CS1110 29 March 2011 Developing array algorithms. Reading: 8.3..8.5

Important point: how we create the invariant, as a picture

Haikus (5-7-5) seen on Japanese computer monitors

Yesterday it worked. Today it is not working. Windows is like that.

Serious error. All shortcuts have disappeared. Screen. Mind. Both are blank.

A crash reduces Your expensive computer To a simple stone.

The Web site you seek Cannot be located, but Countless more exist.

Three things are certain: Death, taxes, and lost data. Guess which has occurred? Chaos reigns within. Reflect, repent, and reboot. Order shall return.

Prelim Thursday, 14 April, 7:30PM. Olin 155 and 255 Review session, Sunday, 10 April, 1–3. Phillips 101 Handout (coming later) describes what will be covered.

Quiz in class, Thursday, 31 March

Memorize the 4 loopy questions and be able to tell whether a given loop satisfies them or not.

Reason for quiz:

1. You need to understand the 4 loopy questions in order to understand the array algorithms we will be developing.

Developing algorithms on arrays

We develop several important algorithms on arrays.

With each, specify the algorithm by giving its precondition and postcondition as pictures.

Then, draw the invariant by drawing another picture that "generalizes" the precondition and postcondition, since the invariant is true at the beginning and at the end.

Four loopy questions —memorize them:

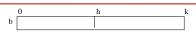
- 1. How does loop start (how to make the invariant true)?
- 2. When does it stop (when is the postcondition true)?
- 3. How does repetend make progress toward termination?
- 4. How does repetend keep the invariant true?

Horizontal notation for arrays, strings, Vectors

	0		k	b.lengtl
b	<=	sorted	>=	

Example of an assertion about an array b. It asserts that:

- 1. b[0..k-1] is sorted (i.e. its values are in ascending order)
- 2. Everything in b[0..k-1] is \leq everything in b[k..b.length-1]



Given the index h of the First element of a segment and the index k of the element that Follows the segment, the number of values in the segment is k-h.

b[h ... k-1] has k-h elements in it.



Generalize: To derive or induce (a general conception or principle) from particulars. To make general: render applicable to a wider class

Generalization: All dogs hate cats

square sides: equal angles: equal

rhombus sides: equal



rhombus is a generalization of square square is a particular kind of rhombus

problem: Tile an 8 x 8 kitchen

generalization: Tile a 2ⁿ x 2ⁿ kitchen (all using L-shaped tiles)

generalization: Tile an n x n kitchen

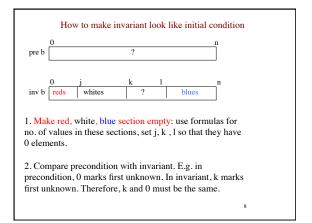
Invariant as picture: Generalizing pre- and post-condition Finding the minimum of an array. Given array b satisfying precondition P, store a value in x to truthify postcondition Q:



The invariant as picture: Generalizing pre- and post-condition Put negative values before nonnegative ones. Given is precondition P:

(values in 0..n-1 are unknown) (values in 0..k-1 are < 0,

values in k..n-1 are > 0)



Partition algorithm: Given an array b[h.k] with some value x in b[h]: h k

P: b x ?

Swap elements of b[h.k] and store in j to truthify Q: h j k

Q: b <= x | x | >= x

change: b $\frac{h}{3.54162381}$ into b $\frac{j}{121354638}$ or b $\frac{j}{123134568}$ x is called the pivot value.

x is not a program variable; x just denotes the value initially in b[h].

