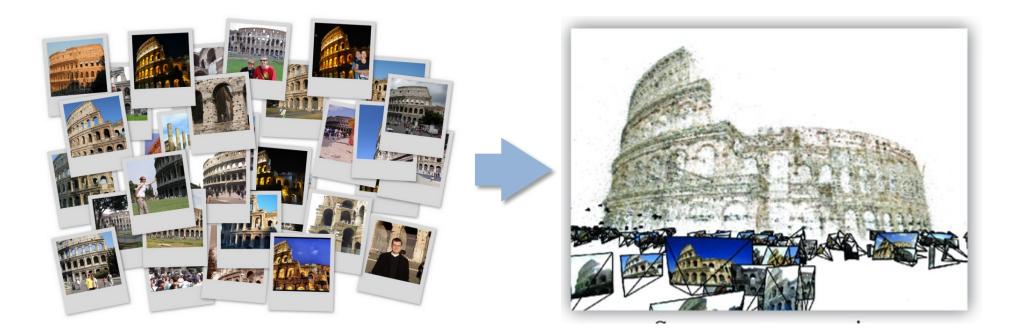
Quiz 7 (on Canvas) Closed book / closed note

Ends at 1:08pm

CS5670: Computer Vision

Structure from motion



Readings

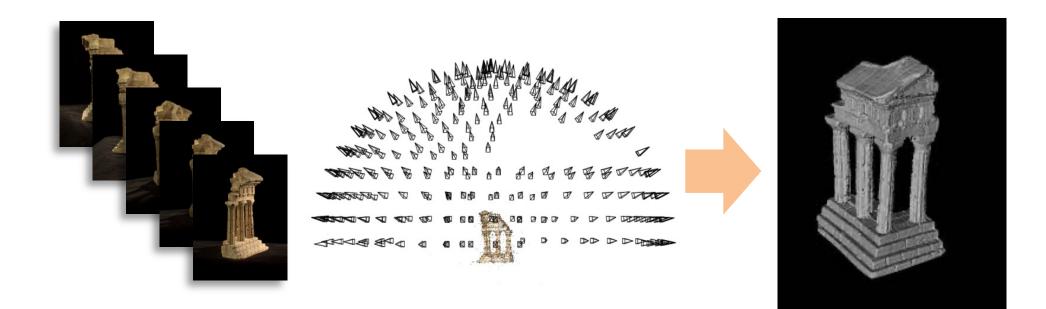
• Szeliski (2nd Edition), Chapter 11.4

Announcements

- Project 4 due tomorrow, 3/31, by 8pm
- Project 5 on NeRF coming up after Spring Break

Reminder: multi-view stereo

Problem formulation: given several images of the same object or scene, compute a representation of its 3D shape



Structure from motion

- Multi-view stereo assumes that cameras are calibrated – Extrinsics and intrinsics are known for all views
- How do we compute calibration if we don't know it? In general, this is called *structure from motion*

Large-scale structure from motion

Dubrovnik, Croatia. 4,619 images (out of an initial 57,845). Total reconstruction time: 23 hours Number of cores: 352

Two views



- Solve for Fundamental matrix / Essential matrix
- Factorize into intrinsics, rotation, and translation

What about more than two views?

• The geometry of three views is described by a 3 x 3 x 3 tensor called the *trifocal tensor*

- After this it starts to get complicated...
 - Instead, we explicitly solve for camera poses and scene geometry

Structure from motion

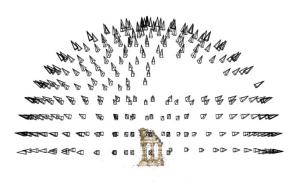
- Given many images, how can we
 - a) figure out where they were all taken from?
 - b) build a 3D model of the scene?



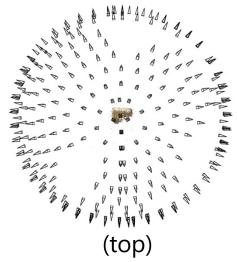
This is the **structure from motion (SfM)** problem

Structure from motion



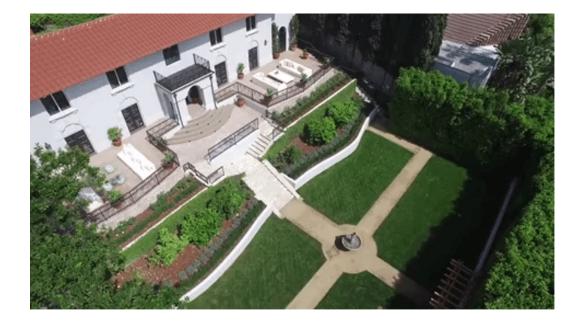


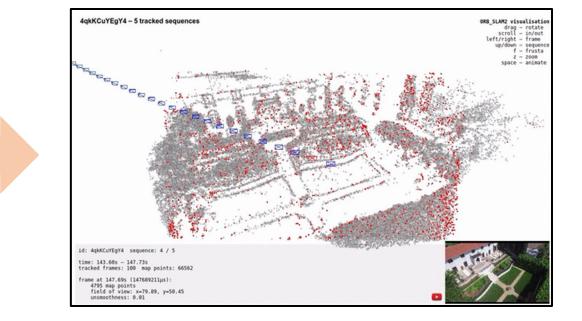
Reconstruction (side)



- Input: images with 2D points in correspondence $p_{i,j} = (u_{i,j}, v_{i,j})$
- Output
 - structure: 3D location \mathbf{x}_i for each point p_i
 - motion: camera parameters \mathbf{R}_j , \mathbf{t}_j & possibly \mathbf{K}_j
- Objective function: minimize *reprojection error*

Can also compute camera poses from video (often called Visual SLAM)

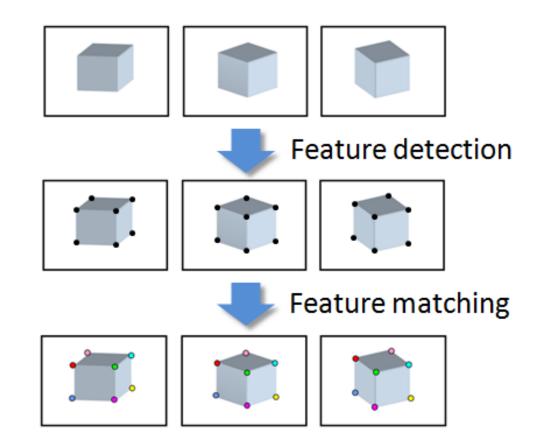




What we've seen so far...

- 2D transformations between images
 - Translations, affine transformations, homographies...
- Fundamental matrices
 - Represent relationships between 2D images in the form of corresponding 2D lines
- What's new: Explicitly representing 3D geometry of cameras and points

Input



Triangulation & camera calibration

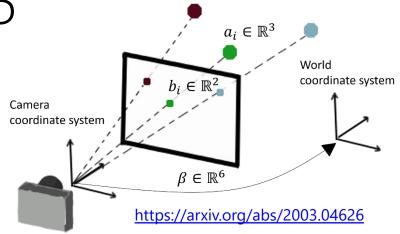
- Suppose we have known camera parameters, each of which observes a point
 - How can we compute the 3D location of that point?
 - This is called *triangulation* (known since ancient times)



- And have matches between these points and an image
- How can we compute the camera parameters?
- This is called *camera calibration* (or *camera*



Liu Hui (c. 263), How to measure the height of a sea island.



Structure from motion

- What if we don't know 3D points or camera parameters?
- SfM solves both of these problems at once
- A kind of chicken-and-egg problem
 - (but solvable)

Photo Tourism

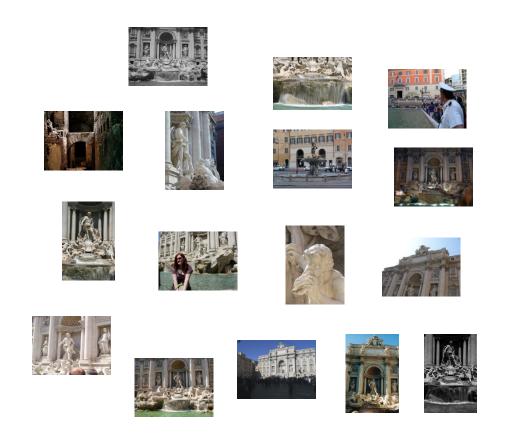


First step: how to get correspondence?

• Feature detection and matching

Feature detection

Detect features using SIFT [Lowe, IJCV 2004]



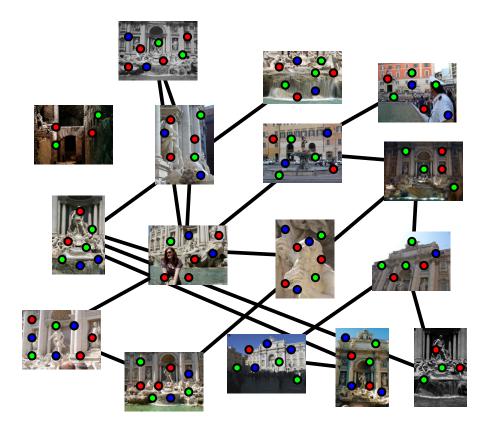
Feature detection

Detect features using SIFT [Lowe, IJCV 2004]



Feature matching

Match features between each pair of images



Feature matching

Refine matching using RANSAC to estimate fundamental matrix between each pair

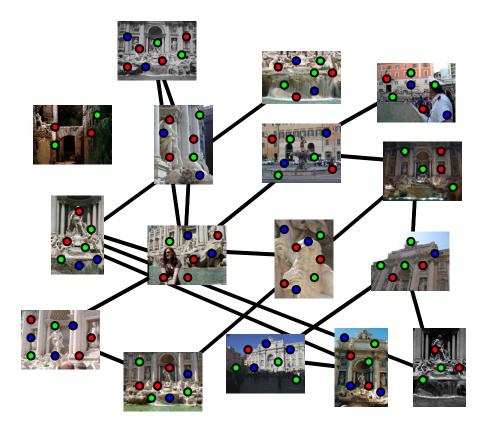
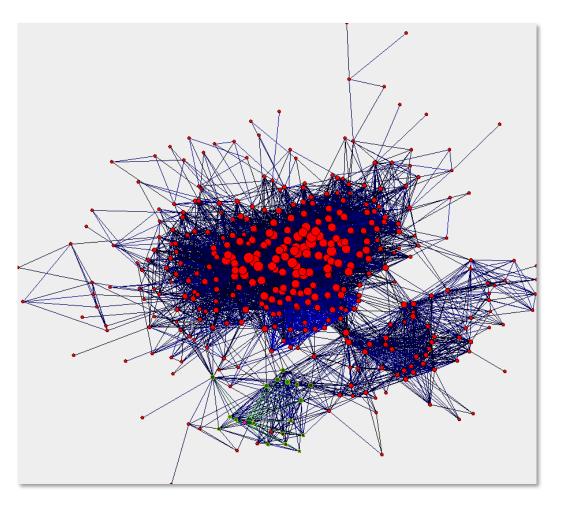


Image connectivity graph

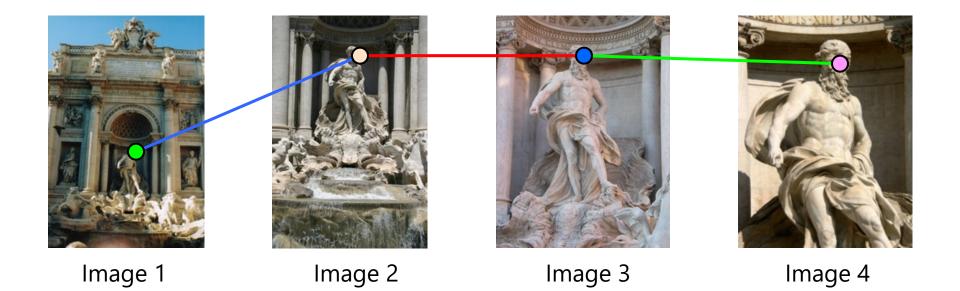


(graph layout produced using the Graphviz toolkit: <u>http://www.graphviz.org/</u>)

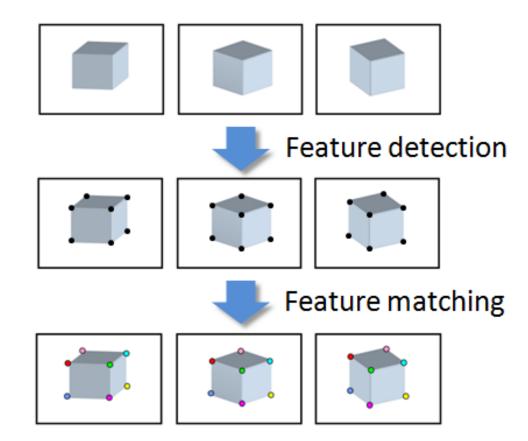


Correspondence estimation

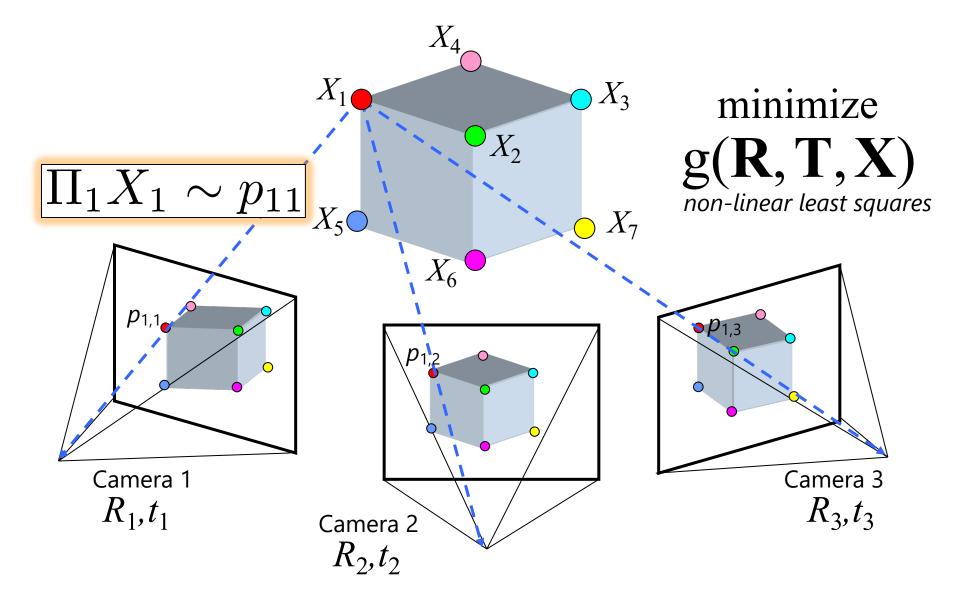
 Link up pairwise matches to form connected components of matches across several images



Input to Structure from Motion



Structure from motion



Problem size

- What are the variables?
 - Cameras and points
- How many variables per camera?
 6 (if calibrated), more if uncalibrated
- How many variables per point?

- 3

- Trevi Fountain collection 466 input photos
 - + > 100,000 3D points
 - = very large optimization problem

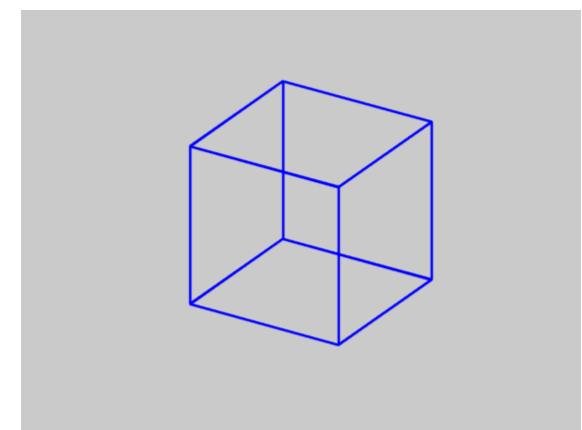
Structure from motion

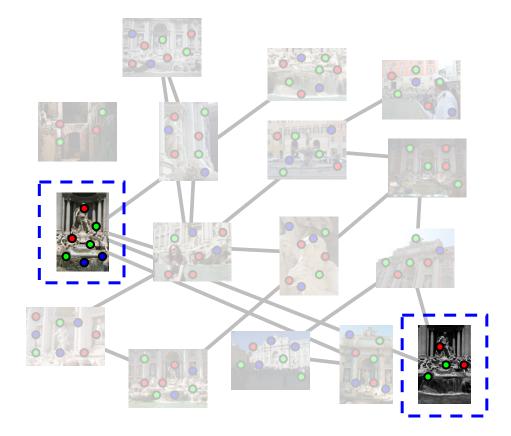
- Minimize sum of squared reprojection errors: $g(\mathbf{X}, \mathbf{R}, \mathbf{T}) = \sum_{i=1}^{m} \sum_{j=1}^{n} w_{ij} \cdot \left\| \mathbf{P}(\mathbf{x}_i, \mathbf{R}_j, \mathbf{t}_j) - \begin{bmatrix} u_{i,j} \\ v_{i,j} \end{bmatrix} \right\|^2$ predicted mage location indicator variable: is point i visible in image j?
- Minimizing this function is called *bundle adjustment*
 - Optimized using non-linear least squares, e.g.
 Levenberg-Marquardt algorithm

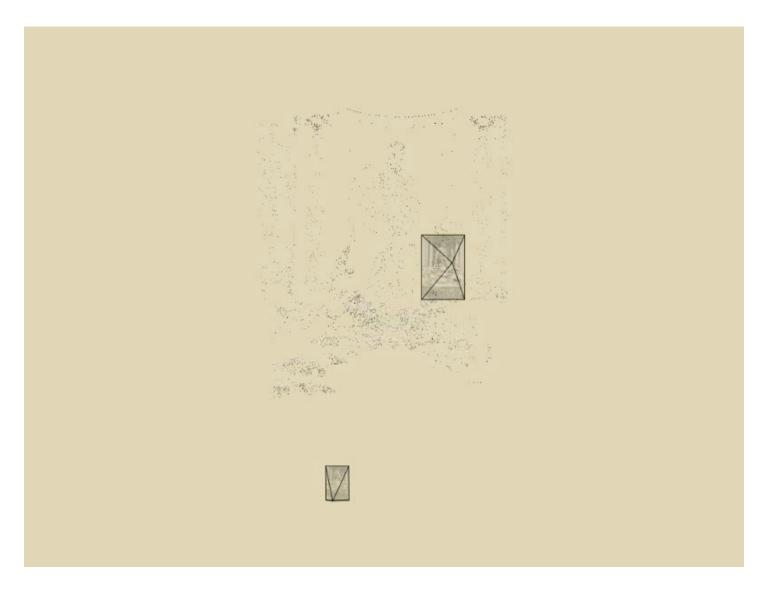
Is SfM always uniquely solvable?

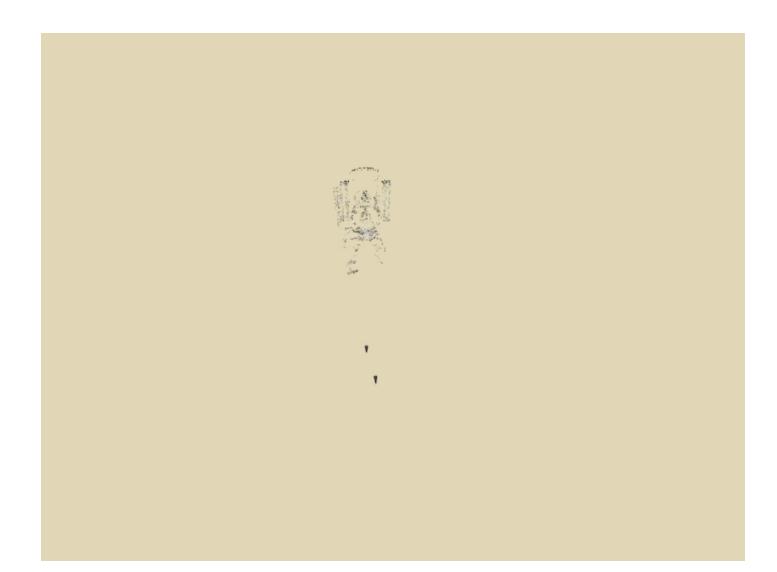
Is SfM always uniquely solvable?

• No...





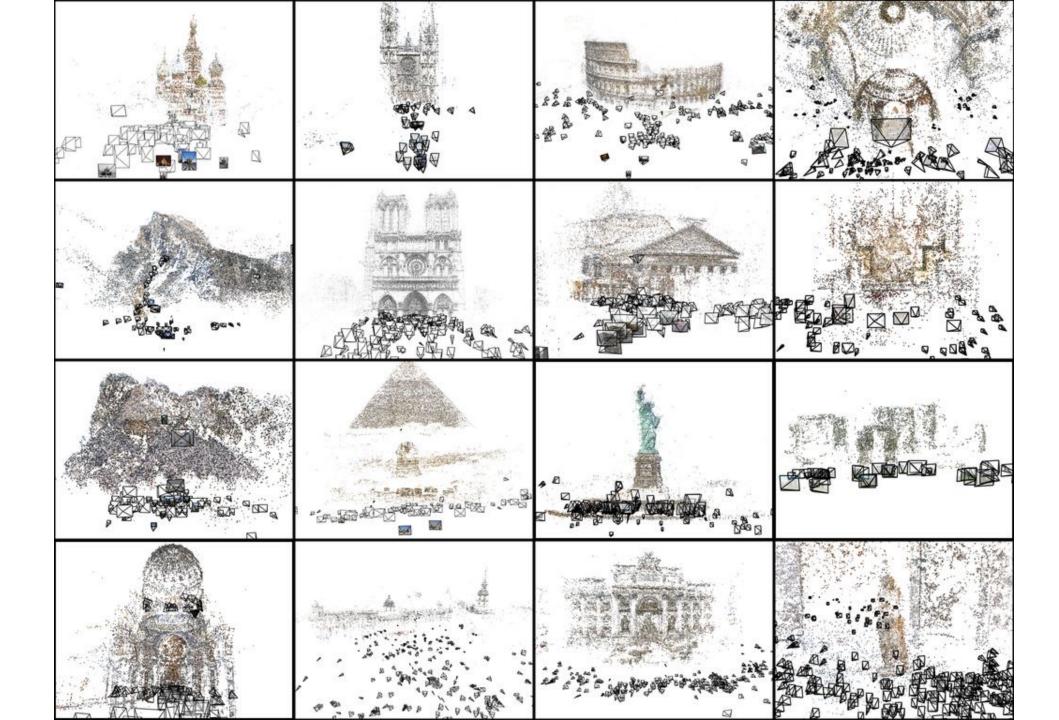




Time-lapse reconstruction of Dubrovnik, Croatia, viewed from above

Photo Tourism







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Libration

From Wikipedia, the free encyclopedia

This article is about astronomical observations. For molecular motion, see Libration (molecule). Not to be confused with liberation, libration, or vibration.

In astronomy, **libration** is a perceived oscillating motion of orbiting bodies relative to each other, notably including the motion of the Moon relative to Earth, or of trojan asteroids relative to planets. Lunar libration is distinct from the slight changes in the Moon's apparent size viewed from Earth. Although this appearance can also be described as an oscillating motion, it is caused by actual changes in the physical distance of the Moon because of its elliptic orbit around Earth. Lunar libration is caused by three phenomena detailed below.

Contents [hide]
1 Lunar libration
2 Trojan libration
3 See also
4 References
5 External links

Lunar libration [edit source]

The Moon keeps one hemisphere of itself facing the Earth, due to tidal locking. Therefore, humans' first view of the far side of the Moon resulted from lunar exploration on October 7, 1959. However, this simple picture is only approximately true: over time, slightly *more* than half (about 59%) of the Moon's surface is seen from Earth due to libration.^[1]

Libration is manifested as a slow rocking back and forth of the Moon as viewed from Earth, permitting an observer to see slightly different halves of the surface at different times.

There are three types of lunar libration:

- *Libration in longitude* results from the eccentricity of the Moon's orbit around Earth; the Moon's rotation sometimes leads and sometimes lags its orbital position.
- Libration in latitude results from a slight inclination (about 6.7 degrees) between the Moon's axis of rotation and the normal

https://en.wikipedia.org/wiki/Libration



The phase and libration of the Moon for 2013 at hourly intervals, with music, titles and supplemental graphics. □



Simulated views of the Moon over one month, demonstrating librations in latitude and longitude. Also visible are

Libration

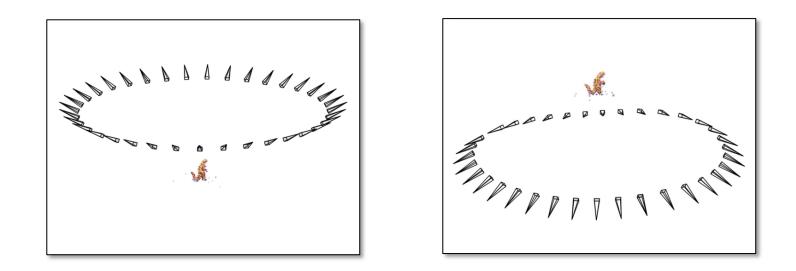


Questions?

SfM – Failure cases

• Necker reversal



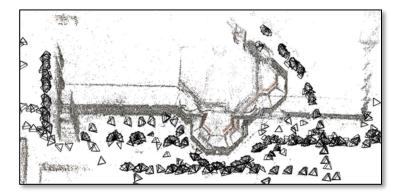


Structure from Motion – Failure cases

• Repetitive structures: Symmetries in man-made scenes









SfM applications

- 3D modeling
- Surveying
- Robot navigation and mapmaking
- Virtual and augmented reality
- Visual effects ("Match moving")
 - <u>https://www.youtube.com/watch?v=RdYWp70P_kY</u>

Applications – Hyperlapse



https://www.youtube.com/watch?v=SOpwHaQnRSY

https://www.youtube.com/watch?v=sA4Za3Hv6ng

Applications: Visual Reality & Augmented Reality

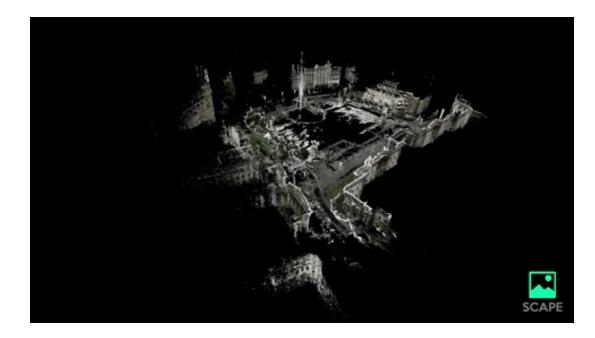


Oculus https://www.youtube.com/watch?v=KOG7yTz1iTA



Hololens https://www.youtube.com/watch?v=FMtvrTGnP04

Applications: Visual Reality & Augmented Reality



Scape: Building the 'AR Cloud': Part Three — 3D Maps, the Digital Scaffolding of the 21st Century

https://medium.com/scape-technologies/building-the-ar-cloud-part-three-3d-maps-thedigital-scaffolding-of-the-21st-century-465fa55782dd

Application: AR walking directions





https://www.theverge.com/2019/8/8/20776247/google-maps-live-view-ar-walkingdirections-ios-android-feature

Questions?