## 1 Where to put your long-burning light bulb?

Refer to the dot-matrix examples from the lecture on 4/8. Suppose you have one extra-long-life light bulb that can be used in a  $7 \times 5$  board for displaying a digit (0 to 9; all are equally likely to be displayed). In which positions of the  $7 \times 5$  board would you put this special long-life light bulb? Assume that a bulb (i,j) that is in a lit part of the board simply stays on—instead of first turning off and then back on—when the display changes to another digit that requires bulb (i,j) to be on. Consider the following cases:

- 1. The longer that a bulb is on, the more it degrades.
- 2. Switching a bulb on (and off) frequently causes it to degrade. (Take the extreme case—assume that continuous burning doesn't degrade the bulb.)

Function TheDigits returns a 10-by-1 cell array D such that  $D\{k\}$  is the matrix encoding digit k. *Part of* the function is shown below:

```
function D = TheDigits
% D is a 10-by-1 cell array.
% D{k} is a 7-by-5 matrix that encodes the digit k. (D{10} encodes 0.)
D = cell(10, 1);
D{1} = [0 \ 0 \ 1 \ 0 \ 0; \dots
          0 1 1 0 0;...
          0 0 1 0 0;...
          0 0 1 0 0;...
          0 0 1 0 0;...
          0 0 1 0 0;...
          0 1 1 1 0];
D{2} = [0 \ 1 \ 1 \ 1 \ 0; \dots
          1 0 0 0 1;...
          0 0 0 0 1;...
          0 0 0 1 0;...
          0 0 1 0 0;...
          0 1 0 0 0;...
          1 1 1 1 1];
D\{10\} = [0 \ 1 \ 1 \ 1 \ 0; \ldots
          1 0 0 0 1;...
          1 0 0 0 1;...
          1 0 0 0 1;...
          1 0 0 0 1;...
          1 0 0 0 1;...
          0 1 1 1 0];
```

## 2 Challenge question

Refer to the question above. What if you have five extra-long-life light bulbs? Determine in which positions you should place these special light bulbs in the two cases described above.