

Lecture 23

Multidimensional Arrays

Announcements for This Lecture

Material

- Section 9.1
 - Last new material for final!
- Section 12.1 next time
 - Relevant to assignment
 - But not on the exam
- Next week: wrapping up
- Review sessions in 2 weeks
 - Will announce next week

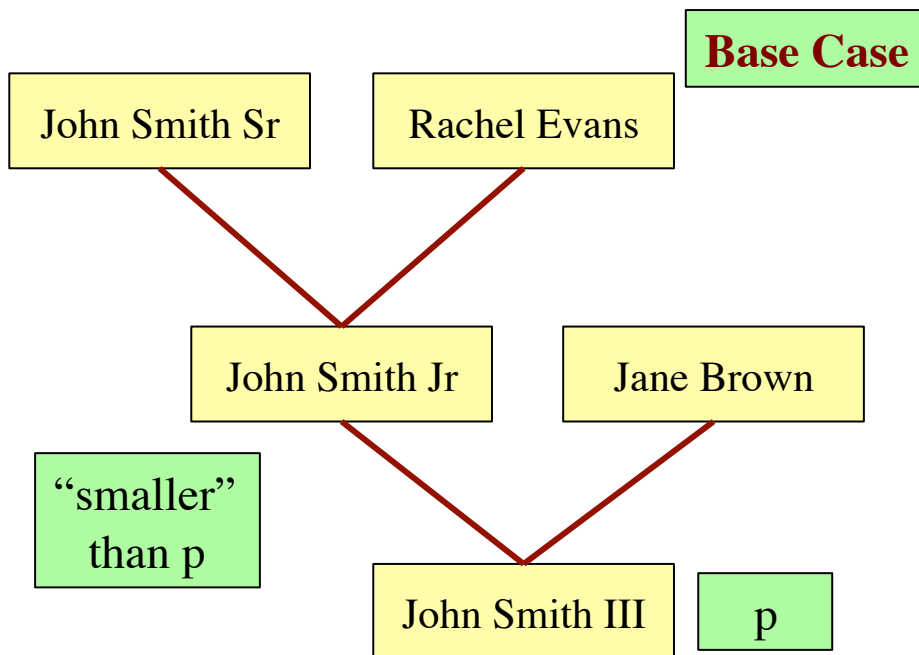
Assignments

- A6 still being graded
 - Having to “eyeball it”
 - Will take us this week
- Assignment A7 now posted
 - Last assignment of semester
 - Please meet suggested dates
 - Makes it manageable
 - Due Saturday after classes

Prelim II: How I Lowered the Mean

- **Progress to Termination**

- Arguments of recursive calls must somehow get “smaller”
- Each call closer to base case



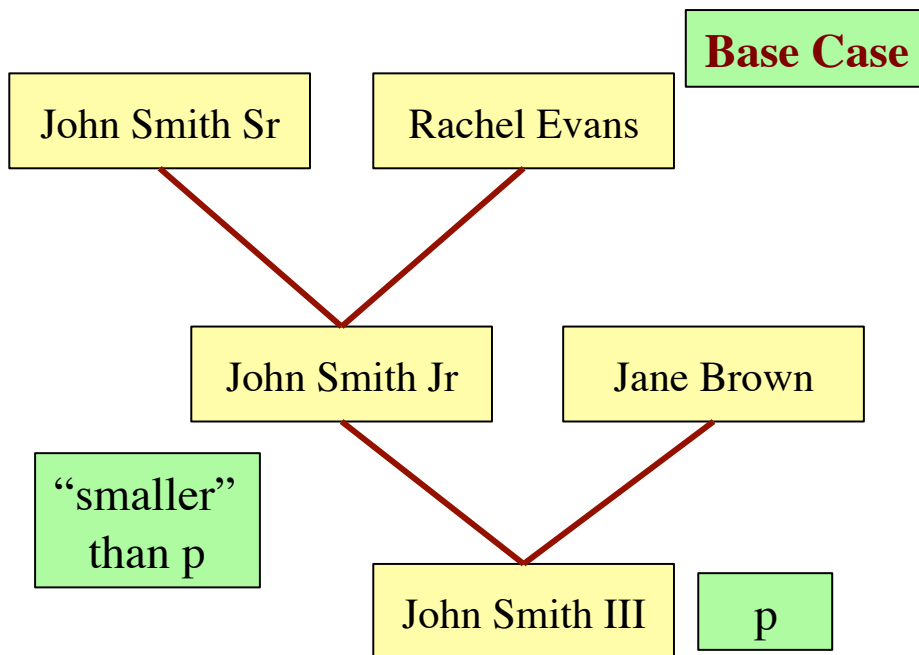
```
/** Yields: number of family members  
 * (including profile p and his/her  
 * ancestors) with given first name */  
public static int withName(Profile p,  
                           String s) {  
  
    int count =  
        (p.getName().equals(s) ? 1 : 0);  
  
    if (father != null)  
        count = count+withName(father,s);  
  
    if (mother != null)  
        count = count+withName(mother,s);  
    return count;  
}
```

Static Method

Prelim II: How I Lowered the Mean

- **Progress to Termination**

- Arguments of recursive calls must somehow get “smaller”
- Each call closer to base case



```
/** Yields: number of family members  
 * (including profile p and his/her  
 * ancestors) with given first name */  
public int withName(String s) {  
    int count =  
        (getName().equals(s) ? 1 : 0);  
  
    if (father != null)  
        count = count+father.withName(s);  
  
    if (mother != null)  
        count = count+mother.withName(s);  
    return count;  
}
```

Instance Method

What is Up with reveal1 in A6?

Try it Yourself

```
/** Extract and return ... */
public String reveal() {
    ...
    int p= 4;
    String result= "";

    // inv: All hidden chars before
    // pixel p are in result[0..k-1]
    for (int k= 0; k < len; k= k+1) {
        result= result +
            (char) (getHidden(p));
        p= p+1;
    }
    return result;
}
```

n^2 algorithm
(n is the length
of message)

```
/** Extract and return ... */
public String reveal() {
    ...
    int p= 4;
    char[] result= new char[len];

    // inv: All hidden chars before
    // pixel p are in result[0..k-1]
    for (int k= 0; k < len; k= k+1) {
        result[k]=
            (char) (getHidden(p));
        p= p+1;
    }
    return new String(result);
}
```

linear algorithm
(n time steps)

Overview of Two-Dimensional Arrays

- Type of d is `int[][]`

(“`int` array array” / “an array of `int` arrays”)

- To declare variable d:

```
int d[][];
```

- Create a new array and assign to d:

```
d = new int[5][4];
```

- Initializer for two-dimensional array:

```
int[][] d = {{5,4,7,3},{4,8,9,7},{5,1,2,3},{4,1,2,9},{6,7,8,0}};
```

		0	1	2	3
d	0	5	4	7	3
	1	4	8	9	7
	2	5	1	2	3
	3	4	1	2	9
	4	6	7	8	0

Overview of Two-Dimensional Arrays

- Access value in position at row 3, col 2:

`d[3][4]`

- Access value in position at row 3, col 2:

`d[3][2] = 8;`

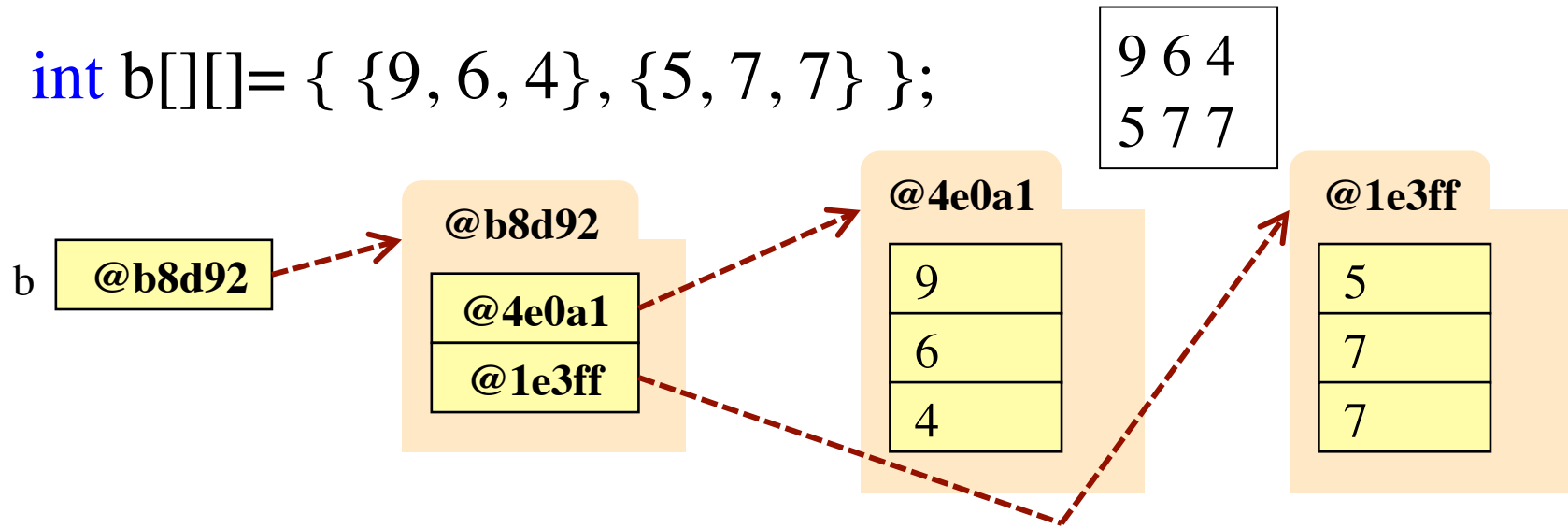
		0	1	2	3
d	0	5	4	7	3
	1	4	8	9	7
	2	5	1	2	3
	3	4	1	2	9
	4	6	7	8	0

Some Mysterious Features

- An odd symmetry
 - Number of rows of d: `d.length`
 - Number of columns in row r of d: `d[r].length`
- Also, try `toString(int[])` in the demo

How Multidimensional Arrays are Stored

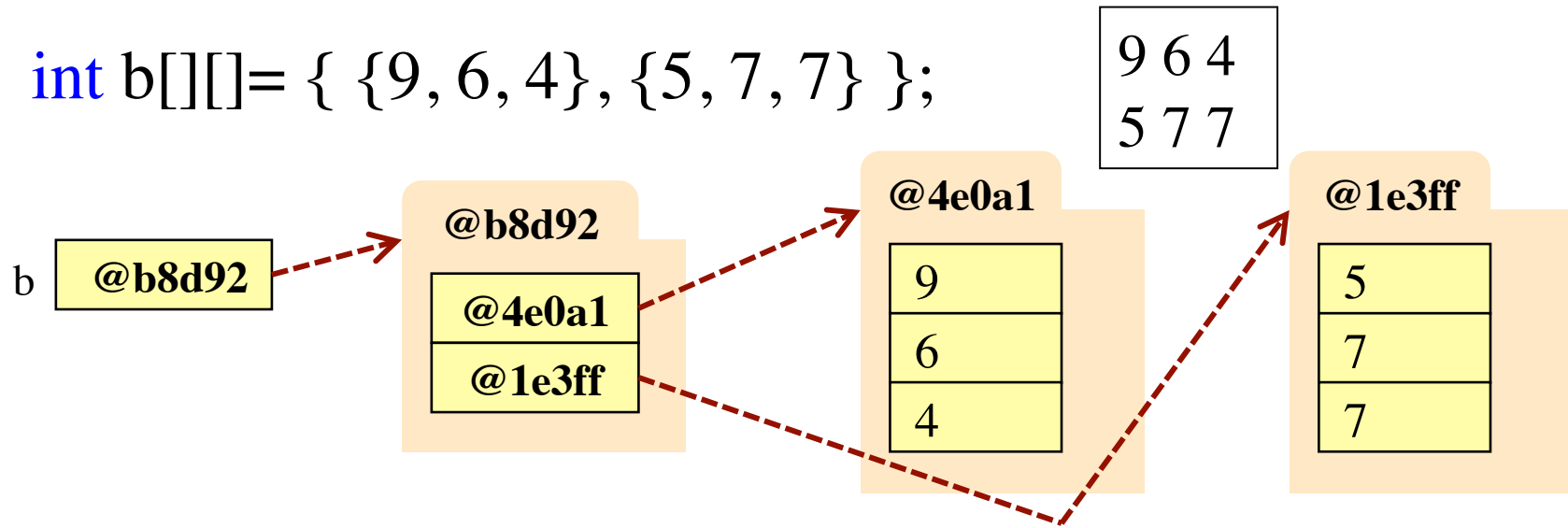
- `int b[][] = { {9, 6, 4}, {5, 7, 7} };`



- `b` holds name of a one-dimensional array object
 - Has `b.length` elements
 - Its elements are the names of 1D arrays
- `b[i]` holds the name of a one-dimensional array of **ints**
 - Has length `b[i].length`

How Multidimensional Arrays are Stored

- `int b[][] = { {9, 6, 4}, {5, 7, 7} };`



- `b` holds name of a one-dimensional array object
 - Has `b.length` elements
 - Its elements are the names of
- `b[i]` holds the name of a one-
 - Has length `b[i].length`

`java.util.Arrays.deepToString` recursively creates a String for all these arrays

Ragged Arrays: Rows w/ Different Length

- Declare variable b of type **int[][]**

```
int[][] b;
```

- Create a 1-D array of length 2 and store name in b

```
b= new int[2][] // Elements have int[] (and start as null)
```

- Create **int** array, store its name in b[0]

```
b[0]= new int[] {17, 13, 19};
```

- Create **int** array, store its name in b[1]

```
b[1]= new int[] {28, 95};
```

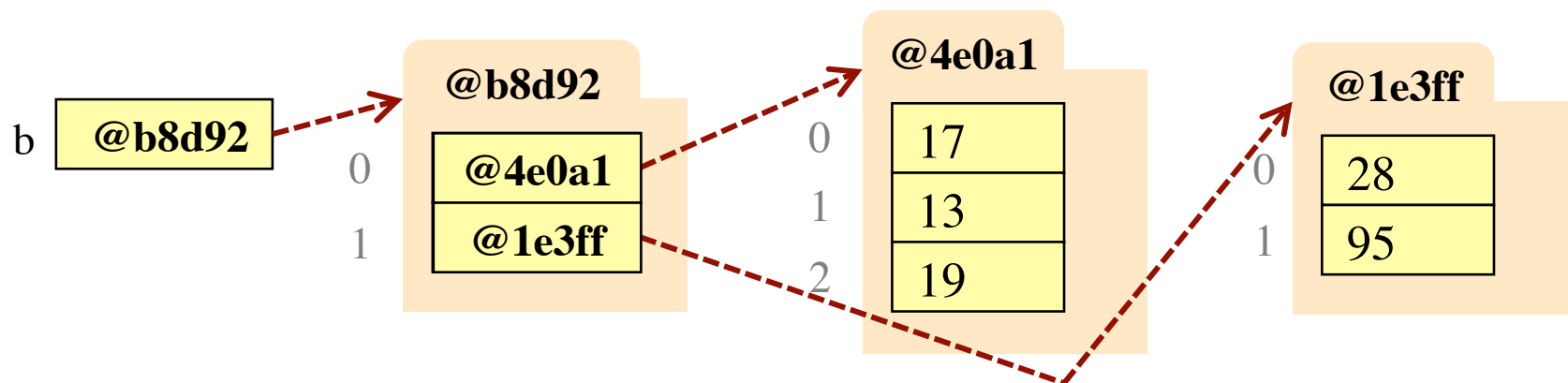
Ragged Arrays: Rows w/ Different Length

- Create **int** array, store its name in b[0]

```
b[0]= new int[] {17, 13, 19};
```

- Create **int** array, store its name in b[1]

```
b[1]= new int[] {28, 95};
```



Incomplete Initialization

- Sample Code:

```
int[][] b = new int[3][];
```

```
b[0] = new int[3];
```

```
b[0][0] = 2;
```

```
b[0][1] = 3;
```

```
b[1] = new int[2];
```

```
b[1][0] = 4;
```

```
b[1][1] = 5;
```

- What is b[0][2]?

A: 5

B: 0 (default int value)

C: null

D: None. Exception!

E: I don't know

Incomplete Initialization

- Sample Code:

```
int[][] b = new int[3][];
```

```
b[0] = new int[2];
```

```
b[0][0] = 2;
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b[0][1] = 3;
```

```
b[1] = new int[3];
```

```
b[1][0] = 4;
```

```
b[1][1] = 5;
```

- What is b[2][0]?

A: 5

B: 0 (default int value)

C: null

D: None. Exception!

E: I don't know

Aside: Image Array

- ImageArray used 1D array
 - Flattened version of 2D array
 - Simulated with $p = r * \text{length} + c$
- Uses less memory
 - Each row a folder in 2D array
 - ImageArray uses one folder
- Faster to access
 - 2D array needs 2 memory look-ups
 - 1D array is math+memory look-up
 - Computation faster than memory
- But 1D is harder to use

		0	1	2	3
a	0	5	4	7	3
	1	4	8	9	7
	2	5	1	2	3
	3	4	1	2	9
	4	6	7	8	0

b	5	4	7	3	4	8	9	7	...
---	---	---	---	---	---	---	---	---	-----

Pascal's Triangle

									0
									1
									2
									3
									4
									5
									...

- Creating the triangle:
 - The first and last entries on each row are 1.
 - Each other entry is the sum of the two entries above it
 - Row r has $r+1$ values.

Pascal's Triangle

										0
										1
										2
										3
										4
										5
										...

- Entry $p[i][j]$ = number of ways i elements can be chosen from a set of size j !
- $p[i][j] = \text{"i choose j"} = \binom{i}{j}$

Recursive formula:

$$\text{for } 0 < i < j, \quad p[i][j] = p[i-1][j-1] + p[i-1][j]$$

Pascal's Triangle

							0
			1				1
		1		1			2
	1		2		1		3
	1	3		3		1	4
1	4		6		4	1	5
1	5	10	10	5	1		...

- **Binomial Theorem:** Row r gives the coefficients of $(x + y)^r$
 - $(x + y)^2 = 1x^2 + 2xy + 1y^2$
 - $(x + y)^3 = 1x^3 + 3x^2y + 3xy^2 + 1y^3$
 - $(x + y)^r = \sum_{0 \leq k \leq r} \binom{r}{k} x^k y^{r-k}$

Ragged Arrays for Pascal's Triangle

```
/** Yields: ragged array of first n rows of Pascal's triangle. Precondition: 0 ≤ n */
public static int[][] pascalTriangle(int n) {
    int[][] b= new int[n][];    // First n rows of Pascal's triangle
    // invariant: rows 0..i-1 have been created
    for (int i = 0; i != b.length; i= i+1) {
        b[i]= new int[i+1];    // Create row i of Pascal's triangle
        b[i][0]= 1;            // Calculate row i of Pascal's triangle
        // invariant b[i][0..j-1] have been created
        for (int j= 1; j < i; j= j+1) {
            b[i][j]= b[i-1][j-1] + b[i-1][j];
        }
        b[i][i]= 1;
    }
    return b;
}
```

Summing Up a Multidimensional Array

```
/** Yields: Sum of elements of b.
```

```
* Precondition: b is an Integer or an array with base type Integer. */
```

```
public static int sum(Object b) {  
    if (b instanceof Object[]) {  
        Object[] bb= (Object[]) b;  
        int sum= 0;  
        //inv: sum = sum of b[0..k-1]  
        for (int k= 0; k < bb.length; k= k+1) {  
            sum= sum + sum(bb[k]);  
        }  
        return sum;  
    }  
    // { b has type Integer }  
    return 0 + (Integer) b;  
}
```

Recursive call
on nested array

Base Case