## Frontiers: Offline Reinforcement Learning

### Sanjiban Choudhury







## Frontiers



### Problem: Insane number of papers out there!!

Impossible for outsiders to find any sort of scaffolding

Many of these papers recycle old ideas while butchering the insight

Hope: Sparse set of papers that give you reach







## Our Strategy

**Goal:** Engage with various frontiers of research on robot decision making

**Strategy:** Equip you with a sparse "support vector" of papers that gives you maximal reach on the problem

**Expectation:** For details and concrete implementation, you should be able to look that up

The Problem



#### Robots can augment human capabilities to tackle these problems

## Real World, Real Problems





## Robots only really work in the CLOSED world



















#### The Dream



#### Reality





### Generalize to variations of the OPEN world?









## Machine learning's answer!



#### Big Data

Credit: Sergey Levine "Offline RL lecture"

Big Models



## Hasn't quite been true so far robotics ...

#### On the quest for shared priors w/ machine learning



Interact with the physical world to learn bottom-up commonsense 1 i.e. "how the world works"

Credit: Andy Zeng



## Hasn't quite been true so far robotics ...



Data

Interact with the **physical** world to learn **bottom-up commonsense** 

Credit: Andy Zeng

On the quest for shared priors w/ machine learning



i.e. "how the world works"

#### But for today, let's pretend we can collect a ton of data

# How can we learn "optimal" from large data collected by *any* policy?

## Goal: Offline Reinforcement Learning





#### occasionally get more data



Credit: Sergey Levine "Offline RL lecture"





big datasets from past interaction



train for many epochs

# Different paradigms of RL

### on-policy RL



Credit: Sergey Levine "Offline RL lecture"

![](_page_13_Picture_4.jpeg)

#### on-policy RL

![](_page_14_Figure_2.jpeg)

![](_page_14_Figure_3.jpeg)

![](_page_14_Figure_4.jpeg)

![](_page_14_Figure_5.jpeg)

Credit: Sergey Levine "Offline RL lecture"

![](_page_14_Picture_7.jpeg)

### off-policy RL

![](_page_14_Picture_9.jpeg)

![](_page_14_Picture_10.jpeg)

![](_page_15_Figure_0.jpeg)

![](_page_15_Figure_1.jpeg)

Credit: Sergey Levine "Offline RL lecture"

![](_page_15_Picture_3.jpeg)

![](_page_15_Picture_5.jpeg)

#### Offline Reinforcement Learning: Tutorial, Review, and Perspectives on Open Problems

Sergey Levine<sup>1,2</sup>, Aviral Kumar<sup>1</sup>, George Tucker<sup>2</sup>, Justin Fu<sup>1</sup> <sup>1</sup>UC Berkeley, <sup>2</sup>Google Research, Brain Team

![](_page_16_Picture_2.jpeg)

#### Fun collab tutorial: <u>https://colab.research.google.com/drive/</u> <u>1oJOYIAIOI9d1JjlutPY66KmfPkwPCgEE?usp=sharing</u>

![](_page_16_Picture_4.jpeg)

### How is this even possible?

- 1. Find the "good stuff" in a dataset full of good and bad behaviors
- 3. "Stitching": parts of good behaviors can be recombined

![](_page_17_Figure_4.jpeg)

![](_page_17_Picture_5.jpeg)

Credit: Sergey Levine "Offline RL lecture"

2. Generalization: good behavior in one place may suggest good behavior in another place

Sometimes\*

### Does it work?

### Large-scale Q-learning with continuous actions (QT-Opt)

![](_page_19_Picture_1.jpeg)

![](_page_19_Picture_2.jpeg)

Kalashnikov, Irpan, Pastor, Ibarz, Herzong, Jang, Quillen, Holly, Kalakrishnan, Vanhoucke, Levine. QT-Opt: Scalable Deep Reinforcement Learning of Vision-**Based Robotic Manipulation Skills** 

![](_page_19_Picture_5.jpeg)

#### Offline reinforcement learning for safer blood glucose control in people with type 1 diabetes

#### Harry Emerson<sup>a,\*</sup>, Matthew Guy<sup>a,b</sup>, Ryan McConville<sup>a</sup>

<sup>a</sup> University of Bristol, 1 Cathedral Square, Bristol, BS1 5TS, United Kingdom <sup>b</sup> University Hospital Southampton, Tremona Road, Southampton, SO16 6YD, Hampshire, United Kingdom

#### Table 2

best performing algorithm highlighted in bold.

Algorithm	Reward	TIR (%)	TBR (%)	CV (%)	Failure (%)
$\mathbf{B}\mathbf{C}\mathbf{Q}^{\dagger}$	$-41,034 \pm 1,060$	65.8 ± 0.6	$1.0~\pm~0.1$	$35.1 \pm 0.4$	0.00
$\mathbf{C}\mathbf{Q}\mathbf{L}^{\dagger}$	$-45,259 \pm 1,071$	$56.2 \pm 0.5$	$0.1 \pm 0.1$	$30.3\pm0.3$	0.00
TD3-BC <sup>†</sup>	$-37,955 \pm 547$	$65.3 \pm 0.5$	$0.2 \pm 0.1$	$33.3\pm0.2$	0.00
SAC-RNN <sup>‡</sup>	$-93,480 \pm 71,826$	34.9 ± 3.1	$4.1 \pm 0.7$	$29.6 \pm 1.3$	13.3
PID <sup>§</sup>	$-49,077 \pm 556$	$61.6 \pm 0.3$	$0.4\pm0.1$	$33.5\pm0.2$	0.00

## Optimal Insulin Dose

The mean performance of the offline RL algorithms: BCQ, CQL and TD3-BC against the online RL approach SAC-RNN and the control baseline PID. TD3-BC can be seen to significantly improve the proportion of TIR when compared to the PID and the SAC-RNN algorithms. This is done so without any associated increase in risk (reward) or TBR. Statistical significance was confirmed via a Friedman rank test for all glucose metrics (p < 0.05).  $\dagger$ ,  $\ddagger$  and  $\S$  indicate an offline RL, online RL and classical control algorithm respectively, with the

![](_page_20_Picture_9.jpeg)

## Combustion control in power stations

#### **DeepThermal: Combustion Optimization for Thermal Power Generating Units Using Offline Reinforcement Learning**

#### Xianyuan Zhan<sup>1</sup>\*, Haoran Xu<sup>2,3,4</sup>\*, Yue Zhang<sup>2,3</sup>, Xiangyu Zhu<sup>2,3</sup>, Honglei Yin<sup>2,3</sup>, Yu Zheng<sup>2,3,4</sup>

<sup>1</sup> Institute for AI Industry Research (AIR), Tsinghua University, Beijing, China <sup>2</sup> JD iCity, JD Technology, Beijing, China
 <sup>3</sup> JD Intelligent Cities Research, Beijing, China <sup>4</sup> Xidian University, Xi'an, China

{zhanxianyuan, ryanxhr, zhangyuezjx, zackxiangyu, yinhonglei93}@gmail.com, msyuzheng@outlook.com

![](_page_21_Figure_6.jpeg)

Figure 4: Real-world experiments at CHN Energy Nanning Power Station

![](_page_21_Picture_8.jpeg)

## Goal-directed conversation

#### CHAI: A CHatbot AI for Task-Oriented Dialogue with Offline Reinforcement Learning

Siddharth Verma UC Berkeley

Justin Fu UC Berkeley

Metric	Fluency	Coherency	On-Topic	Human-Likeness	Total
CHAI-prop	$4.31 \pm 0.97$	$3.91 \pm 1.17$	$4.16 \pm 0.99$	$3.47 \pm 1.27$	$\bf 15.84 \pm 3.86$
He et al. (2018) (Utility)	$3.56 \pm 1.34$	$2.47 \pm 1.39$	$3.09 \pm 1.40$	$2.13 \pm 1.13$	$11.25\pm4.50$
Lang. Model	$4.06 \pm 1.11$	$2.66 \pm 1.36$	$3.63 \pm 1.18$	$2.50\pm1.10$	$12.84 \pm 3.66$

Table 2: Human evaluation scores comparing CHAI, He et al. (2018), and language model (higher is better). Numbers are reported as means and standard deviations over 32 trials. CHAI scores the highest across all metrics.

Mengjiao Yang UC Berkeley

Sergey Levine UC Berkeley

![](_page_22_Picture_8.jpeg)

## We have already covered a fundamental algorithm in class that can learn from offline data.

## What is it?

![](_page_23_Picture_3.jpeg)

![](_page_23_Picture_4.jpeg)

![](_page_24_Figure_1.jpeg)

For every  $(s_t, a_t, c_t, s_{t+1})$ 

 $Q^*(s_t, a_t) = Q^*(s_t, a_t) + \alpha(c(s_t, a_t) + \gamma \min_{a'} Q^*(s_{t+1}, a') - Q^*(s_t, a_t))$ 

![](_page_24_Picture_6.jpeg)

![](_page_24_Picture_7.jpeg)

### For every $(s_t, a_t, c_t, s_{t+1})$

#### $Q^*(s_t, a_t) = Q^*(s_t, a_t) + \alpha$

Notice we are *not* approximating  $Q^{\pi}(s_t, a_t)$ 

We don't even care about  $\pi$ 

We can learn from any data!

$$(c(s_t, a_t) + \gamma \min_{a'} Q^*(s_{t+1}, a') - Q^*(s_{t+1}, a'))$$

![](_page_25_Picture_7.jpeg)

![](_page_25_Picture_8.jpeg)

### For every $(s_t, a_t, c_t, s_{t+1})$

#### $Q^*(s_t, a_t) = Q^*(s_t, a_t) + \alpha$

#### Conditions for convergence

- 2.  $\lim_{k\to a}$
- 3.  $\lim_{k \to 0} \frac{1}{2}$

$$(c(s_t, a_t) + \gamma \min_{a'} Q^*(s_{t+1}, a') - Q^*(s_{t+1}, a'))$$

1. Each state-action pair is visited infinite times

$$\sum_{k=0}^{\infty} \alpha_k = \infty$$
  
 $\sum_{k=0}^{\infty} \alpha_k^2 < \infty$ ,

![](_page_26_Picture_10.jpeg)

![](_page_26_Picture_11.jpeg)

### For every $(s_t, a_t, c_t, s_{t+1})$

#### $Q^*(s_t, a_t) = Q^*(s_t, a_t) + \alpha$

What happens1. Each sidewhen this is2.  $\lim_{k \to 0} 1$ not met?3.  $\lim_{k \to 0} 1$ 

$$(c(s_t, a_t) + \gamma \min_{a'} Q^*(s_{t+1}, a') - Q^*(s_{t+1}, a'))$$

#### 1. Each state-action pair is visited infinite times

$$_{\infty}\sum_{k=0}^{\infty}\alpha_{k}=\infty$$

$$-\infty \sum_{k=0}^{\infty} \alpha_k^2 < \infty$$

![](_page_27_Picture_8.jpeg)

![](_page_27_Picture_9.jpeg)

![](_page_27_Picture_10.jpeg)

![](_page_28_Picture_0.jpeg)

![](_page_28_Picture_1.jpeg)

**S**1 +1

## Consider the following MDP

![](_page_29_Figure_3.jpeg)

### Let's say I collected some data from the MDP

![](_page_30_Picture_1.jpeg)

![](_page_30_Picture_2.jpeg)

![](_page_30_Picture_3.jpeg)

50%

#### What would happen if I did Q-learning with this data?

![](_page_31_Picture_1.jpeg)

50%

![](_page_31_Picture_3.jpeg)

50%

## Think-Pair-Share!

Think (30 sec): What would happen if we did Q-learning with this data? Ideas on how to fix it.

#### Pair: Find a partner

Share (45 sec): Partners exchange ideas

![](_page_32_Picture_5.jpeg)

**S**2

**S**0

-10 -10

**S**1

+1

![](_page_32_Picture_6.jpeg)

### Why is offline RL hard?

![](_page_33_Figure_1.jpeg)

how well it does

Kumar, Fu, Tucker, Levine. Stabilizing Off-Policy Q-Learning via Bootstrapping Error Reduction. NeurIPS '19

Credit: Sergey Levine "Offline RL lecture"

![](_page_33_Figure_5.jpeg)

it does (Q-values)

![](_page_34_Figure_1.jpeg)

Figure from *Diagnosing Bottlenecks in Deep Q-learning Algorithms*. **K.\*,** Fu\*, Levine. ICML 2019

![](_page_34_Picture_4.jpeg)

![](_page_34_Picture_8.jpeg)

### Why is offline RL hard?

#### **Fundamental problem:** counterfactual queries

![](_page_35_Figure_2.jpeg)

**Online RL** algorithms don't have to handle this, because they can simply **try** this action and see what happens

**Offline RL** methods must somehow account for these unseen ("out-of-distribution") actions, ideally in a safe way ...while still making use of generalization to come up with behaviors that are better than the best thing seen in the data!

Levine, Kumar, Tucker, Fu. Offline Reinforcement Learning: Tutorial, Review, and Perspectives on Open Problems. '20

Credit: Sergey Levine "Offline RL lecture"

Is this good? Bad?

How do we know if we didn't see it in the data?

![](_page_35_Picture_15.jpeg)

![](_page_36_Picture_1.jpeg)

50%

## Why not just do imitation learning?

![](_page_36_Picture_4.jpeg)

50%

![](_page_36_Picture_6.jpeg)

## Now consider this MDP

![](_page_37_Picture_1.jpeg)

![](_page_37_Figure_3.jpeg)

What is the optimal policy? What would imitation learning do?

![](_page_37_Picture_5.jpeg)

Pessimism

Don't deviate too much from the data collecting policy

Credit: Sergey Levine "Offline RL lecture"

## Pessimism as a policy constraint

 $Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + E_{\mathbf{a}' \sim \pi_{new}}[Q(\mathbf{s}', \mathbf{a}')]$  $\pi_{new}(\mathbf{a}|\mathbf{s}) = \arg\max_{\pi} E_{\mathbf{a} \sim \pi(\mathbf{a}|\mathbf{s})}[Q(\mathbf{s}, \mathbf{a})] \text{ s.t. } D_{\mathrm{KL}}(\pi \| \pi_{\beta}) \leq \epsilon$ 

Choose any divergence, e.g. KL!

 $\pi_{\beta}(\mathbf{a}|\mathbf{s})$ 

![](_page_39_Picture_9.jpeg)

![](_page_39_Picture_10.jpeg)

### TD3+BC: Most simple and effective offline RL!

#### A Minimalist Approach to **Offline Reinforcement Learning**

Scott Fujimoto<sup>1,2</sup> Shixiang Shane Gu<sup>2</sup> <sup>1</sup>Mila, McGill University <sup>2</sup>Google Research, Brain Team scott.fujimoto@mail.mcgill.ca

$$\pi = \operatorname*{argmax}_{\pi}$$

$$\pi = \operatorname*{argmax}_{\pi} \mathbb{E}_{(s,a) \sim \mathcal{D}} \left[ \lambda Q(s, \pi(s)) - (\pi(s) - a)^2 \right],$$

$$\mathbb{E}_{(s,a)\sim\mathcal{D}}[Q(s,\pi(s))].$$

		BC	BRAC-p	AWAC	CQL	Fisher-BRC	TD3+BC
Random	HalfCheetah	$2.0\pm 0.1$	23.5	2.2	$21.7 \pm 0.9$	<b>32.2</b> ±2.2	10.2 ±1.3
	Hopper	<b>9.5</b> ±0.1	11.1	9.6	<b>10.7</b> ±0.1	11.4 ±0.2	<b>11.0</b> ±0.1
	Walker2d	<b>1.2</b> ±0.2	0.8	5.1	<b>2.7</b> ±1.2	<b>0.6</b> ±0.6	1.4 ±1.6
Medium	HalfCheetah	<b>36.6</b> ±0.6	44.0	37.4	$37.2\pm0.3$	<b>41.3</b> ±0.5	<b>42.8</b> ±0.3
	Hopper	$30.0\pm\!0.5$	31.2	72.0	$44.2 \pm 10.8$	<b>99.4</b> ±0.4	<b>99.5</b> ±1.0
	Walker2d	$11.4 \pm \! 6.3$	72.7	30.1	$57.5 \pm 8.3$	<b>79.5</b> ±1.0	<b>79.7</b> ±1.8
Medium Replay	HalfCheetah	<b>34.7</b> ±1.8	45.6	-	<b>41.9</b> ±1.1	<b>43.3</b> ±0.9	<b>43.3</b> ±0.5
	Hopper	$19.7 \pm \! 5.9$	0.7	-	$\textbf{28.6} \pm 0.9$	35.6 ±2.5	<b>31.4</b> ±3.0
	Walker2d	8.3 ±1.5	-0.3	-	$15.8 \pm 2.6$	<b>42.6</b> ±7.0	<b>25.2</b> ±5.1
Medium Expert	HalfCheetah	<b>67.6</b> ±13.2	43.8	36.8	27.1 ±3.9	<b>96.1</b> ±9.5	<b>97.9</b> ±4.4
	Hopper	<b>89.6</b> ±27.6	1.1	80.9	111.4 ±1.2	<b>90.6</b> ±43.3	$112.2 \pm 0.2$
	Walker2d	$12.0 \pm \! 5.8$	-0.3	42.7	<b>68.1</b> ±13.1	103.6 ±4.6	101.1 ±9.3
Expert	HalfCheetah	<b>105.2</b> ±1.7	3.8	78.5	<b>82.4</b> ±7.4	<b>106.8</b> ±3.0	105.7 ±1.9
	Hopper	<b>111.5</b> ±1.3	6.6	85.2	111.2 ±2.1	112.3 ±0.2	$112.2 \pm 0.2$
	Walker2d	$56.0 \pm 24.9$	-0.2	57.0	103.8 ±7.6	<b>79.9</b> ±32.4	105.7 ±2.7
	Total	595.3 ±91.5	284.1	-	764.3 ±61.5	<b>974.6</b> ±108.3	<b>979.3</b> ±33.4

Table 2: Average normalized score over the final 10 evaluations and 5 seeds. The highest performing scores are highlighted. CQL and Fisher-BRC are re-run using author-provided implementations to ensure an identical evaluation process, while BRAC and AWAC use previously reported results.  $\pm$  captures the standard deviation over seeds. TD3+BC achieves effectively the same performances as the state-of-the-art Fisher-BRC, despite being much simpler to implement and tune and more than halving the computation cost.

![](_page_41_Picture_2.jpeg)

## Works on real self-driving problems!

#### **Imitation Is Not Enough: Robustifying Imitation with Reinforcement Learning for Challenging Driving Scenarios**

Yiren Lu<sup>1</sup>, Justin Fu<sup>1</sup>, George Tucker<sup>2</sup>, Xinlei Pan<sup>1</sup>, Eli Bronstein<sup>1</sup>, Rebecca Roelofs<sup>2</sup>, Benjamin Sapp<sup>1</sup>, Brandyn White<sup>1</sup>, Aleksandra Faust<sup>2</sup>, Shimon Whiteson<sup>1</sup>, Dragomir Anguelov<sup>1</sup>, Sergey Levine<sup>2,3</sup>

![](_page_42_Figure_3.jpeg)

![](_page_42_Picture_6.jpeg)

## Works on real self-driving problems!

#### **Imitation Is Not Enough: Robustifying Imitation with Reinforcement Learning for Challenging Driving Scenarios**

Yiren Lu<sup>1</sup>, Justin Fu<sup>1</sup>, George Tucker<sup>2</sup>, Xinlei Pan<sup>1</sup>, Eli Bronstein<sup>1</sup>, Rebecca Roelofs<sup>2</sup>, Benjamin Sapp<sup>1</sup>, Brandyn White<sup>1</sup>, Aleksandra Faust<sup>2</sup>, Shimon Whiteson<sup>1</sup>, Dragomir Anguelov<sup>1</sup>, Sergey Levine<sup>2,3</sup>

![](_page_43_Picture_3.jpeg)

https://waymo.com/research/imitation-is-not-enough-robustifying-imitation-with-reinforcement-learning/

![](_page_43_Picture_5.jpeg)

![](_page_43_Picture_6.jpeg)

## But choosing a divergence seems arbitrary?

 $Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + E_{\mathbf{a}' \sim \pi_{new}}[Q(\mathbf{s}', \mathbf{a}')]$ 

 $\pi_{\text{new}}(\mathbf{a}|\mathbf{s}) = \arg\max_{\pi} E_{\mathbf{a} \sim \pi(\mathbf{a}|\mathbf{s})}[Q(\mathbf{s},\mathbf{a})] \text{ s.t. } D_{\text{KL}}(\pi \| \pi_{\beta}) \leq \epsilon$ 

![](_page_44_Picture_4.jpeg)

![](_page_44_Picture_6.jpeg)

![](_page_44_Picture_7.jpeg)

### Another notion of pessimism

# Can we make the Q-value itself pessimistic on actions it has not seen?

![](_page_45_Picture_2.jpeg)

# Conservative Q-Learning (CQL)

#### **Conservative Q-Learning** for Offline Reinforcement Learning

Aviral Kumar<sup>1</sup>, Aurick Zhou<sup>1</sup>, George Tucker<sup>2</sup>, Sergey Levine<sup>1,2</sup> <sup>1</sup>UC Berkeley, <sup>2</sup>Google Research, Brain Team aviralk@berkeley.edu

![](_page_46_Picture_3.jpeg)

![](_page_47_Picture_1.jpeg)

**Approach 2: Directly modify the Q-function to be pessimistic** 

Key idea behind CQL: Learn lower-bounds on Q-values

**CQL** Algorithm:

Credit: Aviral Kumar "Conservative Q learning"

- 1. Learn  $\hat{Q}_{CQL}^{\pi}$  using offline data  $\mathcal{D}$ . 2. Optimize policy w.r.t.  $\hat{Q}_{CQL}^{\pi}$ :  $\pi \leftarrow \arg \max_{\pi} \mathbb{E}_{\pi}[\hat{Q}_{CQL}^{\pi}]$ .

![](_page_47_Picture_13.jpeg)

#### Many ways to construct a conservative Q value

#### Recent work has come up with more unified frameworks

#### Original CQL paper proposed one such way

![](_page_48_Picture_4.jpeg)

## Adversarially Trained Actor Critic (ATACL)

#### **Adversarially Trained Actor Critic for Offline Reinforcement Learning**

Ching-An Cheng<sup>\*1</sup> Tengyang Xie<sup>\*2</sup> Nan Jiang<sup>2</sup> Alekh Agarwal<sup>3</sup>

![](_page_49_Picture_3.jpeg)

![](_page_49_Picture_4.jpeg)

![](_page_50_Picture_0.jpeg)

### Key Idea: Relative Pessimism

![](_page_51_Figure_3.jpeg)

Lower bound 
$$< J(\pi) - J(\mu)$$

![](_page_51_Figure_5.jpeg)

#### • Optimize for the worst-case performance compared with the behavior policy $\mu$ .

und of 
$$J(\pi) - J(\mu)$$

Lower bound 
$$\approx J(\pi) - J(\mu)$$

![](_page_51_Figure_9.jpeg)

### Key Idea: Relative Pessimism

![](_page_52_Figure_3.jpeg)

#### • Optimize for the **best worst-case** performance compared with the **behavior policy** $\mu$ .

ATAC frames this problem as a Stackelberg game (i.e., bilevel optimization)

![](_page_52_Picture_7.jpeg)

### A Stackelberg Game for Offline RL

• ATAC optimizes for relative pessimism via solving a Stackelberg game

![](_page_53_Figure_3.jpeg)

relative pessimism

**Bellman error** 

Trade-off conservatism vs. generalization

 $\mathcal{L}_{\mu}(\pi, f) \coloneqq \mathbb{E}_{\mu} |f(s, \pi) - f(s, a)|$  $\mathcal{E}_{\mu}(\pi, f) \coloneqq \mathbb{E}_{\mu}[((f - \mathcal{T}^{\pi}f)(s, a))^2].$ 

![](_page_53_Picture_11.jpeg)

### A Stackelberg Game for Offline RL

• ATAC optimizes for relative pessimism via solving a Stackelberg game

![](_page_54_Figure_3.jpeg)

### **Robust Policy Improvement Property**

$$\mathcal{C}_{\mu}(\pi, f^{\pi}) \ge \mathcal{L}(\pi, Q^{\pi}) \equiv J(\pi) - J(\mu), \forall \beta \ge 0$$

 $f^{\pi} \in \operatorname*{arg\,min}_{f \in \mathcal{F}} \mathcal{L}_{\mu}(\pi, f) + \beta \mathcal{E}_{\mu}(\pi, f)$   $f \in \mathcal{F}$ Bilinear Payoffs of

relative pessimism

**Bellman error** 

Trade-off conservatism vs. generalization

For all  $\beta \ge 0$ , the ATAC policy is always no worse than the behavior policy that collected the data.

 $\mathcal{L}_{\mu}(\pi, f) \coloneqq \mathbb{E}_{\mu}[f(s, \pi) - f(s, a)]$  $\mathcal{E}_{\mu}(\pi, f) \coloneqq \mathbb{E}_{\mu}[((f - \mathcal{T}^{\pi}f)(s, a))^2].$ 

![](_page_54_Picture_13.jpeg)

## Let's look at a simple example

![](_page_55_Figure_2.jpeg)

## Let's say the time horizon T=1 $\widehat{\pi}^* \in \arg \max \mathcal{L}_{\mu}(\pi, f^{\pi})$ s.t. (Multimation $f \in \mathcal{F}$

 $f(s, \cdot)$  $\beta \mathcal{E}_{\mu}$ 

![](_page_55_Picture_5.jpeg)

![](_page_55_Picture_6.jpeg)

## Let's look at a simple example

![](_page_56_Figure_2.jpeg)

## Let's say the time horizon T=1 $\widehat{\pi}^* \in \arg \max \mathcal{L}_{\mu}(\pi, f^{\pi})$ s.t. (Multination $f \in \mathcal{F}$

 $f(s, \cdot)$  $\beta \mathcal{E}_{\mu}$ 

![](_page_56_Picture_5.jpeg)

![](_page_56_Picture_6.jpeg)

## Let's look at a simple example

![](_page_57_Figure_2.jpeg)

$$\widehat{\pi}^* \in \underset{\pi \in \Pi}{\arg \max} \mathcal{L}_{\mu}(\pi, f^{\pi})$$
  
s.t. 
$$f^{\pi} \in \underset{f \in \mathcal{F}}{\arg \min} \mathcal{L}_{\mu}(\pi, f) + \beta \mathcal{E}_{\mu}(\pi, f)$$

$$f(s, \cdot) \qquad \qquad eta \mathcal{E}_{\mu}$$

![](_page_57_Picture_5.jpeg)

### A Stackelberg Game for Offline RL

![](_page_58_Figure_2.jpeg)

#### ATAC

$$\widehat{\pi}^* \in \underset{\pi \in \Pi}{\operatorname{arg\,max}} \mathcal{L}_{\mu}(\pi, f^{\pi})$$
  
s.t. 
$$\widehat{f^{\pi}} \in \underset{f \in \mathcal{F}}{\operatorname{arg\,min}} \mathcal{L}_{\mu}(\pi, f) + \beta \mathcal{E}_{\mu}(\pi, f)$$

hypothesis  $f(s,\cdot)$  with small  $eta \mathcal{E}_{\mu}$ 

Functions that are consistent with the reward and the dynamics on the behavior data

![](_page_58_Picture_7.jpeg)

### A Stackelberg Game for Offline RL

![](_page_59_Figure_2.jpeg)

#### ATAC $\widehat{\pi}^* \in \arg \max \mathcal{L}_{\mu}(\pi, f^{\pi})$ $\pi \in \Pi$ s.t. $f^{\pi} \in \arg \min \mathcal{L}_{\mu}(\pi, f) + \beta \mathcal{E}_{\mu}(\pi, f)$ $f \in \mathcal{F}$

value difference hypothesis  $f(s, \cdot) - f(s, \mu)$ Functions shifted from the original hypotheses

What is the solution to the Stackelberg game?

![](_page_59_Picture_6.jpeg)

### A Stackelberg Game for Offline RL

![](_page_60_Figure_2.jpeg)

![](_page_60_Figure_3.jpeg)

Not the behavior policy in this case...

![](_page_60_Picture_5.jpeg)

### A Stackelberg Game for Offline RL

![](_page_61_Figure_2.jpeg)

![](_page_61_Figure_3.jpeg)

value difference hypothesis  $f(s, \cdot) - f(s, \mu)$ inactive value difference hypothesis

decision policy  $\pi$ 

Not the policy that maximizes a single hypothesis...

![](_page_61_Picture_8.jpeg)

### A Stackelberg Game for Offline RL

![](_page_62_Figure_2.jpeg)

![](_page_62_Figure_3.jpeg)

multiple hypotheses

![](_page_62_Picture_5.jpeg)

### A Stackelberg Game for Offline RL

![](_page_63_Figure_2.jpeg)

![](_page_63_Figure_3.jpeg)

ATAC provides a bridge between offline RL and imitation learning with IPM via the lens of generative adversarial networks (GAN)

#### *Offline RL + Relative Pessimism = IL + Bellman Regularization*

### Solving the Stackelberg Game

**No-Regret + Best** 

![](_page_64_Figure_2.jpeg)

![](_page_64_Figure_4.jpeg)

![](_page_64_Picture_5.jpeg)

decision

$$f \in \mathcal{F} \mathcal{L}_{\mu}(\pi_{k}, f) + \beta \mathcal{E}_{\mu}(\pi_{k}, f)$$

$$Te$$

$$= NoRegret(\pi_{k}, f_{k})$$
Repeat for K iterations

Output uniform mixture of policies (theory) or the last policy (practice) In practice, the above is implemented by two-timescale SGD updates

active objective

Inactive objective

### ATAC Theory (Informal)

#### **Learning Optimality**

Assume  $\mathcal{F}$  satisfies realizability and completeness. Given dataset  $\mathcal{D}$  s.t.  $|\mathcal{D}| = I$  $J(\pi) - J(\hat{\pi}) \le \mathcal{O}\left(\frac{1}{(1-\gamma)N^{1/3}}\right) + \epsilon_{\text{generalization}}(\mathcal{F}, \pi, \mathcal{D})$ 

With a well tuned  $\beta$ , ATAC can compete with any policy within the data coverage.

N. With 
$$\beta = \Theta(N^{2/3})$$
. Then  $\forall \pi \in \Pi$ ,

average Bellman error of  $f_t$  on the distribution of  $\pi$ 

![](_page_65_Picture_10.jpeg)

### ATAC Theory (Informal)

**Robust Policy Improvement** 

Assume  $\mathcal{F}$  satisfies **realizability** without the need of completeness. If  $\mu \in \Pi$ , then  $J(\mu) - J(\bar{\pi})$ 

ATAC always improves over the behavior policy so long as  $\beta = o(N)$ .

$$\leq \mathcal{O}\left(\frac{1}{(1-\gamma)N^{1/2}} + \frac{\beta}{(1-\gamma)N}\right)$$

faster rate

![](_page_66_Picture_9.jpeg)

### Experimental Results

#### **Robust Policy Improvement**

ATAC's robustness property enables online HP selection. We can gradually increase  $\beta$  to tune its performance without breaking the baseline performance.

![](_page_67_Picture_4.jpeg)

![](_page_67_Figure_5.jpeg)

### Experimental Results

		Behavior	ATAC*	CQL	COMBO	TD3BC	IQL	BC
	halfcheetah-rand	-0.1	4.8	35.4	38.8	10.2	-	2.1
	walker2d-rand	0.0	8.0	7.0	7.0	1.4	-	1.6
	hopper-rand	1.2	31.8	10.8	17.9	11.0	-	9.8
	halfcheetah-med	40.6	54.3	44.4	54.2	42.8	47.4	36.1
Episode 13	walker2d-med	62.0	91.0	74.5	75.5	79.7	78.3	6.6
	hopper-med	44.2	102.8	86.6	94.9	<b>99.5</b>	66.3	29.0
Episode 1	halfcheetah-med-replay	27.1	49.5	46.2	55.1	43.3	44.2	38.4
1	walker2d-med-replay	14.8	94.1	32.6	56.0	25.2	73.9	11.3
	hopper-med-replay	14.9	102.8	48.6	73.1	31.4	94.7	11.8
	halfcheetah-med-exp	64.3	95.5	62.4	90.0	97.9	86.7	35.8
Episode 12	walker2d-med-exp	82.6	116.3	98.7	96.1	101.1	109.6	6.4
	hopper-med-exp	64.7	112.6	111.0	111.1	112.2	91.5	111.9
	pen-human	207.8	79.3	37.5	-	-	71.5	34.4
	hammer-human	25.4	6.7	4.4	-	-	1.4	1.5
	door-human	28.6	8.7	9.9	-	-	4.3	0.5
	relocate-human	86.1	0.3	0.2	-	-	0.1	0.0
	pen-cloned	107.7	73.9	39.2	-	-	37.3	56.9
	hammer-cloned	8.1	2.3	2.1	-	-	2.1	0.8
	door-cloned	12.1	8.2	0.4	-	-	1.6	-0.1
	relocate-cloned	28.7	0.8	-0.1	-	-	-0.2	-0.1
	pen-exp	105.7	159.5	107.0	-	-	-	85.1
	hammer-exp	96.3	128.4	86.7	-	-	-	125.6
	door-exp	100.5	105.5	101.5	-	-	-	34.9
	relocate-exp	101.6	106.5	95.0	-	-	-	101.3

#### ATAC achieves SOTA performance, outperforming baseline algorithms in most datasets

Datasets where ATAC is the best performing algorithm, with 9% improvement (median) compared with the best baseline algorithm.

![](_page_68_Figure_6.jpeg)