Pyramid blending



Create a Laplacian pyramid, blend each level

• Burt, P. J. and Adelson, E. H., <u>A multiresolution spline with applications to image mosaics</u>, ACM Transactions on Graphics, 42(4), October 1983, 217-236.



Alpha Blending



Encoding blend weights: $I(x,y) = (\alpha R, \alpha G, \alpha B, \alpha)$ color at $p = \frac{(\alpha_1 R_1, \alpha_1 G_1, \alpha_1 B_1) + (\alpha_2 R_2, \alpha_2 G_2, \alpha_2 B_2) + (\alpha_3 R_3, \alpha_3 G_3, \alpha_3 B_3)}{\alpha_1 + \alpha_2 + \alpha_3}$

Implement this in two steps:

- 1. accumulate: add up the (α premultiplied) RGB α values at each pixel
- 2. normalize: divide each pixel's accumulated RGB by its α value

Q: what if $\alpha = 0$?

Poisson Image Editing



sources/destinations

cloning

- seamless cloning
- For more info: Perez et al, SIGGRAPH 2003
 - <u>http://research.microsoft.com/vision/cambridge/papers/perez_siggraph03.pdf</u>

Some panorama examples



Before Siggraph Deadline: <u>http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/d</u> <u>ougz/siggraph-hires.html</u>

Magic: ghost removal



M. Uyttendaele, A. Eden, and R. Szeliski.

Eliminating ghosting and exposure artifacts in image mosaics.

In Proceedings of the Interational Conference on Computer Vision and Pattern Recognition, volume 2, pages 509--516, Kauai, Hawaii, December 2001.

Magic: ghost removal



M. Uyttendaele, A. Eden, and R. Szeliski.

Eliminating ghosting and exposure artifacts in image mosaics.

In Proceedings of the Interational Conference on Computer Vision and Pattern Recognition, volume 2, pages 509--516, Kauai, Hawaii, December 2001.

Some panorama examples

• Every image on Google Streetview





Questions?

CS6670: Computer Vision Noah Snavely

Lecture 8: Single-view Modeling



Projective geometry



Ames Room

- Readings
 - Mundy, J.L. and Zisserman, A., Geometric Invariance in Computer Vision, Appendix: Projective Geometry for Machine Vision, MIT Press, Cambridge, MA, 1992, (read 23.1 - 23.5, 23.10)
 - available online: <u>http://www.cs.cmu.edu/~ph/869/papers/zisser-mundy.pdf</u>

Projective geometry—what's it good for?

- Uses of projective geometry
 - Drawing
 - Measurements
 - Mathematics for projection
 - Undistorting images
 - Camera pose estimation
 - Object recognition



Paolo Uccello

Applications of projective geometry



Vermeer's Music Lesson



Reconstructions by Criminisi et al.

Measurements on planes



Point and line duality

- A line I is a homogeneous 3-vector
- It is \perp to every point (ray) **p** on the line: **I p**=0



What is the line I spanned by rays **p**₁ and **p**₂?

- I is \perp to $\mathbf{p_1}$ and $\mathbf{p_2} \implies \mathbf{I} = \mathbf{p_1} \times \mathbf{p_2}$
- I can be interpreted as a *plane normal*

What is the intersection of two lines I_1 and I_2 ?

• **p** is \perp to **I**₁ and **I**₂ \Rightarrow **p** = **I**₁ \times **I**₂

Points and lines are *dual* in projective space



- Ideal point ("point at infinity")
 - $p \cong (x, y, 0) parallel to image plane$
 - It has infinite image coordinates

Ideal line

- $I \cong (a, b, 0)$ parallel to image plane
- Corresponds to a line in the image (finite coordinates)
 - goes through image origin (principle point)

3D projective geometry

- These concepts generalize naturally to 3D
 - Homogeneous coordinates
 - Projective 3D points have four coords: **P** = (X,Y,Z,W)
 - Duality
 - A plane **N** is also represented by a 4-vector
 - Points and planes are dual in 3D: **N P**=0
 - Three points define a plane, three planes define a point

3D to 2D: perspective projection

Projection:

Vanishing points (1D)



- Vanishing point
 - projection of a point at infinity
 - can often (but not always) project to a finite point in the image

	center	
image plane		





- Properties
 - Any two parallel lines (in 3D) have the same vanishing point v
 - The ray from **C** through **v** is parallel to the lines
 - An image may have more than one vanishing point
 - in fact, every image point is a potential vanishing point

Two point perspective



Three point perspective



Questions?

Vanishing lines



- Multiple Vanishing Points
 - Any set of parallel lines on the plane define a vanishing point
 - The union of all of these vanishing points is the *horizon line*
 - also called vanishing line
 - Note that different planes (can) define different vanishing lines

Vanishing lines



- Multiple Vanishing Points
 - Any set of parallel lines on the plane define a vanishing point
 - The union of all of these vanishing points is the *horizon line*
 - also called vanishing line
 - Note that different planes (can) define different vanishing lines





- Properties $\mathbf{v} = \mathbf{\Pi} \mathbf{P}_{\infty}$
 - \mathbf{P}_{∞} is a point at *infinity*, **v** is its projection
 - Depends only on line *direction*
 - Parallel lines P_0 + tD, P_1 + tD intersect at P_{∞}



• Properties

- I is intersection of horizontal plane through **C** with image plane
- Compute I from two sets of parallel lines on ground plane
- All points at same height as C project to I
 - points higher than C project above I
- Provides way of comparing height of objects in the scene



Fun with vanishing points



Perspective cues



Perspective cues



Perspective cues



Comparing heights



Measuring height


Computing vanishing points (from lines)



• Intersect p_1q_1 with p_2q_2 $v = (p_1 \times q_1) \times (p_2 \times q_2)$

Least squares version

- Better to use more than two lines and compute the "closest" point of intersection
- See notes by <u>Bob Collins</u> for one good way of doing this:
 - <u>http://www-2.cs.cmu.edu/~ph/869/www/notes/vanishing.txt</u>

Measuring height without a ruler



Compute Z from image measurements

• Need more than vanishing points to do this

The cross ratio

- A Projective Invariant
 - Something that does not change under projective transformations (including perspective projection)

The cross-ratio of 4 collinear points



Can permute the point ordering

 $\frac{\|\mathbf{P}_1 - \mathbf{P}_3\| \|\mathbf{P}_4 - \mathbf{P}_2\|}{\|\mathbf{P}_1 - \mathbf{P}_2\| \|\mathbf{P}_4 - \mathbf{P}_3\|}$

• 4! = 24 different orders (but only 6 distinct values)

This is the fundamental invariant of projective geometry

Measuring height







St. Jerome in his Study, H. Steenwick





Flagellation, Piero della Francesca



video by Antonio Criminisi





Questions?

• 3-minute break

Camera calibration

- Goal: estimate the camera parameters
 - Version 1: solve for projection matrix

- Version 2: solve for camera parameters separately
 - intrinsics (focal length, principle point, pixel size)
 - extrinsics (rotation angles, translation)
 - radial distortion

Vanishing points and projection matrix

• $\boldsymbol{\pi}_1 = \boldsymbol{\Pi} \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T = \boldsymbol{v}_x$ (X vanishing point)

• similarly,
$$\boldsymbol{\pi}_2 = \boldsymbol{v}_Y, \ \boldsymbol{\pi}_3 = \boldsymbol{v}_Z$$

• $\boldsymbol{\pi}_4 = \boldsymbol{\Pi} \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^T = \text{projection of world origin}$

$$\mathbf{\Pi} = \begin{bmatrix} \mathbf{v}_X & \mathbf{v}_Y & \mathbf{v}_Z & \mathbf{0} \end{bmatrix}$$

Not So Fast! We only know v's up to a scale factor

$$\mathbf{\Pi} = \begin{bmatrix} a \, \mathbf{v}_X & b \, \mathbf{v}_Y & c \, \mathbf{v}_Z & \mathbf{0} \end{bmatrix}$$

• Can fully specify by providing 3 reference points

Calibration using a reference object

- Place a known object in the scene
 - identify correspondence between image and scene
 - compute mapping from scene to image



lssues

- must know geometry very accurately
- must know 3D->2D correspondence

Estimating the projection matrix

- Place a known object in the scene
 - identify correspondence between image and scene
 - compute mapping from scene to image



$$\begin{bmatrix} u_i \\ v_i \\ 1 \end{bmatrix} \cong \begin{bmatrix} m_{00} & m_{01} & m_{02} & m_{03} \\ m_{10} & m_{11} & m_{12} & m_{13} \\ m_{20} & m_{21} & m_{22} & m_{23} \end{bmatrix} \begin{bmatrix} X_i \\ Y_i \\ Z_i \\ 1 \end{bmatrix}$$

Direct linear calibration

$$\begin{bmatrix} u_i \\ v_i \\ 1 \end{bmatrix} \cong \begin{bmatrix} m_{00} & m_{01} & m_{02} & m_{03} \\ m_{10} & m_{11} & m_{12} & m_{13} \\ m_{20} & m_{21} & m_{22} & m_{23} \end{bmatrix} \begin{bmatrix} X_i \\ Y_i \\ Z_i \\ 1 \end{bmatrix}$$

$$u_{i} = \frac{m_{00}X_{i} + m_{01}Y_{i} + m_{02}Z_{i} + m_{03}}{m_{20}X_{i} + m_{21}Y_{i} + m_{22}Z_{i} + m_{23}}$$
$$v_{i} = \frac{m_{10}X_{i} + m_{11}Y_{i} + m_{12}Z_{i} + m_{13}}{m_{20}X_{i} + m_{21}Y_{i} + m_{22}Z_{i} + m_{23}}$$

 $u_i(m_{20}X_i + m_{21}Y_i + m_{22}Z_i + m_{23}) = m_{00}X_i + m_{01}Y_i + m_{02}Z_i + m_{03}$ $v_i(m_{20}X_i + m_{21}Y_i + m_{22}Z_i + m_{23}) = m_{10}X_i + m_{11}Y_i + m_{12}Z_i + m_{13}$

$$\begin{bmatrix} X_i & Y_i & Z_i & 1 & 0 & 0 & 0 & 0 & -u_i X_i & -u_i Y_i & -u_i Z_i & -u_i \\ 0 & 0 & 0 & 0 & X_i & Y_i & Z_i & 1 & -v_i X_i & -v_i Y_i & -v_i Z_i & -v_i \end{bmatrix} \begin{bmatrix} m_{00} \\ m_{01} \\ m_{02} \\ m_{03} \\ m_{10} \\ m_{11} \\ m_{12} \\ m_{13} \\ m_{20} \\ m_{21} \\ m_{22} \\ m_{23} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Direct linear calibration



Can solve for m_{ii} by linear least squares

• use eigenvector trick that we used for homographies

Direct linear calibration

• Advantage:

Very simple to formulate and solve

- Disadvantages:
 - Doesn't tell you the camera parameters
 - Doesn't model radial distortion
 - Hard to impose constraints (e.g., known f)
 - Doesn't minimize the right error function

For these reasons, *nonlinear methods* are preferred

- Define error function E between projected 3D points and image positions
 - E is nonlinear function of intrinsics, extrinsics, radial distortion
- Minimize E using nonlinear optimization techniques

Alternative: multi-plane calibration



Images courtesy Jean-Yves Bouguet, Intel Corp.

Advantage

- Only requires a plane
- Don't have to know positions/orientations
- Good code available online! (including in OpenCV)
 - Matlab version by Jean-Yves Bouget:
 http://www.vision.caltech.edu/bouguetj/calib_doc/index.html
 - Zhengyou Zhang's web site: <u>http://research.microsoft.com/~zhang/Calib/</u>

Some Related Techniques

- Image-Based Modeling and Photo Editing
 - Mok et al., SIGGRAPH 2001
 - <u>http://graphics.csail.mit.edu/ibedit/</u>
- Single View Modeling of Free-Form Scenes
 - Zhang et al., CVPR 2001
 - <u>http://grail.cs.washington.edu/projects/svm/</u>
- Tour Into The Picture
 - Anjyo et al., SIGGRAPH 1997
 - <u>http://koigakubo.hitachi.co.jp/little/DL_TipE.html</u>

More than one view?







Public Library, Stereoscopic Looking Room, Chicago, by Phillips, 1923





Mark Twain at Pool Table", no date, UCR Museum of Photography



Epipolar geometry



epipolar lines

Two images captured by a purely horizontal translating camera (*rectified* stereo pair)

$$x_2 - x_1 =$$
the *disparity* of pixel (x_1, y_1)

Stereo matching algorithms

- Match Pixels in Conjugate Epipolar Lines
 - Assume brightness constancy
 - This is a tough problem
 - Numerous approaches
 - A good survey and evaluation: http://www.middlebury.edu/stereo/

Your basic stereo algorithm



For each epipolar line

For each pixel in the left image

- compare with every pixel on same epipolar line in right image
- pick pixel with minimum match cost

Improvement: match windows

Window size







W = 3

W = 20

Better results with adaptive window

- T. Kanade and M. Okutomi, <u>A Stereo Matching Algorithm</u> <u>with an Adaptive Window: Theory and Experiment</u>,, Proc. International Conference on Robotics and Automation, 1991.
- D. Scharstein and R. Szeliski. <u>Stereo matching with</u> <u>nonlinear diffusion</u>. International Journal of Computer Vision, 28(2):155-174, July 1998

Stereo results

- Data from University of Tsukuba
- Similar results on other images without ground truth





Ground truth



Results with window search



Window-based matching (best window size) Ground truth

Better methods exist...



State of the art method

Ground truth

Boykov et al., <u>Fast Approximate Energy Minimization via Graph Cuts</u>, International Conference on Computer Vision, September 1999.

For the latest and greatest: <u>http://www.middlebury.edu/stereo/</u>

Stereo as energy minimization



- What defines a good stereo correspondence?
 - 1. Match quality
 - Want each pixel to find a good match in the other image
 - 2. Smoothness
 - If two pixels are adjacent, they should (usually) move about the same amount

Stereo as energy minimization

- Expressing this mathematically
 - 1. Match quality
 - Want each pixel to find a good match in the other image

$$matchCost = \sum_{x,y} \|I(x,y) - J(x+d_{xy},y)\|$$

- 2. Smoothness
 - If two pixels are adjacent, they should (usually) move about the same amount

$$smoothnessCost = \sum_{neighbor \ pixels \ p,q} |d_p - d_q|$$

- We want to minimize *Energy* = matchCost + smoothnessCost
 - This is a special type of energy function known as an MRF (Markov Random Field)
 - Effective and fast algorithms have been recently developed:
 - Graph cuts, belief propagation....
 - for more details (and code): <u>http://vision.middlebury.edu/MRF/</u>
 - Great <u>tutorials</u> available online (including video of talks)

Depth from disparity



$$disparity = x - x' = \frac{baseline * f}{z}$$

Real-time stereo



<u>Nomad robot</u> searches for meteorites in Antartica <u>http://www.frc.ri.cmu.edu/projects/meteorobot/index.html</u>

- Used for robot navigation (and other tasks)
 - Several software-based real-time stereo techniques have been developed (most based on simple discrete search)
Stereo reconstruction pipeline

- Steps
 - Calibrate cameras
 - Rectify images
 - Compute disparity
 - Estimate depth

What will cause errors?

- Camera calibration errors
- Poor image resolution
- Occlusions
- Violations of brightness constancy (specular reflections)
- Large motions
- Low-contrast image regions

Active stereo with structured light







Li Zhang's one-shot stereo



Project "structured" light patterns onto the object
– simplifies the correspondence problem

Laser scanning





Digital Michelangelo Project http://graphics.stanford.edu/projects/mich/

- Optical triangulation
 - Project a single stripe of laser light
 - Scan it across the surface of the object
 - This is a very precise version of structured light scanning







