

# Practical Model Predictive Control

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**Computer Science**

# Congratulate yourself!



Analytically solve continuous state action MDP (LQR)



Handle non-linear costs, dynamics (iLQR)



Handle constraints (AuLa)



makeameme.org



# Today's plan: Let's interact (a lot!)





Nirvana!

Partial Observability

Non-convexity

Long Horizons





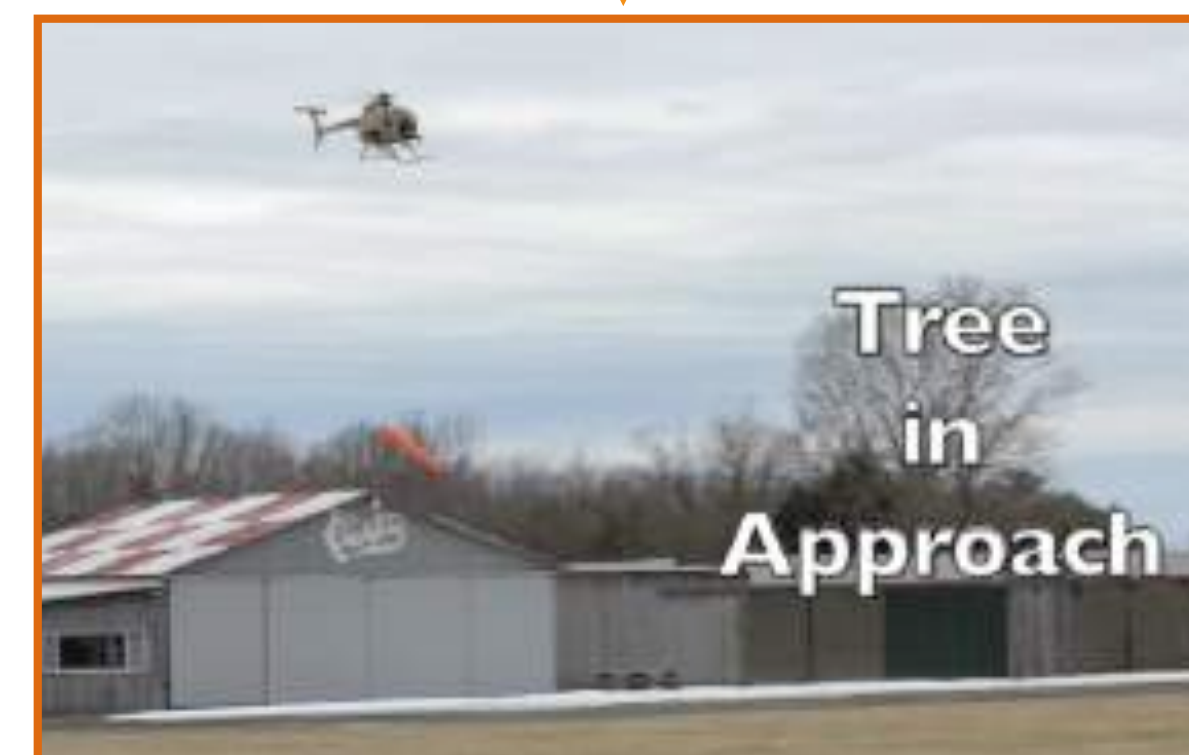
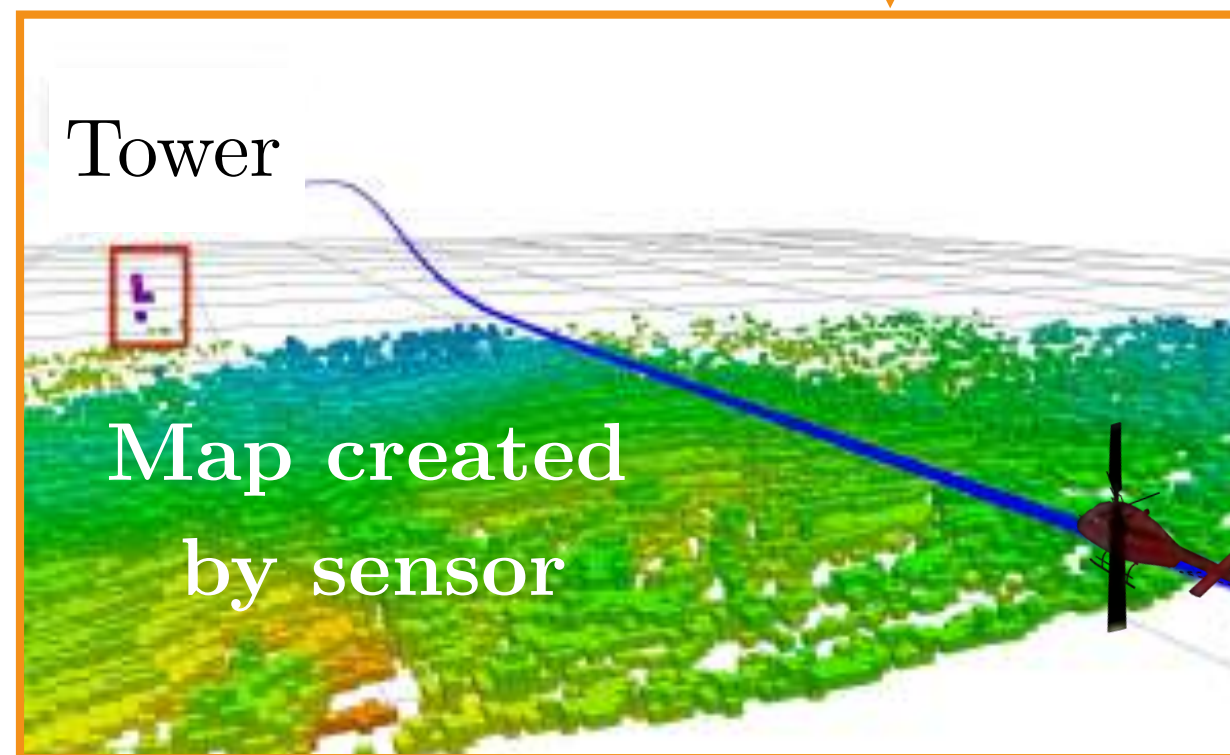
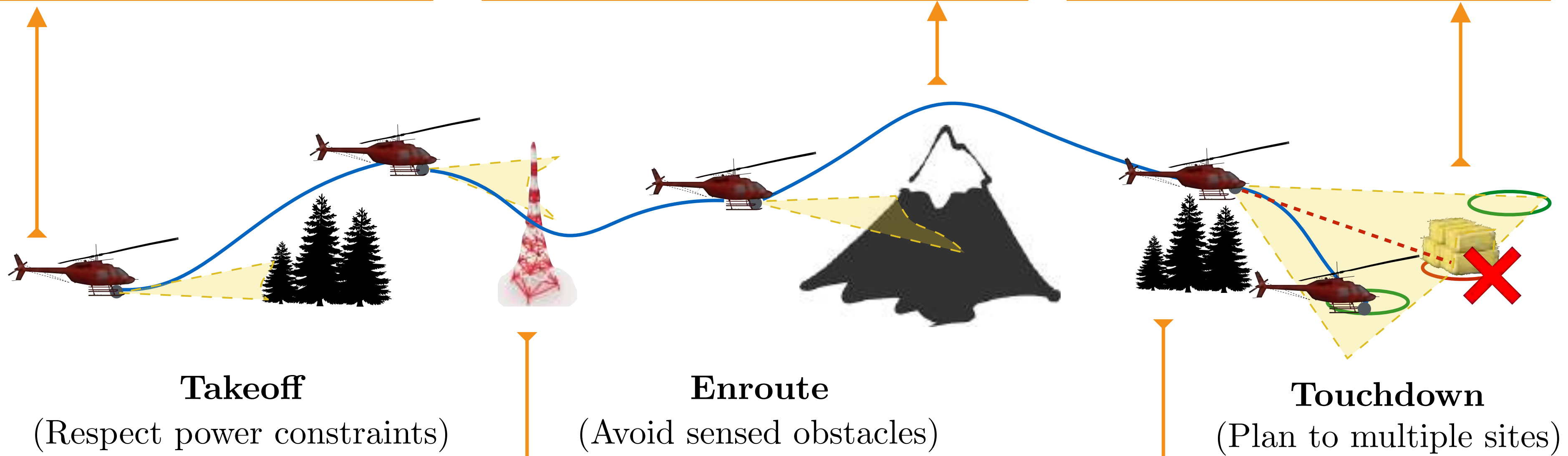
Nirvana!

Long Horizons



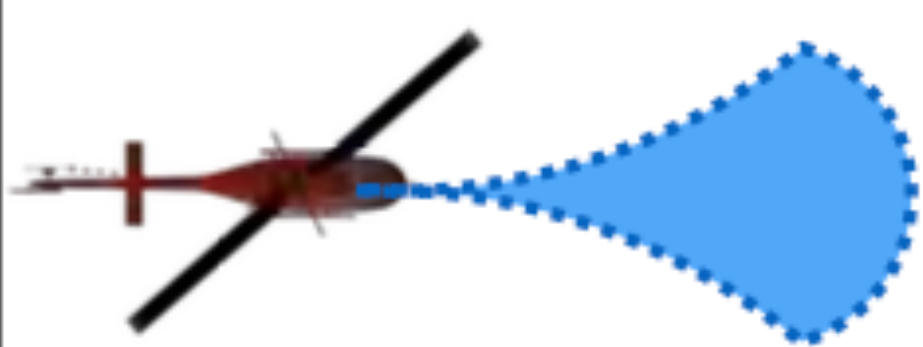






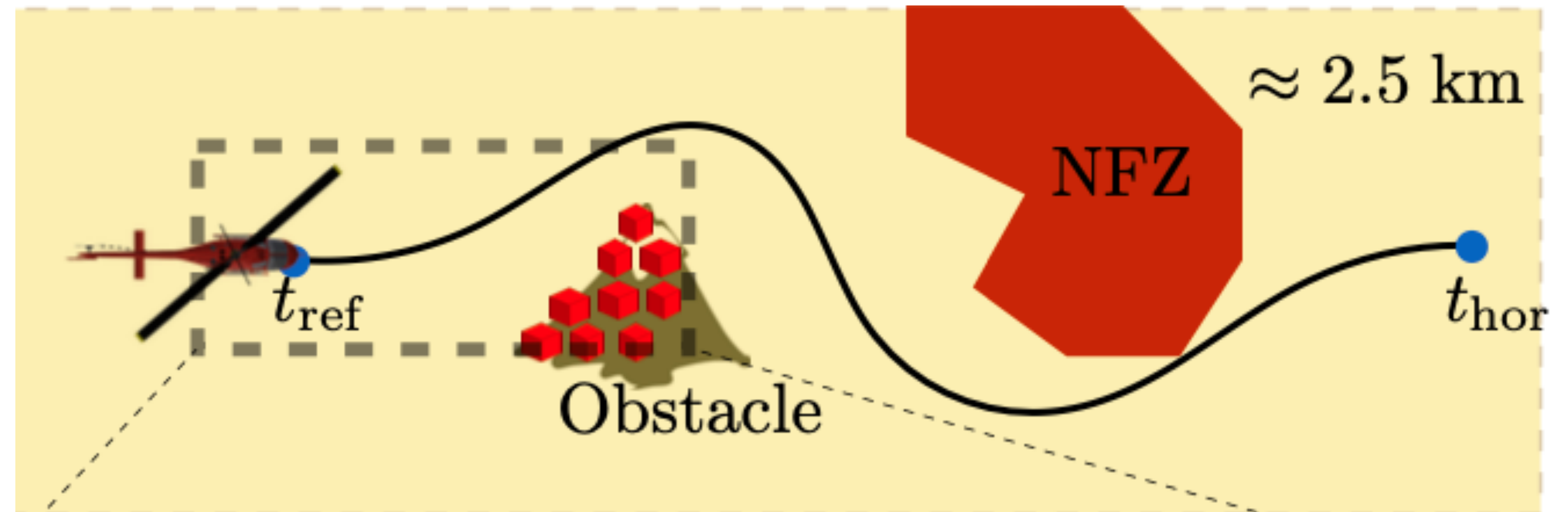


# Can apply iLQR!



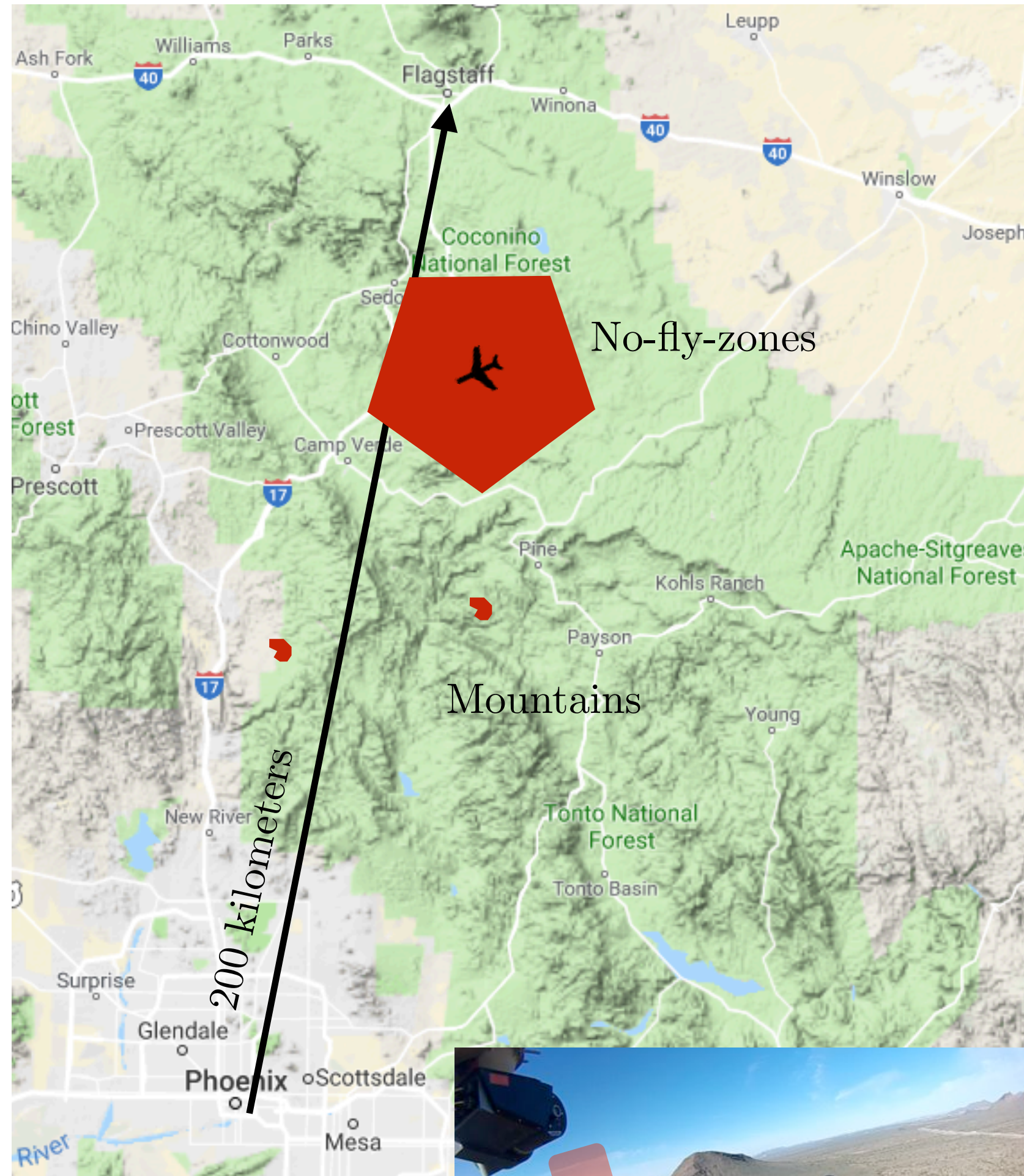
$\mathcal{F}_{\text{dyn}}(\sigma) = 0$   
 $\mathcal{H}_{\text{dyn}}(\sigma) \leq 0$

$s = (x, y, z, \psi,$   
 $\dot{x}, \dot{y}, \dot{z}, \dot{\psi},$   
 $\ddot{x}, \ddot{y}, \ddot{z}, \ddot{\psi})$





# Problem: How do we plan 200 km?



Example mission:

Fly from Phoenix to Flagstaff  
as fast as possible (200 km)

Problem:

Take forever to plan at high  
resolution ALL the way to goal





Activity!



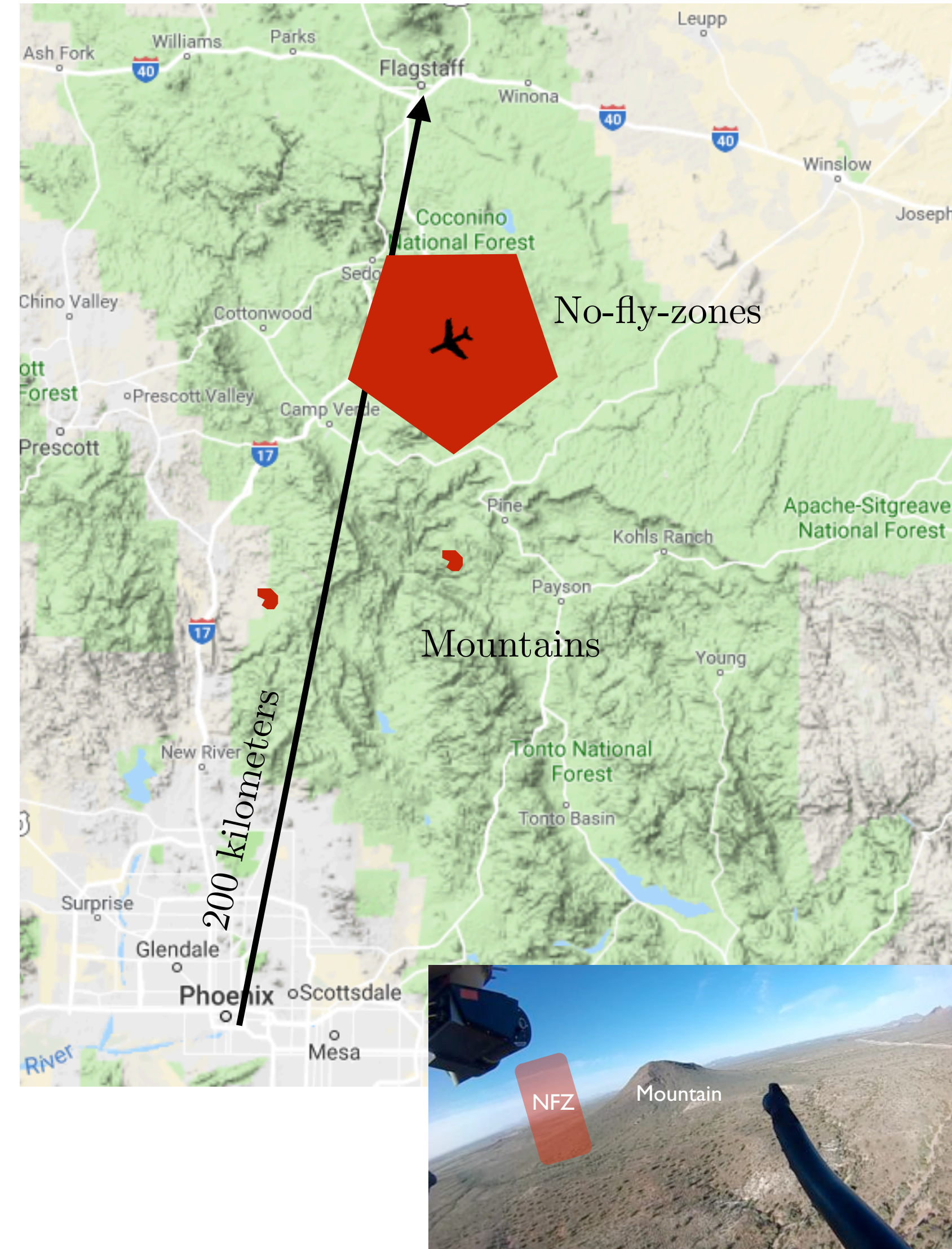


# Think-Pair-Share

Think (30 sec): How do we plan in real-time for a helicopter to go from A to B that is really really far apart?

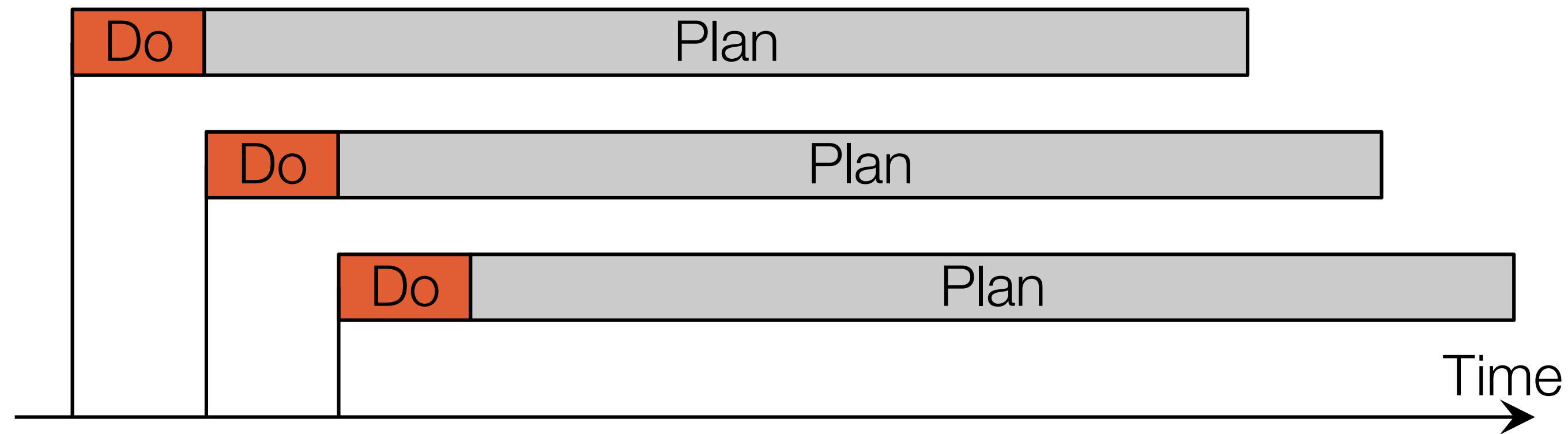
Pair: Find a partner

Share (45 sec): Partners exchange ideas





# Receding Horizon Control (also called MPC!)



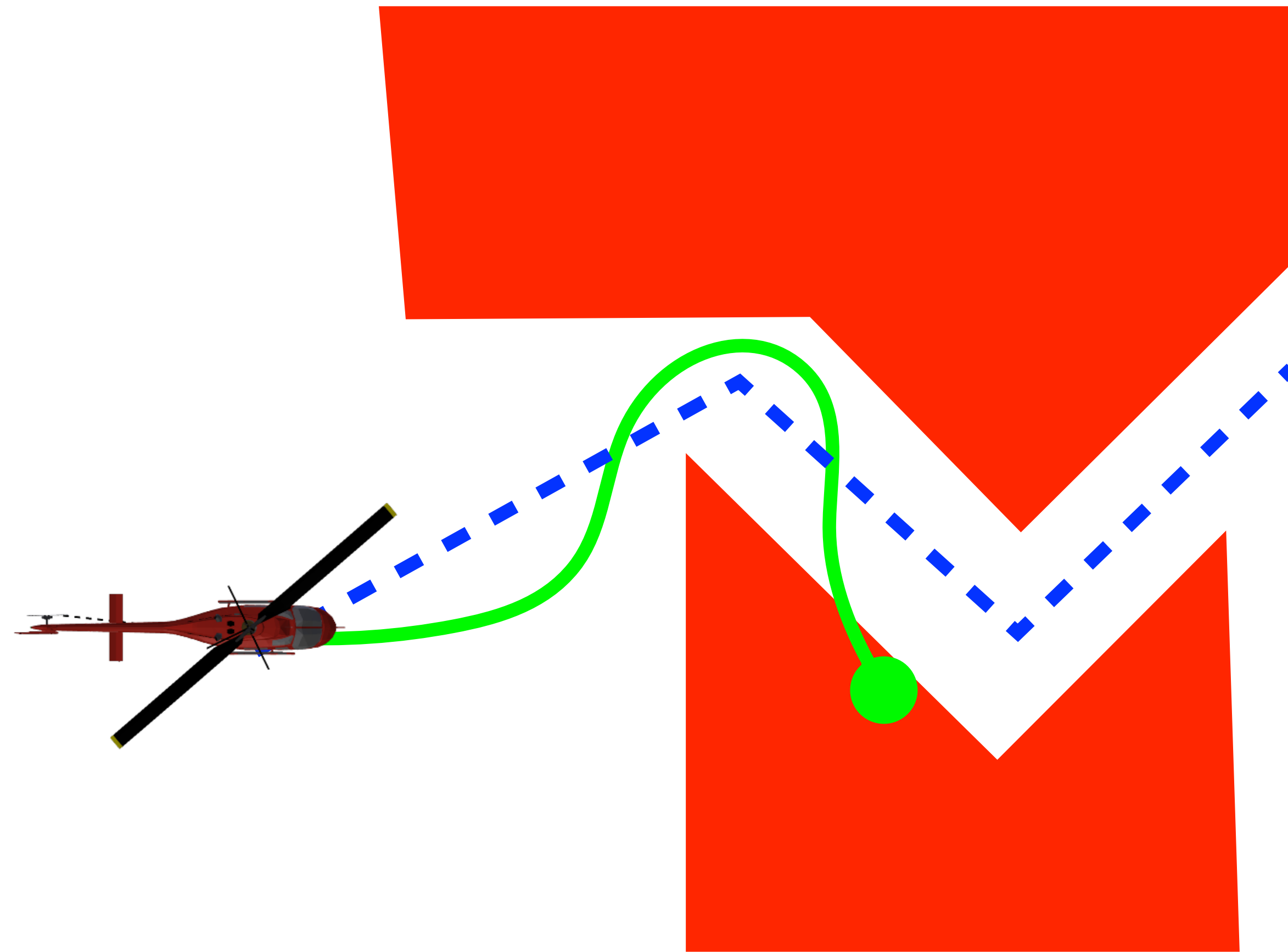
Step 1: Solve optimization problem to a horizon

Step 2: Execute the first control

Step 3: Repeat!

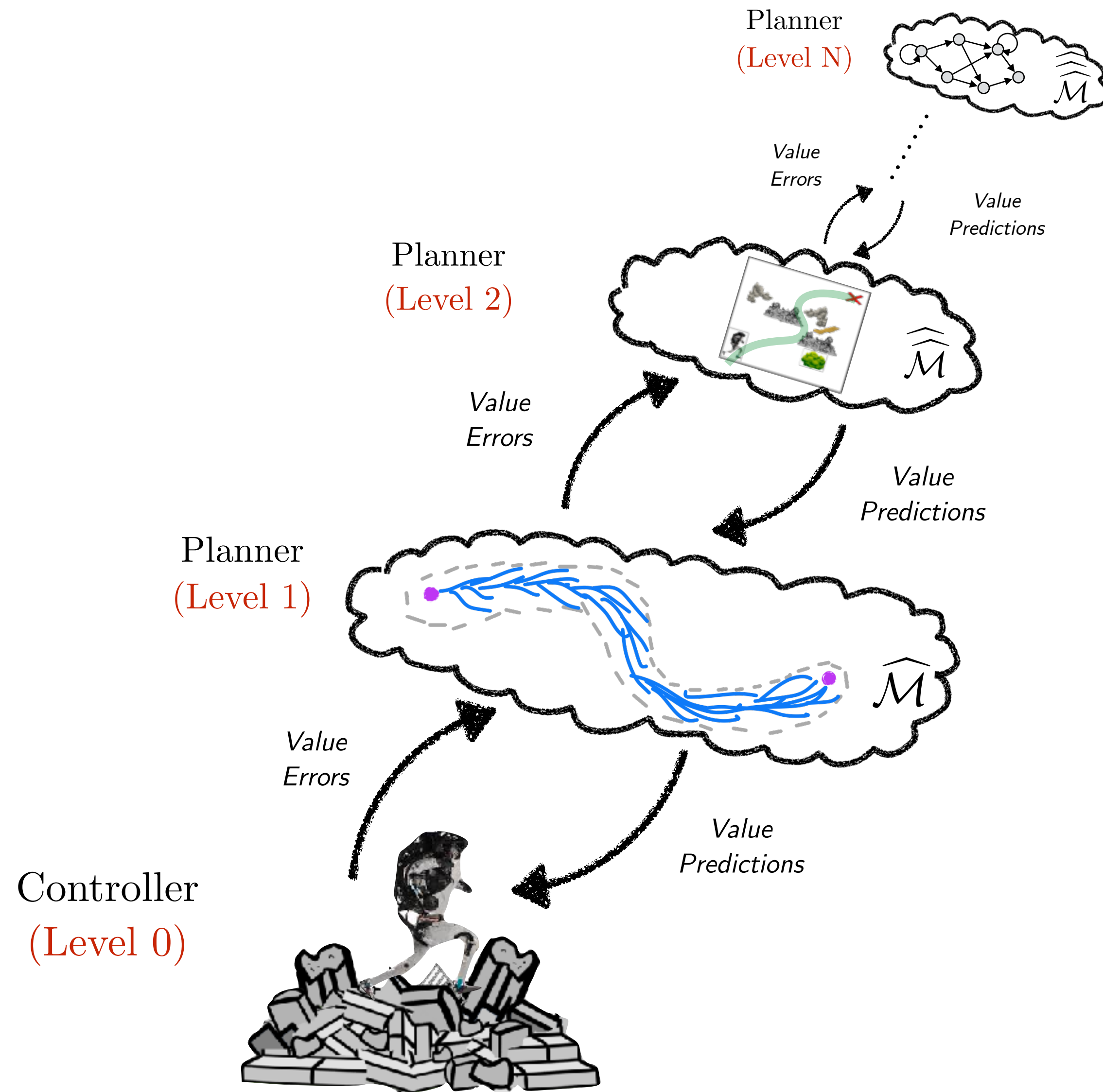


**Problem:** What happens when your global path is impossible to track?





# Hierarchy of value functions





Nirvana!

Non-convexity





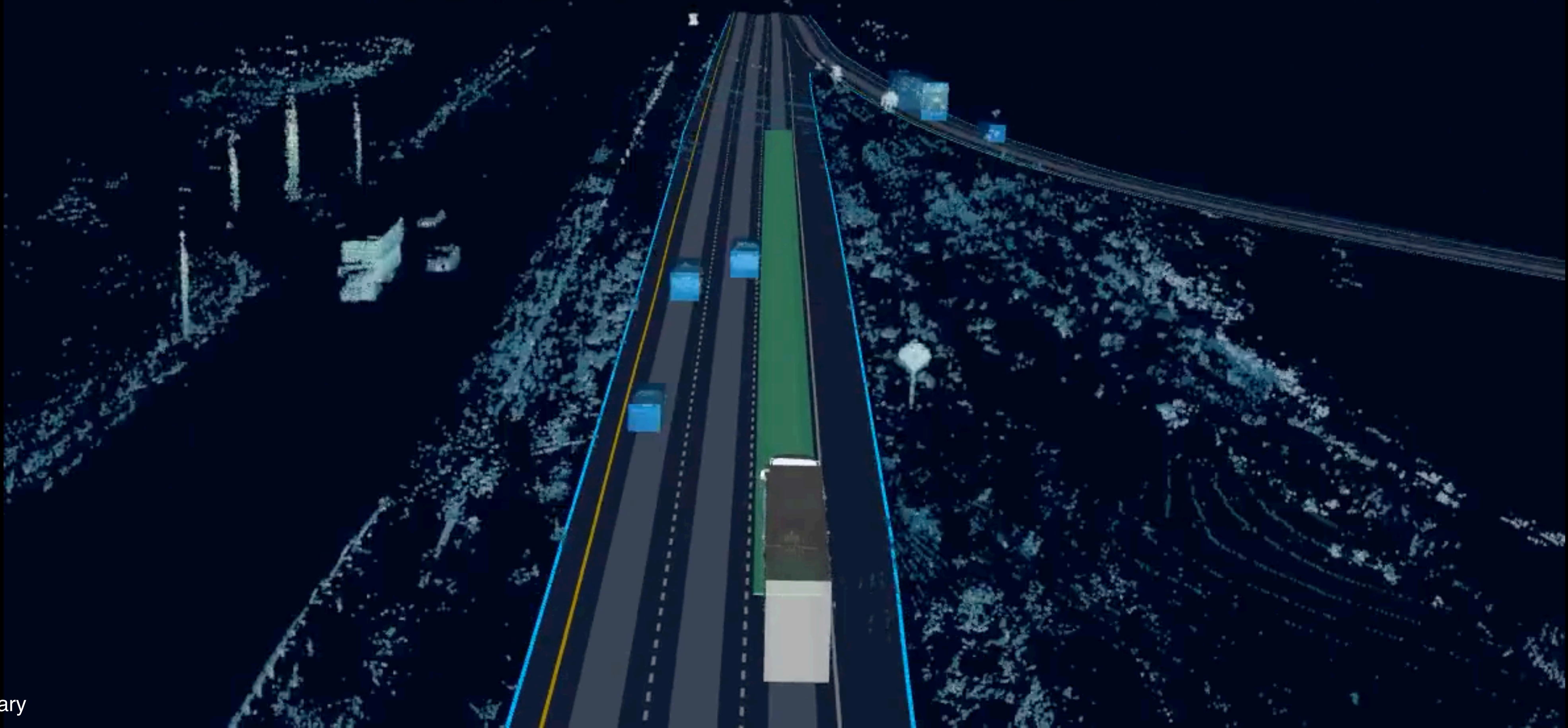
↑ STRAIGHT  
2.1 MI

AUTONOMY



65  
MPH

SPEED  
LIMIT  
75





ACTUAL  
← PLANNER

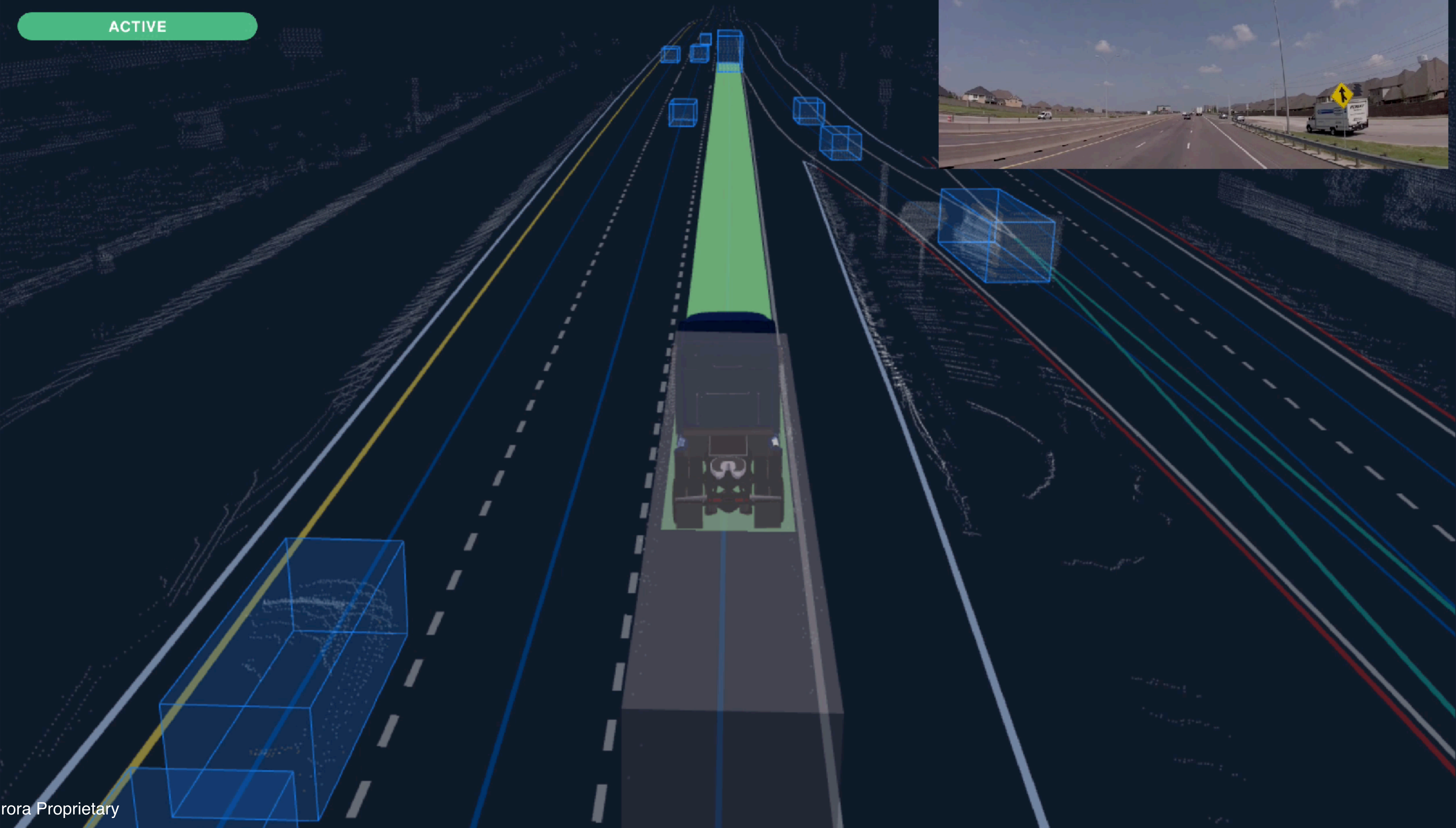


ACTUAL  
→ PLANNER

62.8  
MPH

SPEED  
LIMIT  
70

ACTIVE





ACTUAL  
← PLANNER

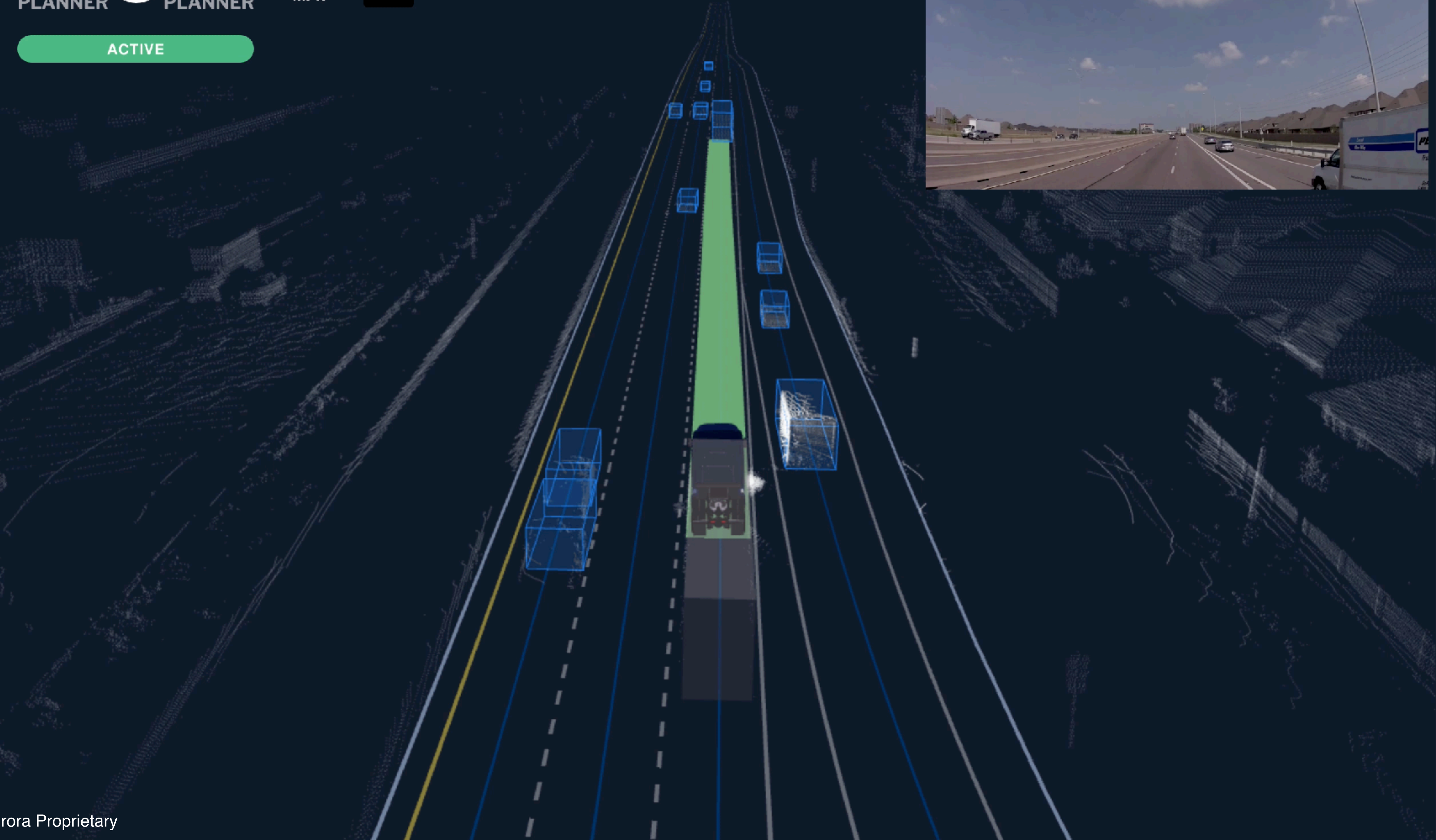


ACTUAL  
→ PLANNER

61.6  
MPH

SPEED  
LIMIT  
70

ACTIVE





Activity!



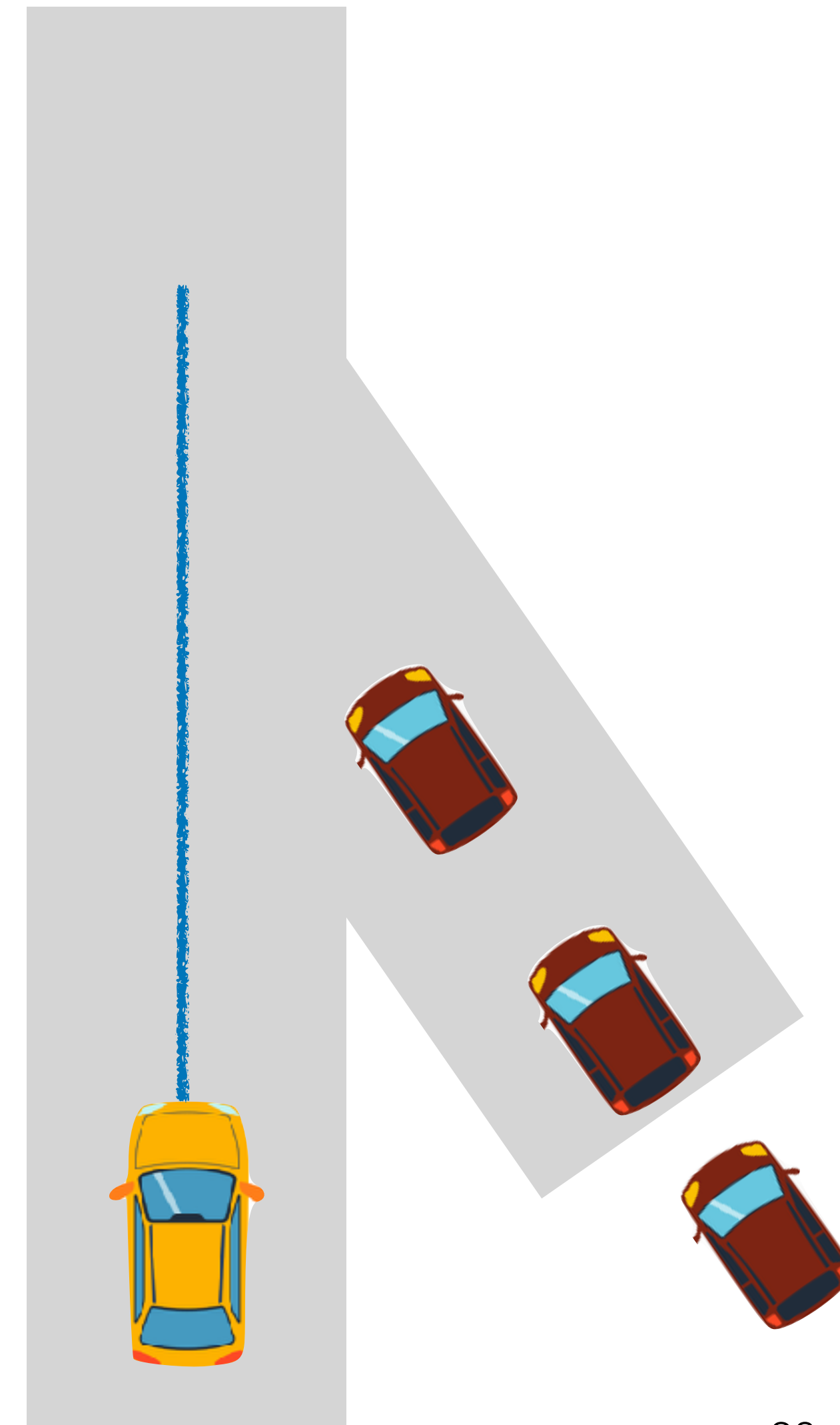


# Think-Pair-Share

Think (30 sec): How will you get iLQR to find the best plan to merge between multiple cars?

Pair: Find a partner

Share (45 sec): Partners exchange ideas





# Ways to initialize iLQR

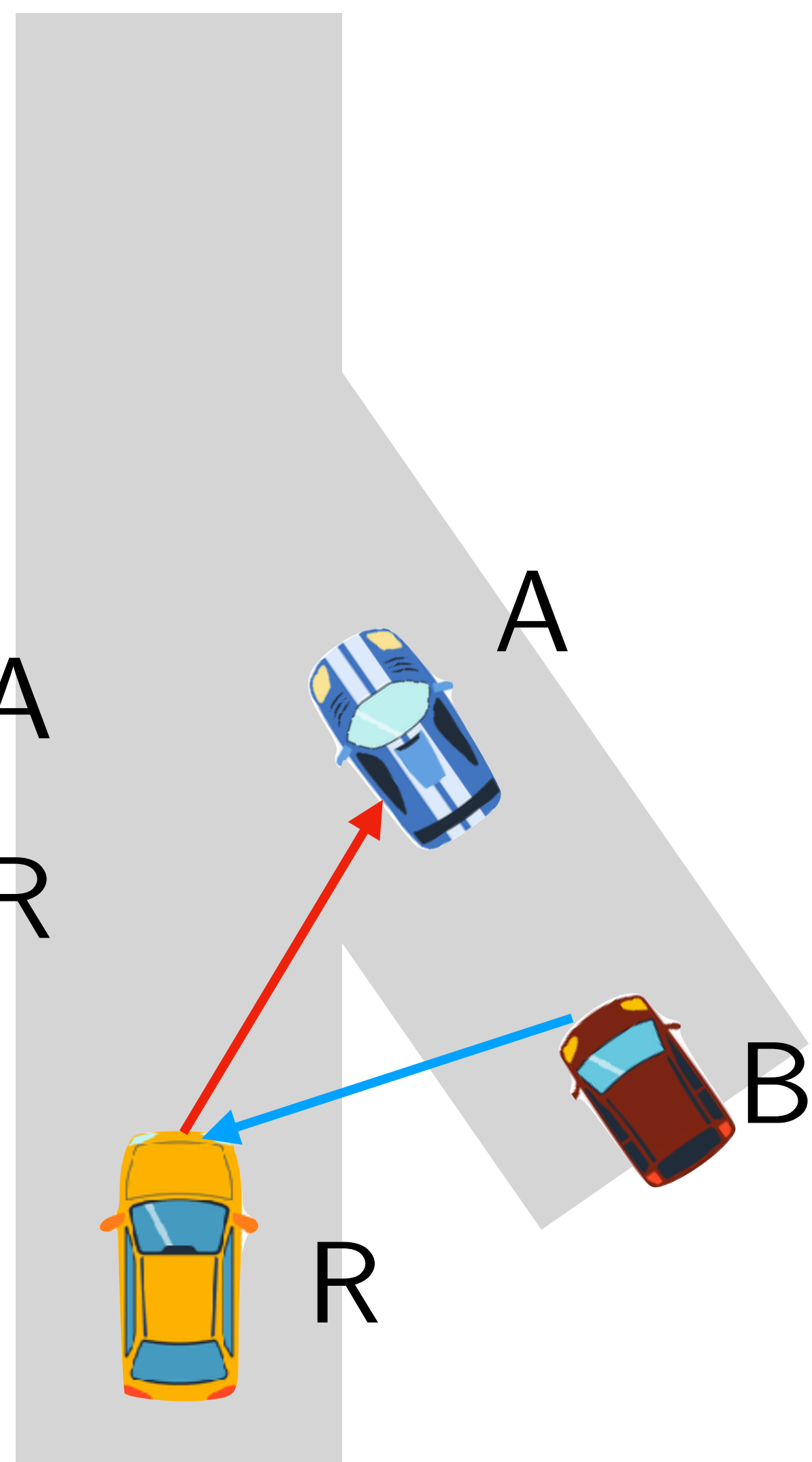
Try multiple random seeds

Try to find discrete modes

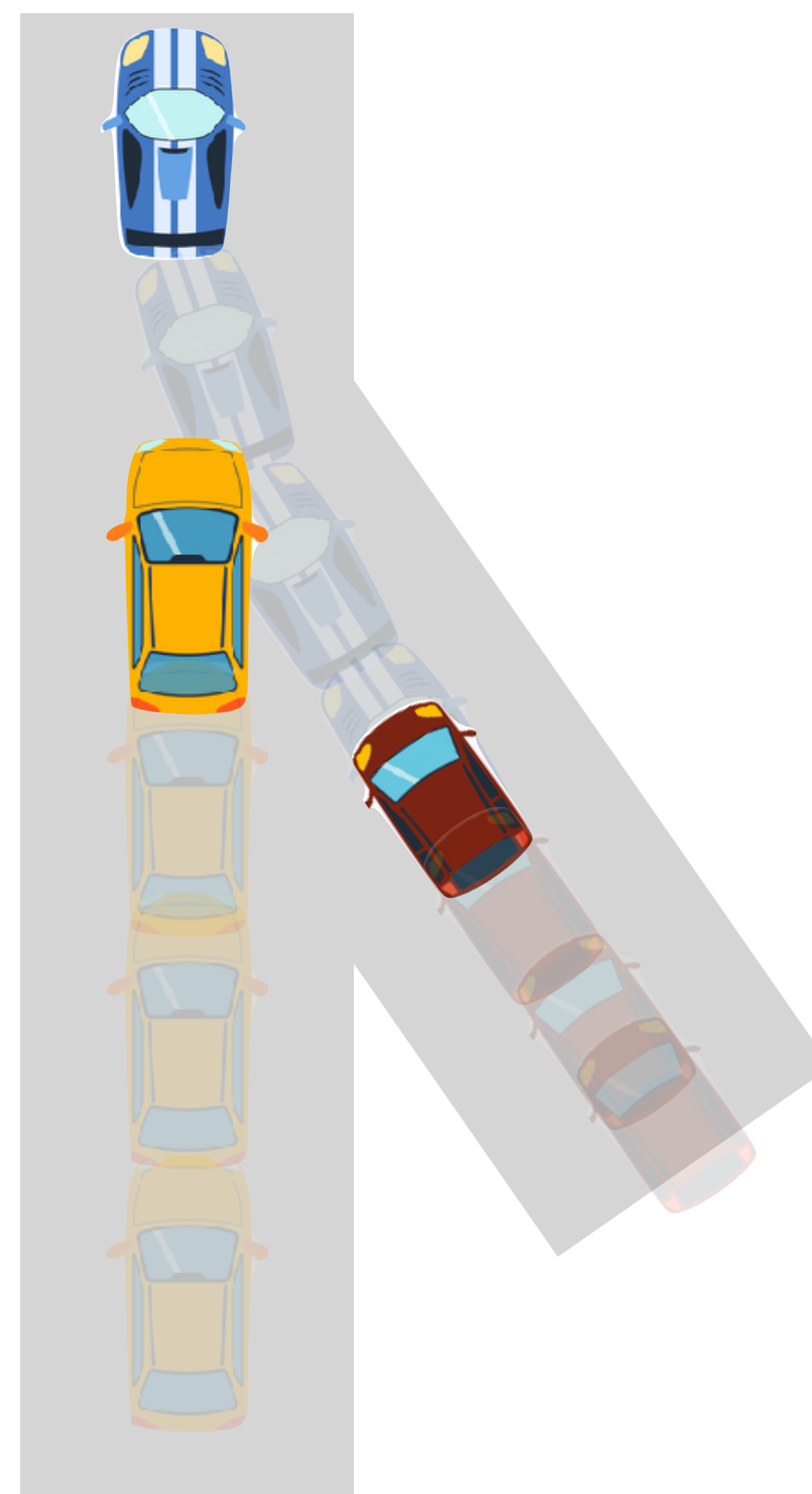


# Mode $\equiv$ A single basin of solution

R Yields to A  
B Yields to R



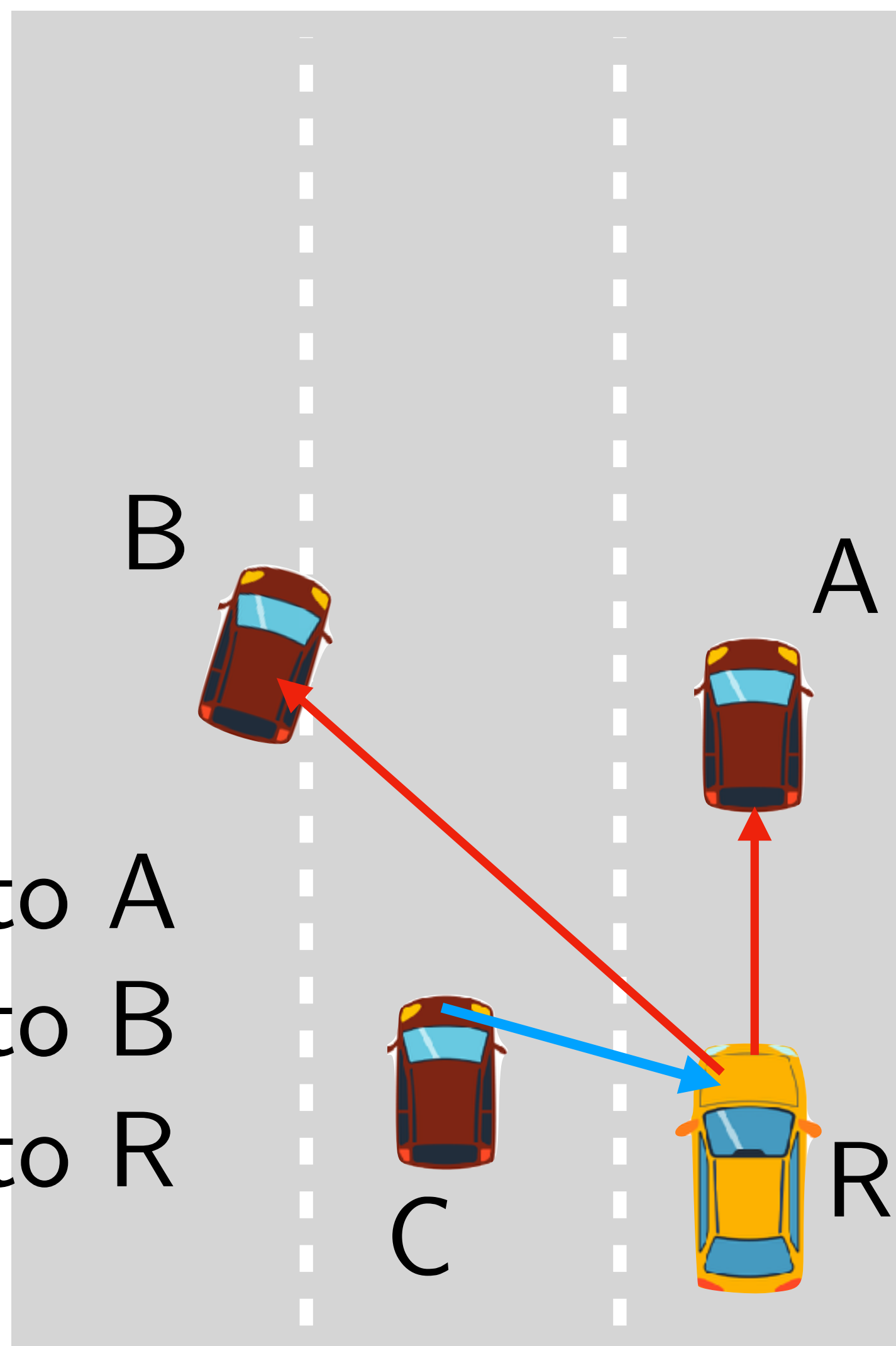
$\equiv$



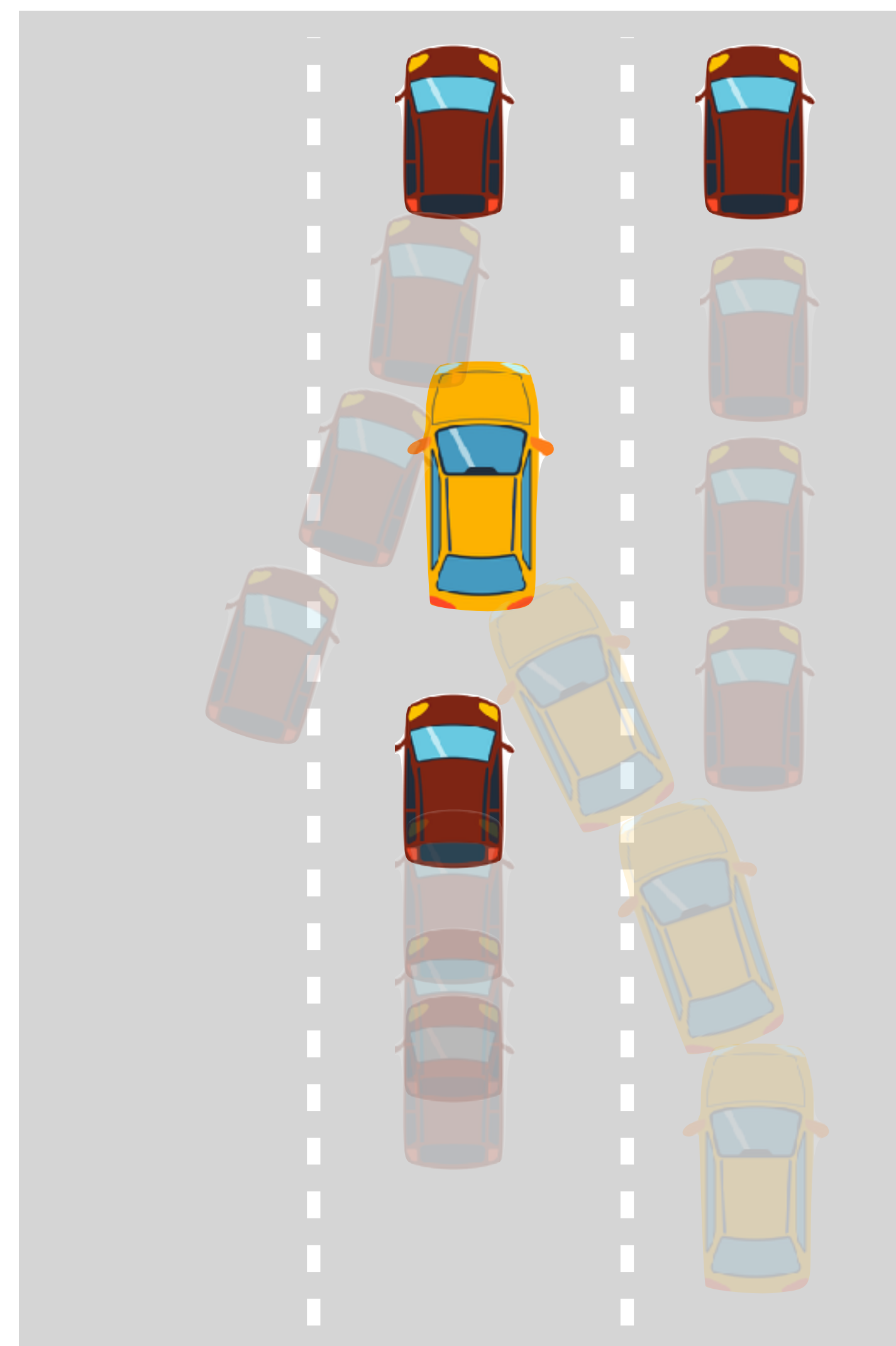


# Mode $\equiv$ A single basin of solution

R Yields to A  
R Yields to B  
C Yields to R



$\equiv$





# How do you find modes for this .... ?

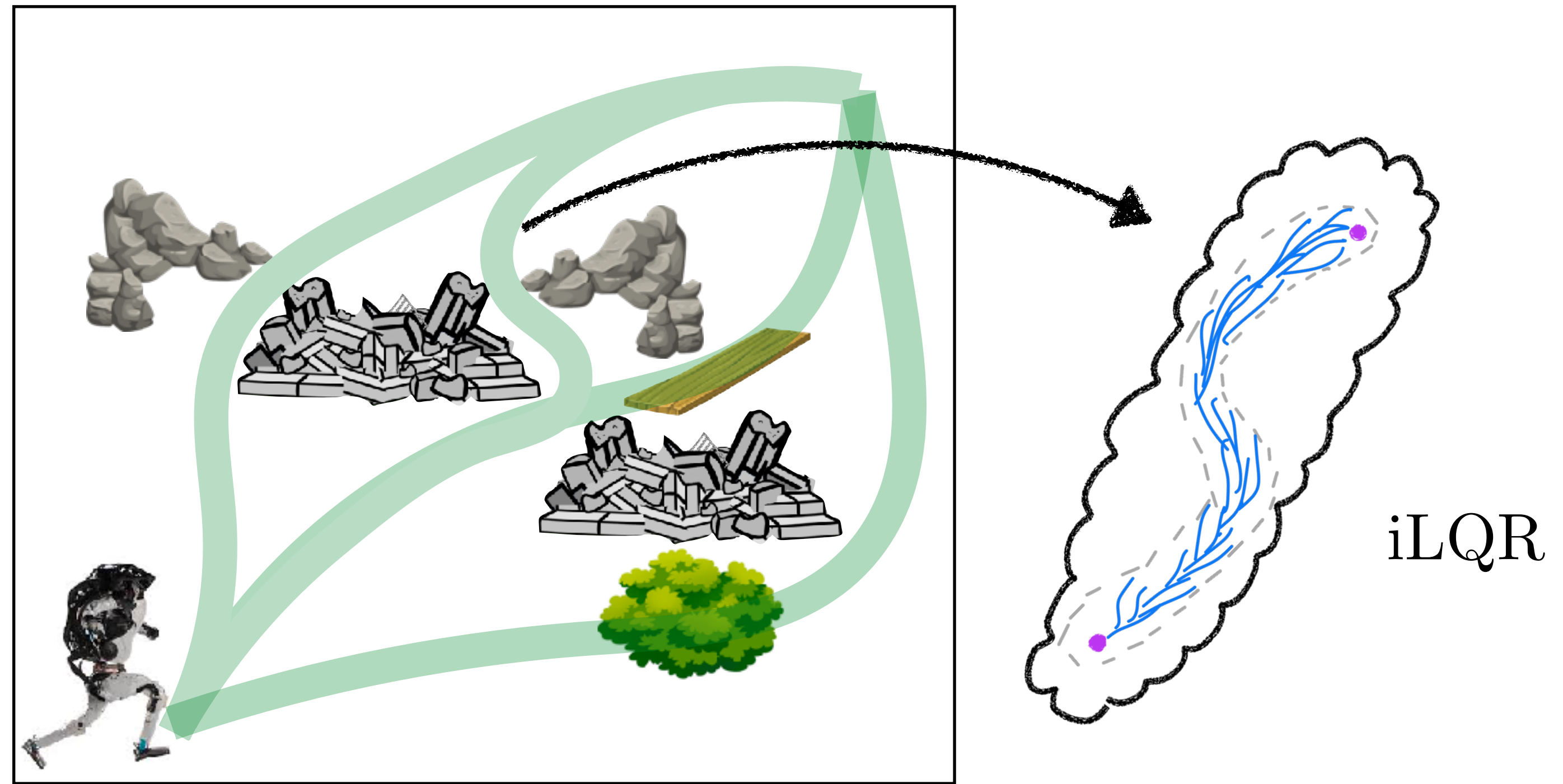




# Train a learner to predict modes

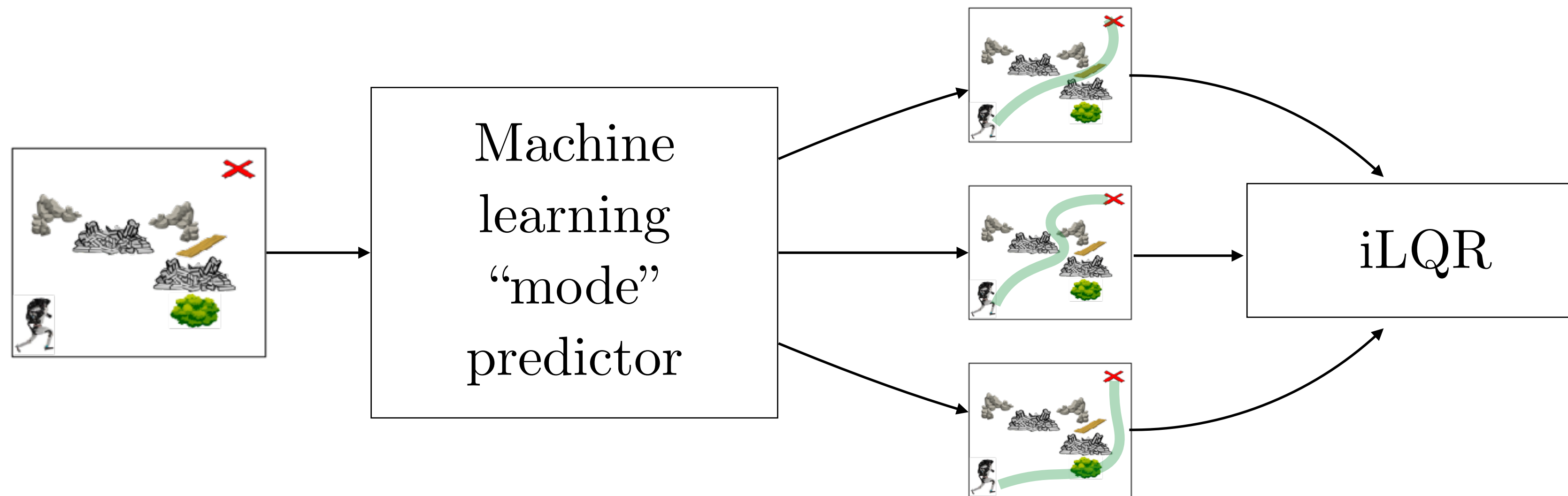
**mode:** a single basin of solution, e.g. workspace tube, sequence of phases, symbols, etc

[Toussiant'18],  
[Deits&Tedrake'15],  
[Mordatch etal'12]





# Train a learner to predict modes



Can be formulated as a list-prediction problem!



Nirvana!

Partial Observability





# The Blindfolded Robot: A Bayesian Approach to Planning with Contact Feedback

An overview of experiments

Brad Saund, Sanjiban Choudhury, Siddhartha Srinivasa, Dmitry Berenson



**M**  
ROBOTICS





# Partially Observable Markov Decision Process (POMDP)

NP-Hard at best

Undecidable in some cases

We will have a whole lecture on  
how to get around solving  
POMDPs!

