

While-Loops and Flow

```

print 'Before while'
count = 0
i = 0
while i < 3:
    print 'Start loop '+ i`
    count = count + i
    i = i + 1
    print 'End loop '
print 'After while'
    
```

Output:

```

Before while
Start loop 0
End loop
Start loop 1
End loop
Start loop 2
End loop
After while
    
```

Some Important Terminology

- assertion:** true-false statement placed in a program to *assert* that it is true at that point
 - Can either be a comment, or an **assert** command
- precondition:** assertion placed before a statement
 - Same idea as **function precondition**, but more general
- postcondition:** assertion placed after a statement
- loop invariant:** assertion supposed to be true before and after each iteration of the loop
 - Distinct from **attribute invariant**
- iteration of a loop:** one execution of its repetend

Assertions versus Asserts

- Assertions prevent bugs**
 - Help you keep track of what you are doing
- Also track down bugs**
 - Make it easier to check belief/code mismatches
- Do not confuse w/ asserts**
 - All asserts are assertions
 - But reverse is not true
 - Cannot always convert a comment to an assert

x is the sum of 1..n

Comment form of the assertion.

| | | | |
|---|---|---|---|
| x | ? | n | 1 |
| x | ? | n | 3 |
| x | ? | n | 0 |

Preconditions & Postconditions

```

# x = sum of 1..n-1
x = x + n
n = n + 1
# x = sum of 1..n-1
    
```

precondition

1 2 3 4 5 6 7 8
x contains the sum of these (6)

postcondition

1 2 3 4 5 6 7 8
x contains the sum of these (10)

Relationship Between Two
If **precondition** is true, then **postcondition** will be true

- Precondition:** assertion placed before a segment
- Postcondition:** assertion placed after a segment

Solving a Problem

```

# x = sum of 1..n
n = n + 1;
# x = sum of 1..n
    
```

precondition

What statement do you put here to make the postcondition true?

postcondition

A: x = x + 1
B: x = x + n
C: x = x + n+1
D: None of the above
E: I don't know

Invariants: Assertions That Do Not Change

- Loop Invariant:** an assertion that is true before and after each iteration (execution of repetend)

```

x = 0; i = 2;
while i <= 5:
    x = x + i*i
    i = i + 1
# x = sum of squares of 2..5
    
```

Invariant:
x = sum of squares of 2..i-1

in terms of the range of integers that have been processed so far

```

graph TD
    Start[i = 2] --> LoopBody[x = x + i*i  
i = i + 1]
    LoopBody --> Decision{i <= 5}
    Decision -- true --> LoopBody
    Decision -- false --> End[ ]
    
```

The loop processes the range 2..5

Invariants: Assertions That Do Not Change

```

x = 0; i = 2
# Inv: x = sum of squares of 2..i-1
while i <= 5:
    x = x + i*i
    i = i + 1
# Post: x = sum of squares of 2..5

```

Integers that have been processed: 2, 3, 4, 5
Range 2..i-1: 2..5

Invariant was always true just before test of loop condition. So it's true when loop terminates

Designing Integer while-loops

```

# Process integers in a..b
# inv: integers in a..k-1 have been processed
k = a
while k <= b:
    process integer k
    k = k + 1
# post: integers in a..b have been processed

```

Command to do something
Equivalent postcondition

Designing Integer while-loops

- Recognize that a range of integers b..c has to be processed
- Write the command and equivalent postcondition
- Write the basic part of the for-loop
- Write loop invariant
- Figure out any initialization
- Implement the repetend (process k)

```

# Process b..c
Initialize variables (if necessary) to make invariant true
# Invariant: range b..k-1 has been processed
while k <= c:
    # Process k
    k = k + 1
# Postcondition: range b..c has b

```

Finding an Invariant

```

# Make b True if no int in 2..n-1 divides n, False otherwise
b = True
k = 2
# invariant: b is True if no int in 2..k-1 divides n, False otherwise
while k < n:
    # Process k;
    if n % k == 0:
        b = False
    k = k + 1
# b is True if no int in 2..n-1 divides n, False otherwise

```

Command to do something
Equivalent postcondition

What is the invariant? 1 2 3 ... k-1 k k+1 ... n

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Finding an Invariant

```

# set x to # adjacent equal pairs in s[0..s.length()-1]
for s = 'ebee', x = 2
# invariant: ???
k = 0
while k < len(s):
    # Process k;
    k = k + 1
# x = # adjacent equal pairs in s[0..s.length()-1]

```

Command to do something
Equivalent postcondition

k: next integer to process.
Which have been processed?

What is the invariant?

| | |
|-----------------|--|
| A: 0..k | A: x = no. adj. equal pairs in s[1..k] |
| B: 1..k | B: x = no. adj. equal pairs in s[0..k] |
| C: 0..k-1 | C: x = no. adj. equal pairs in s[1..k-1] |
| D: 1..k-1 | D: x = no. adj. equal pairs in s[0..k-1] |
| E: I don't know | E: I don't know |

Be Careful!

```

# String s has at least 1 element
# Set c to largest element in s
c = ??
k = ??
# inv: c is largest element in s[0..k-1]
while k < len(s):
    # Process k
    k = k + 1
# c = largest char in s[0..s.length()-1]

```

Command to do something
Equivalent postcondition

- What is the invariant?
- How do we initialize c and k?

| |
|----------------------|
| A: k = 0; c = s[0] |
| B: k = 1; c = s[0] |
| C: k = 1; c = s[1] |
| D: k = 0; c = s[1] |
| E: None of the above |

An empty set of characters or integers has no maximum. Therefore, be sure that 0..k-1 is not empty. You must start with k = 1.