# Hyperparameter optimization

CS6787 Lecture 6 — Fall 2019

# But First... Final Project Parameters

CS 6787 — Fall 2019

#### Overview

- Implement a machine learning system to solve a problem
- Use one or more of the techniques we discussed in class
- To achieve an improvement over some baseline method
  - Measuring both statistical performance and hardware performance
  - Or at least evaluate and attempt to achieve such a speedup
- Otherwise, very open-ended
  - Groups of up to three

## Project proposals due in two weeks

- The main body should be about one page in length.
- It should describe the project you intend to do.
- It should contain at least one citation of a relevant paper that we did not cover in class.
- It should include some preliminary or exploratory work you've already done, that helps to support the idea that your project is feasible.
  - Doesn't have to be much work at all, just a nonzero amount of work.
- In addition to the one-page text proposal, one short **experiment plan** per person

# Experiment plan

• The hypothesis

• The proxy

• The protocol

• Expected results

## In-class feedback activity

• On Wednesday, October 16

- Basically, breakout sessions to discuss your project ideas with your peers.
  - You are not committing to work on the specific project you present during the feedback activity. You can always change your ideas as a result of the feedback.
- Prepare a two-minute verbal pitch of your ideas.
- And try not to sit with others in your group.
  - To get a wider variety of feedback.

# Questions?

# Hyperparameter optimization

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# Review — We've covered many methods

- Stochastic gradient descent
  - Step size/learning rate, how long to run
- Mini-batching
  - Batch size
- Momentum
  - Momentum parameter
- Kernel trick/feature extraction
  - How many features to extract
- Variance reduction
  - Step size, epoch length

How do we set these parameters?

# So Far: Theory

- Theoretical analysis of convex problems gives us a **recipe** for assigning hyperparameters
  - Also gives guarantees that the algorithm will converge with some optimal rate
- Often based on strong-convexity/Lipschitz constants  $\mu$ , L, etc.
  - Parameters that we can bound analytically, regardless of the data
- This is usually enough to get an asymptotically optimal rate
  - Certainly in the worst case

# The Worst-Case Perspective

• Essentially, the theory I showed you is doing

- We're not using the training data at all to set the parameters
  - $\bullet$  Or if we are, we're only using it to compute constants like  $\mu$  and L
- Question: can we use the data to improve our choice of parameters over what the theory gives us?

# Demo

# What happened?

• Theory only minimizes an upper bound on the objective.

- But actual algorithm can do much better than the bound.
  - As we saw in the demo.
- Problem: in the demo, to find the best parameter setting, we had to first solve the problem exactly, then run the algorithm many times.
  - Computationally intractable in practice!
- Can we use a cheaper heuristic to set the parameters?

# Hyperparameter Optimization

## Hyperparameter Optimization

• Also called metaparameter optimization

Also called tuning

• Any system that chooses hyperparameters automatically

• What's the difference between the model parameters, and the hyperparameters?

# Many Settings; Many Strategies

- In some settings, just care about the model accuracy
  - Just want to set things like the learning rate
- In other settings, also want to make the hardware fast
  - Want to choose what hardware to run on, how many cores, etc.
- In all settings, there's many ways to do hyperparameter optimization

# Simplest Strategy: The Null Hyperparameter Optimizer

• Simplest thing to do is to just set the parameters based on folklore.

• Momentum: 
$$\beta = ?$$

# The Effect of Using Folklore

- Folklore can lead you astray!
  - Can actually find simple cases where the folklore settings are wrong.
  - This is a good way to start a research paper.
- ...but folklore is folklore for a reason!
  - It exists where people have found empirically that they get good results.
  - So when you try something new, the first thing to compare to is folklore.
- To be honest, the results you get from just using the folklore settings are really not that bad for a lot of practical purposes.

# From the simplest strategy to... The Most Complicated Strategy

• Spend twenty-five years training a Strong AI on custom hardware, then have it set your hyperparameters.

• ...more explicitly, just get a human to set your hyperparameters.

- Fortunately, we happen to have a lot of humans
  - But human effort, particularly expert human effort, doesn't scale.

# Tuning By Hand

• Just fiddle with the parameters until you get the results you want

• Probably the most common type of hyperparameter optimization

• Upsides: the results are generally pretty good...

- Downsides: lots of effort, and no theoretical guarantees
  - Although there's nothing fundamental that prevents us from having theory here

# Demo

#### Grid Search

• Define some grid of parameters you want to try

- Try all the parameter values in the grid
  - By running the whole system for each setting of parameters
- Then choose the setting with the best result

• Essentially a brute force method

#### Downsides of Grid Search

- As the number of parameters increases, the cost of grid search increases exponentially!
  - Why?
- Still need some way to choose the grid properly
  - Something this can be as hard as the original hyperparameter optimization
- Can't take advantage of any **insight** you have about the system!

## Making Grid Search Fast

#### • Early stopping to the rescue

• Can run all the grid points for one epoch, then discard the half that performed worse, then run for another epoch, discard half, and continue.

#### Can take advantage of parallelism

- Run all the different parameter settings independently on different servers in a cluster.
- An embarrassingly parallel task.
- Downside: doesn't reduce the energy cost.

#### One Variant: Random Search

• This is just grid search, but with randomly chosen points instead of points on a grid.

- This solves the curse of dimensionality
  - Don't need to increase the number of grid points exponentially as the number of dimensions increases.
- Problem: with random search, not necessarily going to get anywhere near the optimal parameters in a finite sample.

#### One Variant: Best Ball

• Works with epochs.

• At each epoch, do a small grid search around the current hyperparameter settings

- Then evaluate the objective and choose the "best ball"
  - The choice of parameters that gave the best objective for that epoch
- And repeat until a solution of desired quality is achieved.

# An Alternative: Bayesian Optimization

- Statistical approach for minimizing noisy black-box functions.
- Idea: learn a statistical model of the function from hyperparameter values to the loss function
  - Then choose parameters to minimize the loss under this model
- Main benefit: choose the hyperparameters to test not at random, but in a way that gives the **most information about the model** 
  - This lets it learn faster than grid search

## Effect of Bayesian Optimization

- Downside: it's a pretty heavyweight method
  - The updates are not as simple-to-implement as grid search
- Upside: empirically it has been demonstrated to **get better results in fewer experiments** 
  - Compared with grid search and random search
- Pretty widely used method
  - Lots of research opportunities here.

#### A related method: DFO

• Derivative-free optimization

• Also called zeroth-order optimization

• These methods optimize a function using only evaluations, no derivatives

- Ideal for use with hyperparameter optimization
  - Also ideal for reinforcement learning

# The opposite of DFO Gradient-based optimization

• These strategies say: "I'm doing SGD to learn, I may as well use it to optimize my hyperparameters."

• When we can efficiently differentiate with respect to the hyperparameters, this strategy actually works pretty well.

• But generally, we can't do it.

#### Methods that Look at the Data

• Many methods look at curvature/variance info to decide how to set hyperparameters, and update their settings throughout the algorithm

• Example: **ADAGRAD** 

• Example: Adam

• Which you will be reading in a few weeks.

# Evaluating the Hyperparameter Optimization

# How to evaluate the hyperparameters?

- Unlike the model parameters, we're not given a loss function
- Can't we just use the training loss?
- Not always: we don't want to overfit the hyperparameters
  - Especially not when they are things that affect the model

#### Cross-Validation

• Partition part of the available data to create an **validation dataset** that we don't use for training.

• Then use that set to evaluate the hyperparameters.

- Typically, multiple rounds of cross-validation are performed using different partitions
  - Can get a very good sense of how good the hyperparameters are
  - But at a significant computational cost!

# Evaluating the System Cost

- In practice we don't just care about the statistics
  - Not just about the accuracy after a fixed number of iterations
- We care about wall-clock time, and we care about energy
  - How much did solving this problem actually cost?
- The parameters we chose can affect these systems properties
  - As we saw with our SVRG demo!
- Need to include systems cost as part of the metric!

# Hardware efficiency

• How long does an iteration take, on average?

• Hardware efficiency measures the systems cost of doing a single update.

- Key point: many hyperparameters do not affect hardware efficiency
  - Which ones?

• Which hyperparameters do affect hardware efficiency?

# Statistical Efficiency

• How many iterations do we need to get to a specified level of accuracy?

• Statistical efficiency measures how many updates we need to get an answer of the quality that we want.

- Which hyperparameters affect statistical efficiency?
  - And which ones don't?

# Total performance

• Total cost of running the algorithm is:

#### HARDWARE EFFICIENCY x STATISTICAL EFFICIENCY

• We can estimate these quantities separately, then use their product to evaluate our hyperparameters.

• For example, we can use theory to evaluate statistical efficiency and a hardware model to evaluate hardware efficiency.

# Benefits of Looking at Both

• Looking at both statistical and hardware efficiency together has some important benefits!

• Many times the **optimal parameter settings are different** than if you set the parameters to optimize hardware efficiency or statistical efficiency individually.

• There's a lot of open research opportunities here!

### One example: YellowFin Tuner

- System that among other things tunes the momentum
  - As well as using asynchronous parallelism, which we'll talk about later.

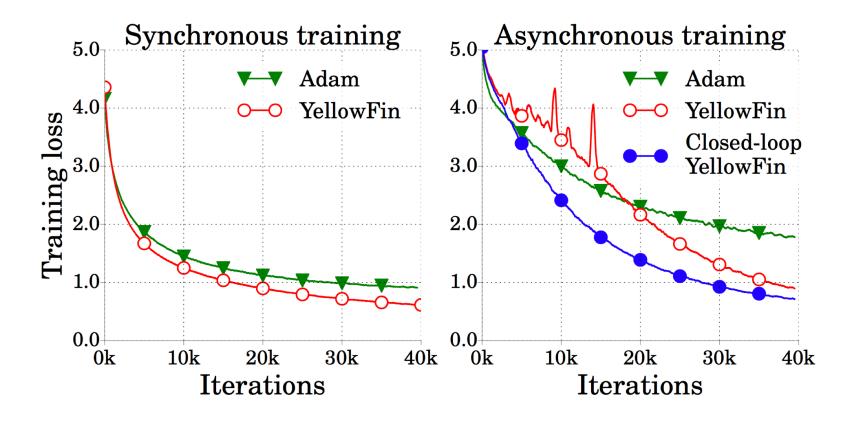


Figure 1 from "YellowFin and the Art of Momentum Tuning" Zhang et al, 2017.

## Questions?

- Upcoming things
  - Fall break next Monday no lecture
  - Paper review 4a or 4b due Today
  - Paper Presentation #5 on Wednesday
  - In class discussion of project ideas the following Wednesday