## CS1110 4 November 2008

Developing array algorithms. Reading: 8.5

Important point: how we create the invariant, as a picture

## Haikus (5-7-5) seen on Japanese computer monitors

Yesterday it worked. Today it is not working. Windows is like that. Serious error. All shortcuts have disappeared. Screen. Mind. Both are blank.

A crash reduces Your expensive computer To a simple stone. The Web site you seek Cannot be located, but Countless more exist.

Three things are certain: Death, taxes, and lost data. Guess which has occurred? Chaos reigns within. Reflect, repent, and reboot. Order shall return.

## "generalizes" the precondition and postcondition, since the invariant is true at the beginning and at the end. Four loopy questions —memorize them:

and postcondition as pictures.

1. How does loop start (how to make the invariant true)?

Then, draw the invariant by drawing another picture that

Developing algorithms on arrays

With each, we specify the algorithm by giving its precondition

We develop several important algorithms on arrays.

- 2. When does it stop (when is the postcondition true)?
- 3. How does repetend make progress toward termination?
- 4. How does repetend keep the invariant true?

2

Invariant as picture: Combining pre- and post-condition

Finding the minimum of an array. Given array b satisfying precondition P, store a value in x to truthify postcondition Q:

Q: b x is the min of this segment

The invariant as picture: Combining pre- and post-condition

Put negative values before nonnegative ones, given precondition P:

P: b ? (values in 0..n-1 are unknown)

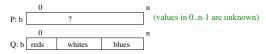
Swap the values of b[0..n-1] and store in k to truthify Q:

 $Q: b \begin{array}{|c|c|c|c|c|}\hline 0 & k & & n \\ \hline & <0 & & >=0 \\ \hline & & & values in k..n-1 are > 0) \\ \hline \end{array}$ 

4

The invariant as picture: Combining pre- and post-condition

**Dutch national flag.** Swap values of 0.n-1 to put the reds first, then the whites, then the blues. That is, given precondition P, swap value of b[0.n] to truthify postcondition Q:



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**Partition algorithm:** Given an array b[h..k] with some value x in b[h]:

h k P: b x ?

Swap elements of b[h..k] and store in j to truthify P:



or b 1 2 3 1 3 4 5 6 8

- x is called the pivot value.
- $\boldsymbol{x}$  is not a program variable;  $\boldsymbol{x}$  just denotes the value initially in b[h].

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## Linear search (for value known to be in array) Vague spec.: Find first occurrence of v in b[h..k-1], which is known to be there. Better spec.: Store an integer in i to truthify postcondition Q: P: 1. v is not in b[h..i-1] 2. v = b[k] h precondition P: b v is in here h postcondition Q: b v not here v ? Can't simply combine P and Q because position of v not known initially. But we can just delete value v from Q: h invariant Q: b v not here ?

