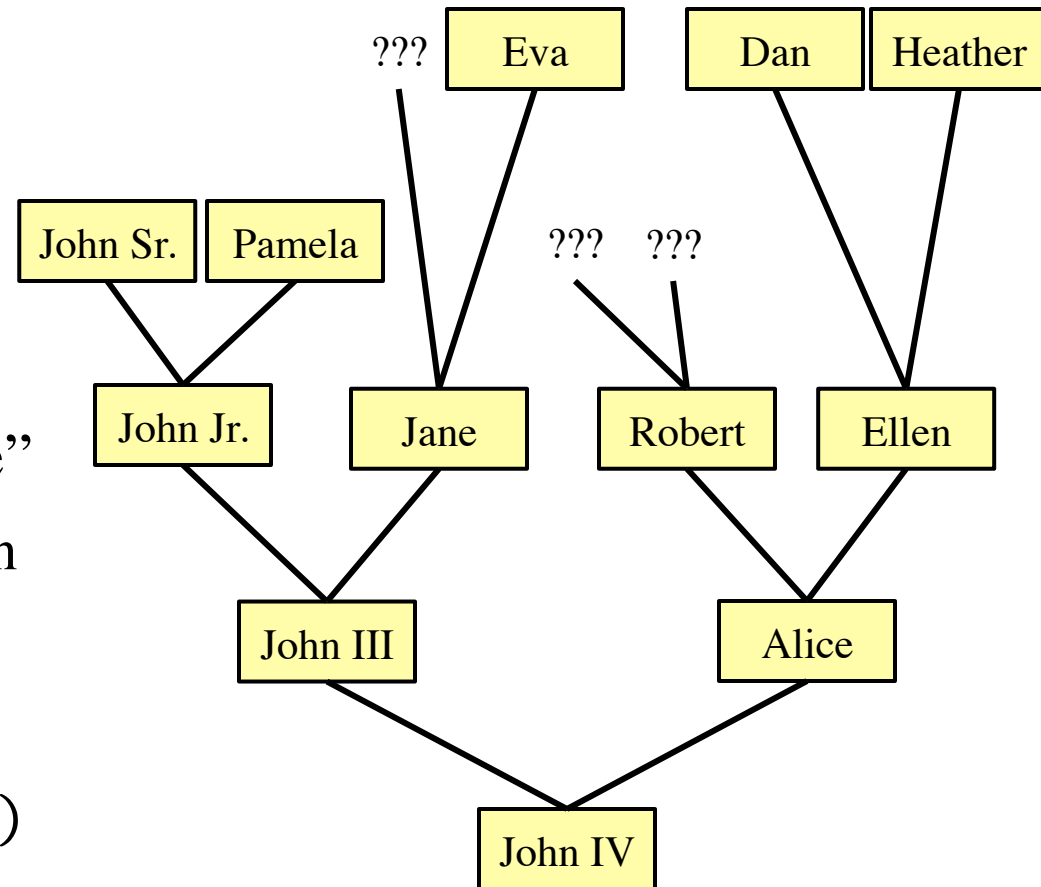
    def sixDegreesOfBacon(self,n):
        """Returns: True if this FacebookProfile is at most n degrees away from Kevin Bacon
        Precondition: n > 0 an int"""
        # Base case
        if (name = 'Kevin Bacon'):
            return True
        if n == 0:
            return False
        # Recursive Case
        for f in self.friends:
            if f._sixDegreesHelper(n-1):
                return True
        return False
```

Extra Problems

- Given a list, use recursion to determine if it is sorted
- Given a String *s*, list all the permutations of String *s*:
 - “XZY” → “XYZ”, “XZY”, “Zyx”, “YXZ”, etc
- Use recursion to find the minimum element in a list

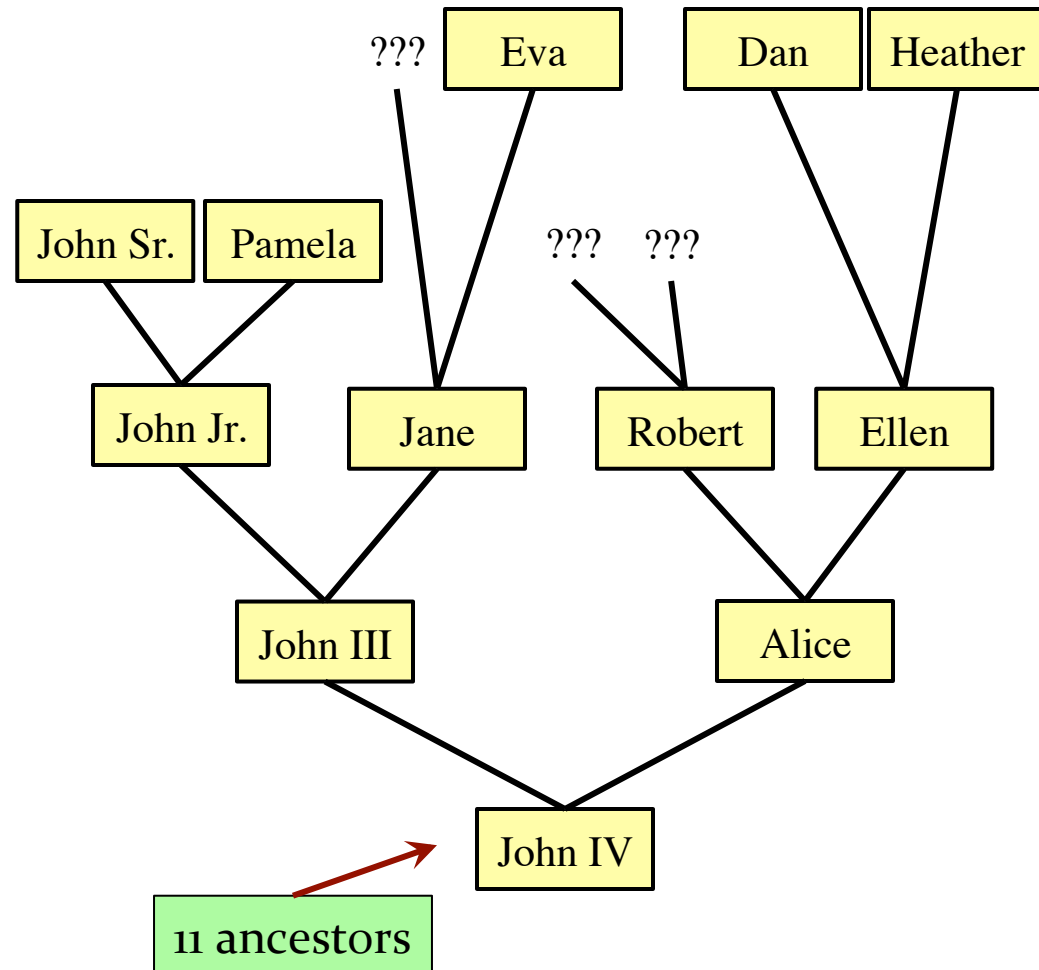
Recursion and Objects

- Class Person (person.py)
 - Objects have 3 attributes
 - `name`: String
 - `mom`: Person (or None)
 - `dad`: Person (or None)
- Represents the “family tree”
 - Goes as far back as known
 - Attributes `mom` and `dad` are None if not known
- **Constructor**: `Person(n,m,d)`
 - Or `Person(n)` if no `mom`, `dad`



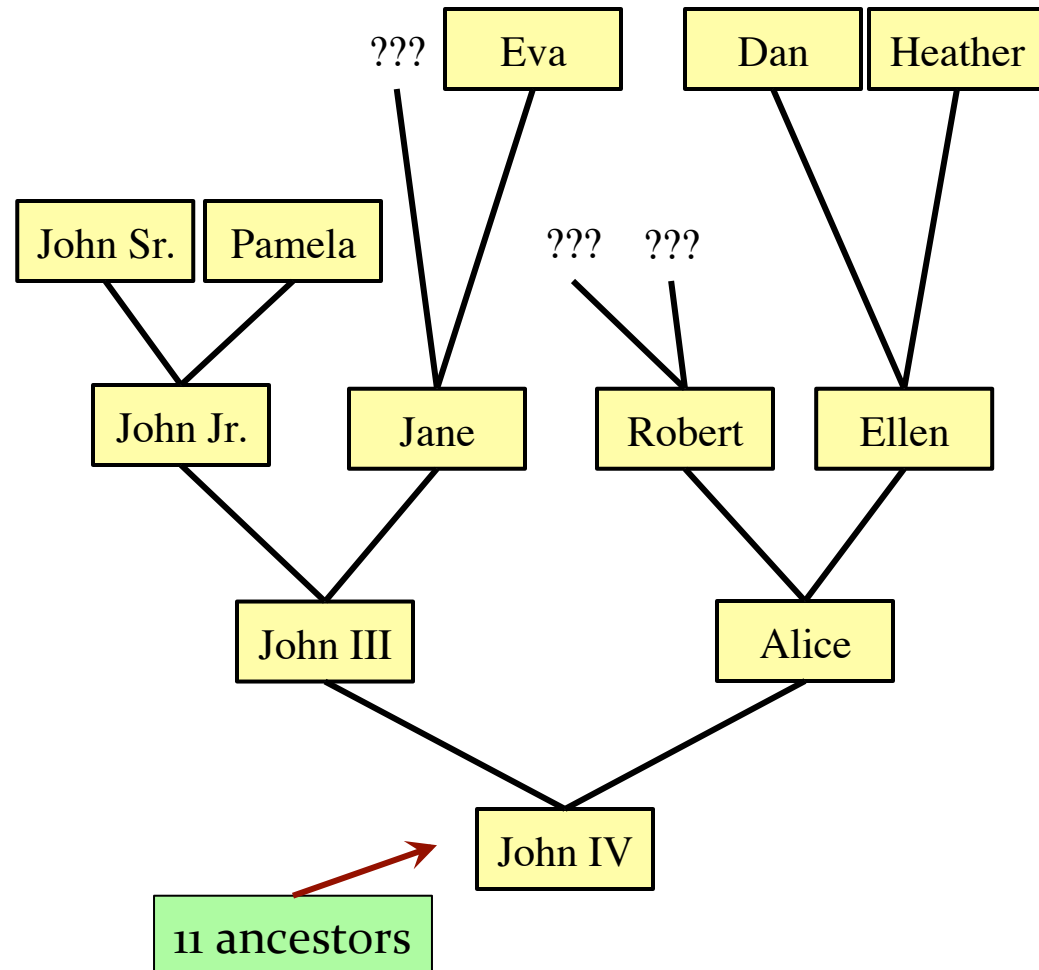
Recursion and Objects

```
def num_ancestors(p):  
    """Returns: num of known ancestors  
    Pre: p is a Person"""  
    # Base case  
    # No mom or dad (no ancestors)  
  
    # Recursive step  
    # Has mom or dad  
    # Count ancestors of each one  
    # (plus mom, dad themselves)  
    # Add them together
```



Recursion and Objects

```
def num_ancestors(p):  
    """Returns: num of known ancestors  
    Pre: p is a Person"""  
    # Base case  
    if p.mom == None and p.dad == None:  
        | return 0  
  
    # Recursive step  
    moms = 0  
    if not p.mom == None:  
        | moms = 1+num_ancestors(p.mom)  
    dads = 0  
    if not p.dad == None:  
        | dads = 1+num_ancestors(p.dad)  
    return moms+dads
```



Questions?