# **CS5670: Computer Vision**

Image Classification



Some Slides from Fei-Fei Li, Justin Johnson, Serena Yeung <u>http://vision.stanford.edu/teaching/cs231n/</u>

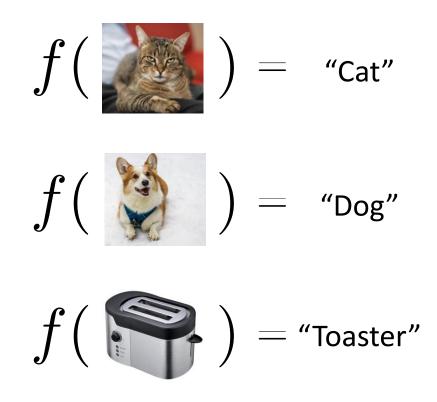
#### References

- Stanford CS231N
  - <u>http://cs231n.stanford.edu/</u>
- Many slides courtesy of Abe Davis

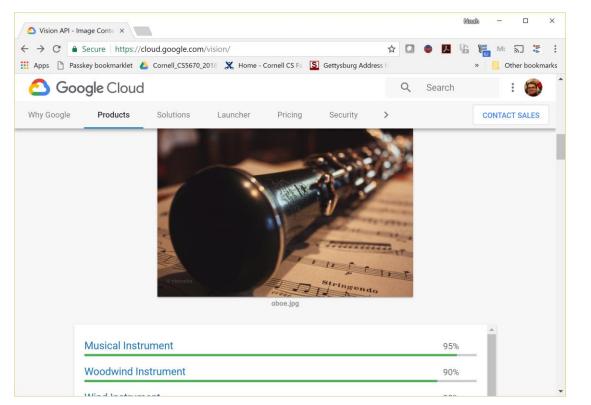
## **Image Classifiers in a Nutshell**

- Input: an image
- Output: the class label for that image
- Label is generally one or more of the discrete labels used in training
  - e.g. {cat, dog, cow, toaster, apple, tomato, truck, ... }

def classifier(image):
 //Do some stuff
 return class\_label;



### Image classification demo



https://cloud.google.com/vision/docs/drag-and-drop

See also:

https://aws.amazon.com/rekognition/

https://www.clarifai.com/

https://azure.microsoft.com/en-us/services/cognitive-services/computer-vision/

• • •

#### **The Semantic Gap**



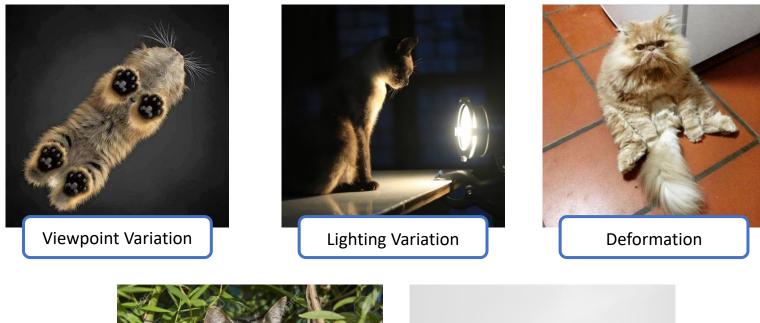
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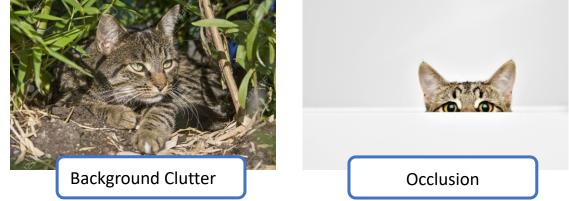
What we see

#### What the computer sees

#### **Variation Makes Recognition Hard**

• The same class of object can appear *very* differently in different images





### The Problem is Under-constrained

- Distinct realities can produce the same image...
- We generally can't compute the "right" answer, but we can compute the most likely one...
- We need some kind of prior to condition on. We can learn this prior from data:

$$f(x) = \underset{\ell_x}{\operatorname{argmax}} P(\ell_x | data)$$

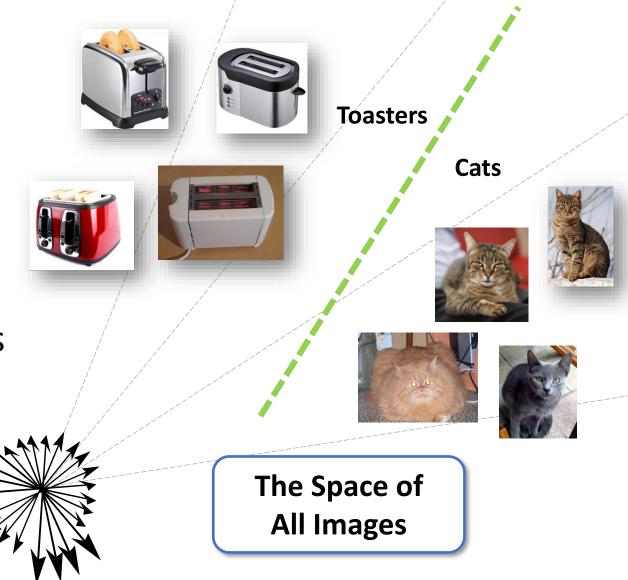




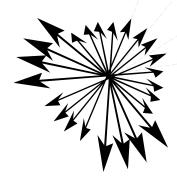
- An image is just a bunch of numbers
- Let's stack them up into a vector
  - Our training data is just a bunch of high-dimensional points now



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- Divide space into different regions for different classes



- An image is just a bunch of numbers
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The Space of All Images

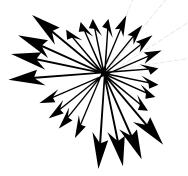
**TOASTER CAT** 

YOUR ARGUMENT IS INVALID

- An image is just a bunch of numbers
- Let's stack them up into a vector
  - Our training data is just a bunch of high-dimensional points now
- Divide space into different regions for different classes

#### or

• Define a distribution over space for each class



**Toasters** 

#### The Space of All Images

Cats

### Image Features and Dimensionality Reduction

- How high-dimensional is an image?
  - Let's consider an iPhone X photo:
    - 4032 x 3024 pixels
    - Every pixel has 3 colors
    - 36,578,304 pixels (36.5 Mega pixels)
- In practice, images sit on a lowerdimensional manifold
- Think of image features and dimensionality reduction as ways to represent images by their location on such manifolds

The Space of All Images

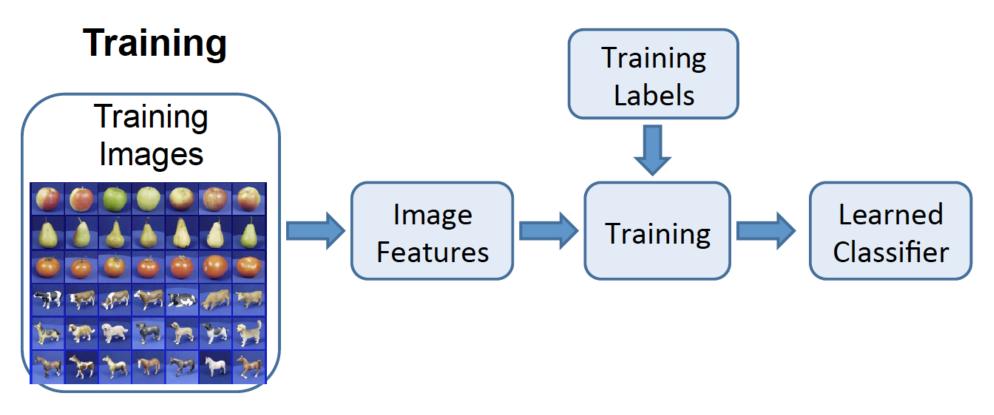
## **Training & Testing a Classifier**

- Collect a database of images with labels
- Use ML to train an image classifier
- Evaluate the classifier on test images

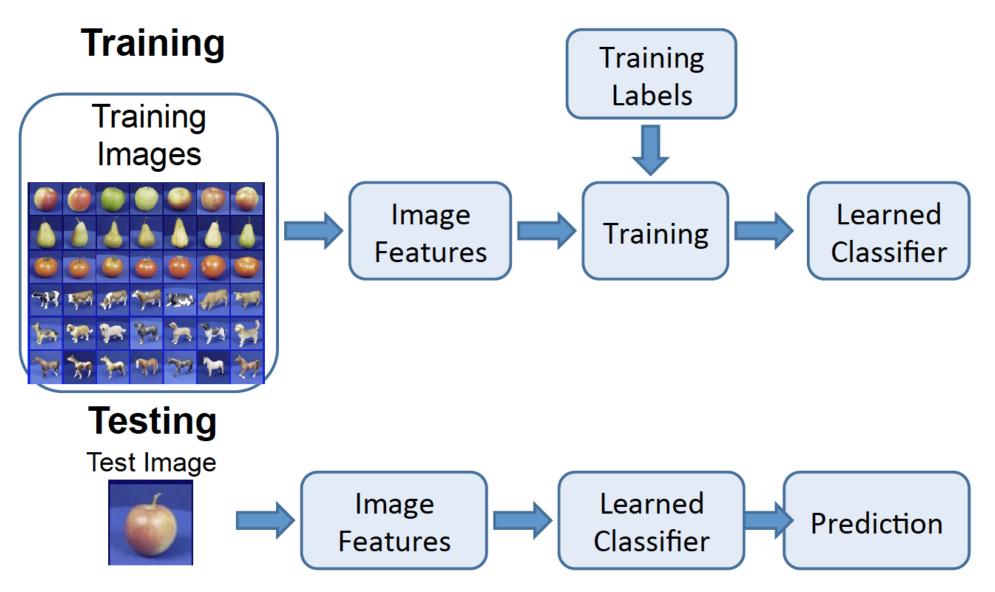
catdogmughatImage: Second second

Example training set

#### **Training & Testing a Classifier**



#### **Training & Testing a Classifier**



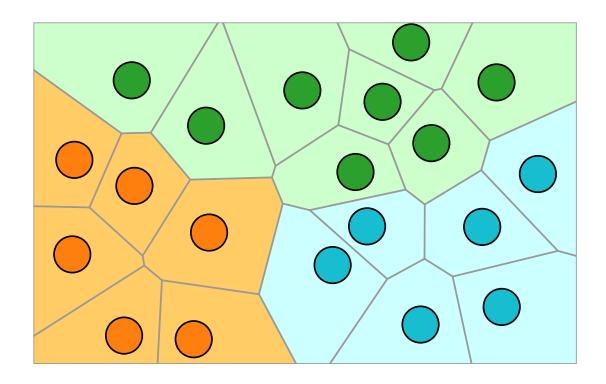
### Classifiers

- Nearest Neighbor
- kNN ("k-Nearest Neighbors")
- Linear Classifier
- Neural Network
- Deep Neural Network
- ...

#### First: Nearest Neighbor (NN) Classifier

#### • Train

- Remember all training images and their labels
- Predict
  - Find the closest (most similar) training image
  - Predict its label as the true label



#### **CIFAR-10 and NN results**

Example dataset: CIFAR-10 10 labels 50,000 training images 10,000 test images.

airplane	🛁 🔤 🐖 🛩 📼 🔤 🔐
automobile	🚍 🚭 🏹 🍋 🚾 🕍 🚟 🐝
bird	Se 🗾 🖉 🐒 🕾 Se
cat	li 🖉 📚 🔤 🎉 🚵 📚 🗾 😻 📝
deer	NG 😪 😭 🥐 🦉 🧊 😭 😪
dog	1971 📶 🔊 🔊 🙈 💓 🔊 💥 🎊
frog	NY 100 100 100 100 100 100 100 100 100 10
horse	
ship	🗃 🚵 💒 👞 🕍 🗫 💋 🖉 🚈
truck	i i i i i i i i i i i i i i i i i i i

#### **CIFAR-10 and NN results**

#### Example dataset: CIFAR-10 10 labels 50,000 training images 10,000 test images.

airplane	🚟 📉 🐖 🛩 🖛 🌌 🔐 🛶
automobile	an a
bird	Re 🗾 💋 📢 🛵 🔨 🦻 🔯 💆
cat	in in in in it in
deer	
dog	1976 🔊 🔊 🔊 🙈 🖉 🕥 🔊
frog	
horse	
ship	🗃 🌌 💒 🛋 🚅 💋 🖉 💆 🙇
truck	V THE SECTION OF SECTI

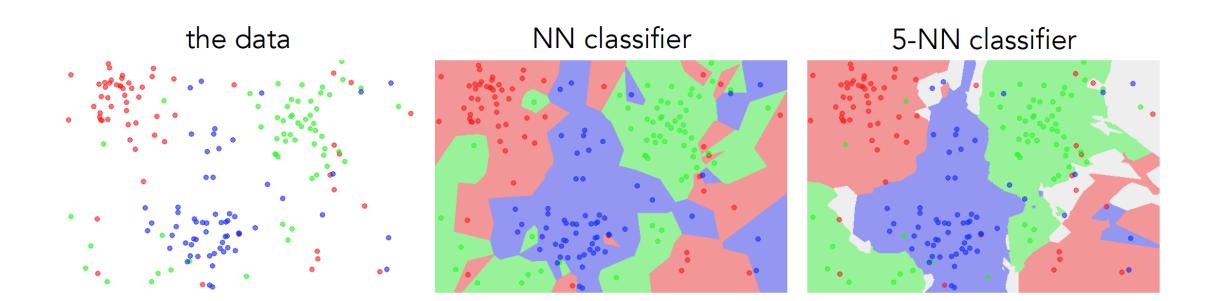
#### For every test image (first column), examples of nearest neighbors in rows



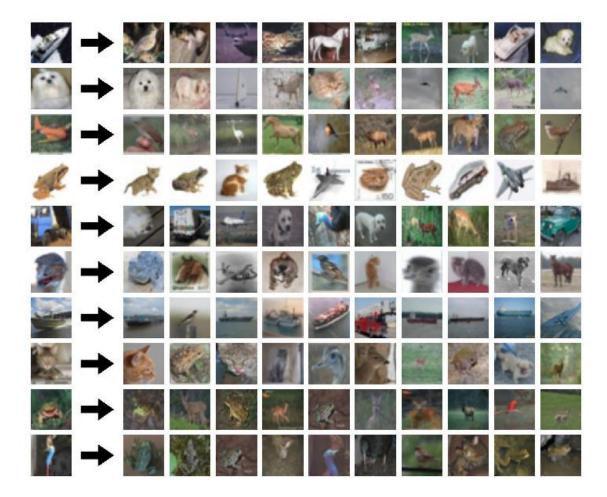
Slides from Andrej Karpathy and Fei-Fei Li http://vision.stanford.edu/teaching/cs231n/

#### k-nearest neighbor

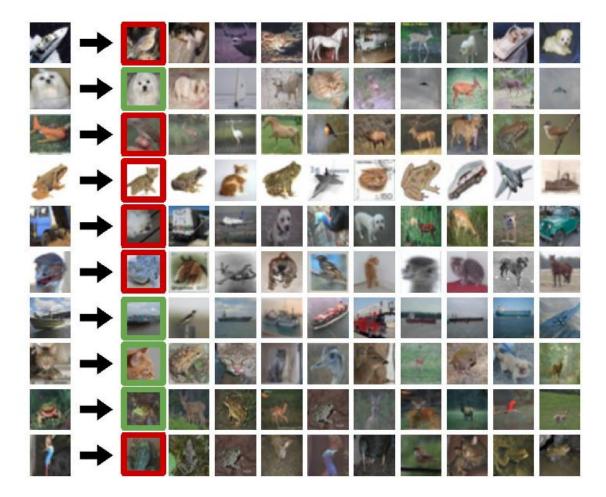
- Find the k closest points from training data
- Take majority vote from K closest points



What does this look like?



#### What does this look like?



#### How to Define Distance Between Images

L1 distance:

$$d_1(I_1,I_2) = \sum_p |I_1^p - I_2^p|$$

Where  $I_1$  denotes image 1, and p denotes each pixel

	test image					
ł	56	10	18			
	90	23	128	133		
2	24	26	178	200		
	2	0	255	220		

4 - - 4 \*----

training image 

pixel-wise absolute value differences

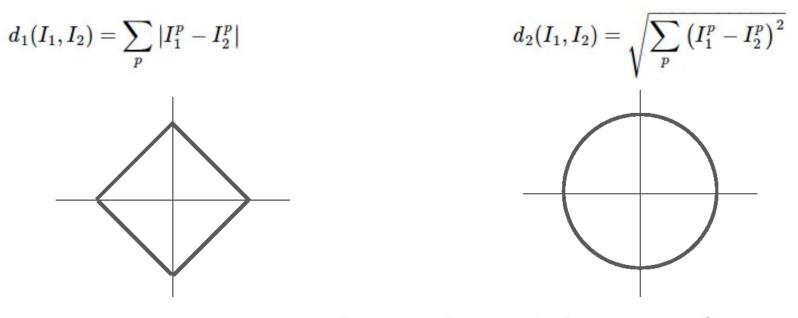
46	12	14	1	
82	13	39	33	450
12	10	0	30	→ 456
2	32	22	108	

### **Choice of distance metric**

• Hyperparameter

L1 (Manhattan) distance

L2 (Euclidean) distance

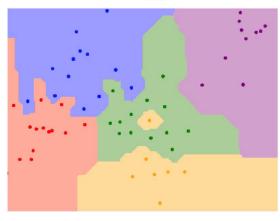


- Two most commonly used special cases of p-norm $\|x\|_p = \left(|x_1|^p + \dots + |x_n|^p\right)^{\frac{1}{p}} \quad p \ge 1, x \in \mathbb{R}^n$ 

K-Nearest Neighbors: Distance Metric

L1 (Manhattan) distance

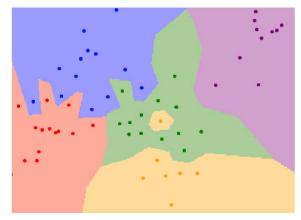
 $d_1(I_1,I_2) = \sum_p |I_1^p - I_2^p|$ 



K = 1

L2 (Euclidean) distance

$$d_2(I_1,I_2) = \sqrt{\sum_p \left(I_1^p - I_2^p
ight)^2}$$



K = 1

Demo: http://vision.stanford.edu/teaching/cs231n-demos/knn/

### Hyperparameters

- What is the **best distance** to use?
- What is the **best value of k** to use?
- These are hyperparameters: choices about the algorithm that we set rather than learn
- How do we set them?
  - One option: try them all and see what works best

Idea #1: Choose hyperparameters that work best on the data

Your Dataset

Idea #1: Choose hyperparameters that work best on the data

**BAD**: K = 1 always works perfectly on training data

Your Dataset

Idea #1: Choose hyperparameters that work best on the data

**BAD**: K = 1 always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, choose hyperparameters that work best on test data

train test
------------

Idea #1: Choose hyperparameters that work best on the data

**BAD**: K = 1 always works perfectly on training data

Your Dataset		
Idea #2: Split data into <b>train</b> and <b>test</b> , choose hyperparameters that work best on test data	idea how algo rm on new dat	
train	test	

Idea #1: Choose hyperparameters that work best on the data

**BAD**: K = 1 always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, chooseBAD: No idea how algorithmhyperparameters that work best on test datawill perform on new data

train test

Idea #3: Split data into train, val, and test; choose	Better!
hyperparameters on val and evaluate on test	Better

train	validation	test
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Your Dataset

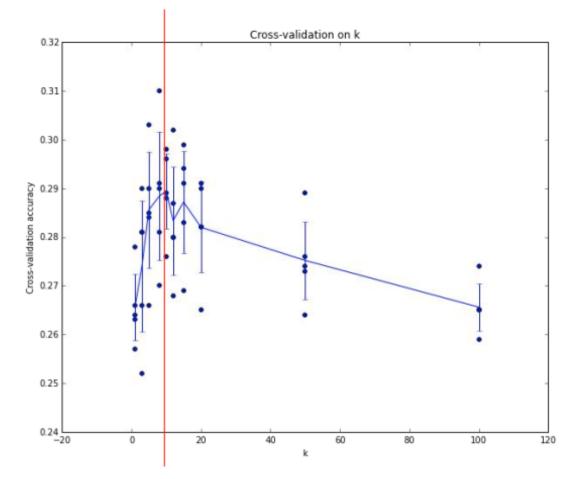
#### Idea #4: Cross-Validation: Split data into folds,

try each fold as validation and average the results

fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test

Useful for small datasets, but not used too frequently in deep learning

### **Hyperparameter Tuning**



Example of 5-fold cross-validation for the value of **k**.

Each point: single outcome.

The line goes through the mean, bars indicated standard deviation

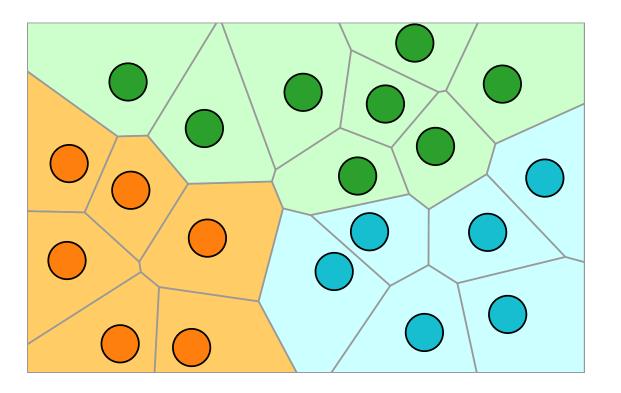
(Seems that k ~= 7 works best for this data)

### **Recap: How to pick hyperparameters?**

- Methodology
  - Train and test
  - Train, validate, test
- Train for original model
- Validate to find hyperparameters
- Test to understand generalizability

### kNN -- Complexity and Storage

- N training images, M test images
- Training: O(1)
- Testing: O(MN)
- We often need the opposite:
  - Slow training is ok
  - Fast testing is necessary

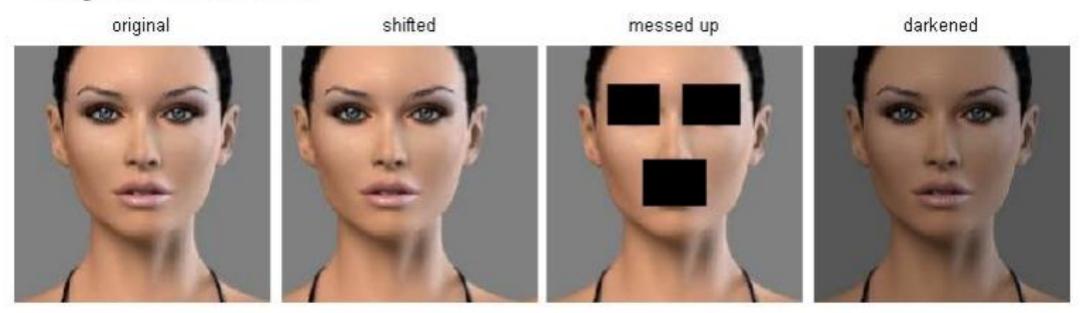


#### k-Nearest Neighbors: Summary

- In image classification we start with a training set of images and labels, and must predict labels on the test set
- The **K-Nearest Neighbors** classifier predicts labels based on nearest training examples
- Distance metric and K are **hyperparameters**
- Choose hyperparameters using the validation set; only run on the test set once at the very end!

## **Problems with KNN: Distance Metrics**

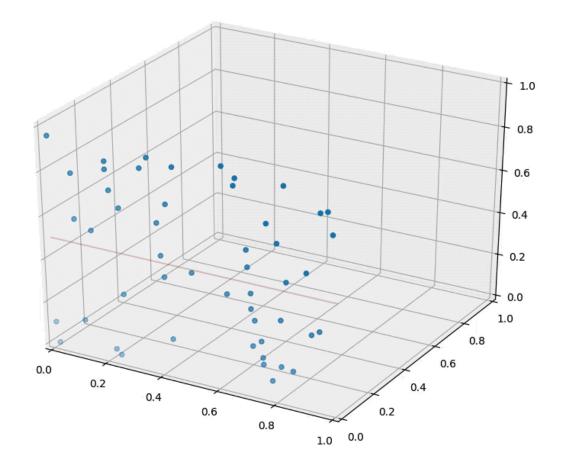
- terrible performance at test time
- distance metrics on level of whole images can be very unintuitive



(all 3 images have same L2 distance to the one on the left)

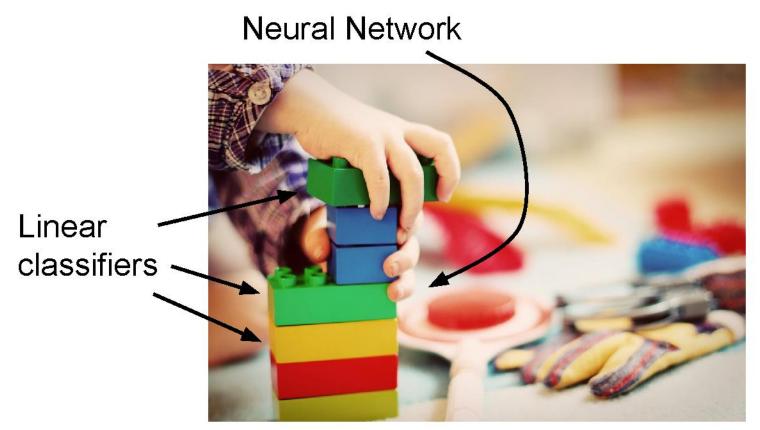
## **Problems with KNN: The Curse of Dimensionality**

- As the number of dimensions increases, the same amount of data becomes more sparse.
- Amount of data we need ends up being exponential in the number of dimensions



Animation from https://www.cs.cornell.edu/courses/cs4780/2018fa/lectures/lecturenote02\_kNN.html

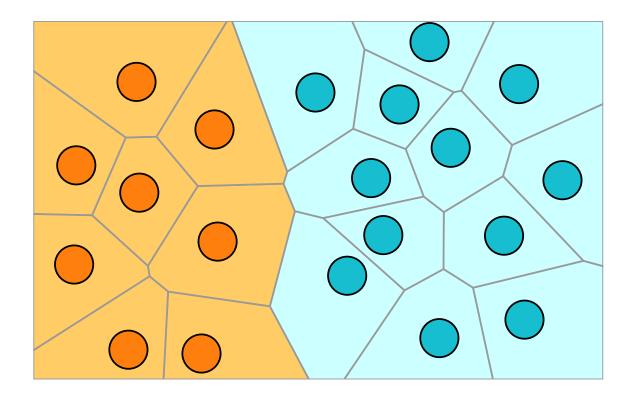
## **Linear Classifiers**



This image is <u>CC0 1.0</u> public domain

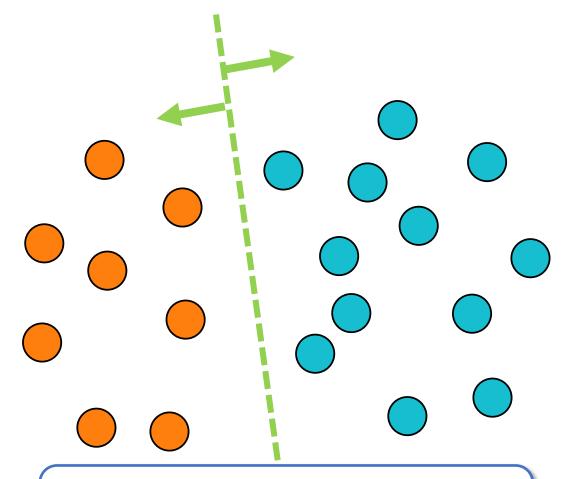
## Linear Classification vs. Nearest Neighbors

- Nearest Neighbors
  - Store every image
  - Find nearest neighbors at test time, and assign same class



# Linear Classification vs. Nearest Neighbors

- Nearest Neighbors
  - Store every image
  - Find nearest neighbors at test time, and assign same class
- Linear Classifier
  - Store hyperplanes that best separate different classes
  - We can compute continuous class score by calculating (signed) distance from hyperplane



We can interpret this as a linear "score function" for each class.

## **Score functions**



#### class scores

Slide adapted from Andrej Karpathy and Fei-Fei Li http://vision.stanford.edu/teaching/cs231n/

## **Parametric Approach**

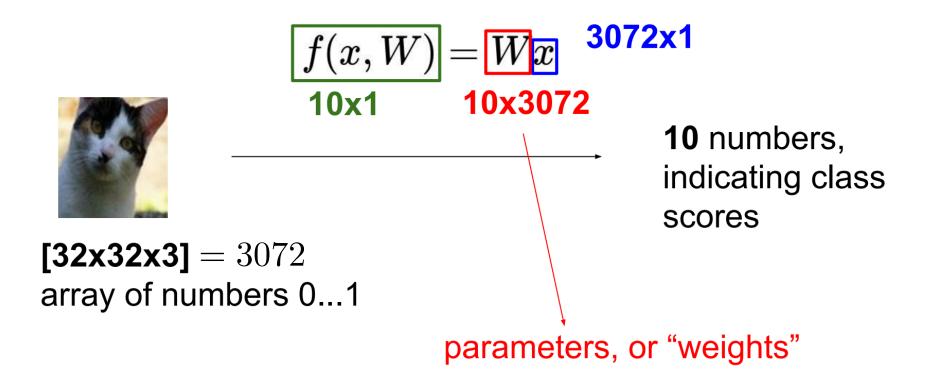


image parameters f(x,W)

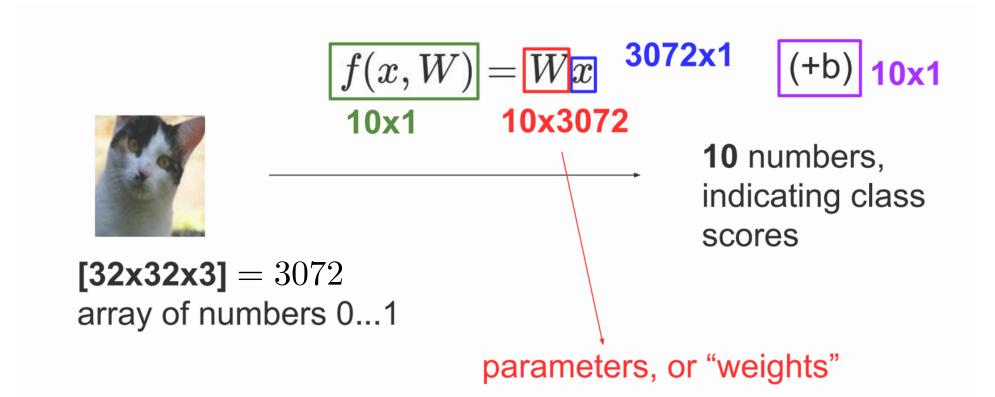
**10** numbers, indicating class scores

[32x32x3] = 3072array of numbers 0...1 (3072 numbers total)

## **Parametric Approach: Linear Classifier**

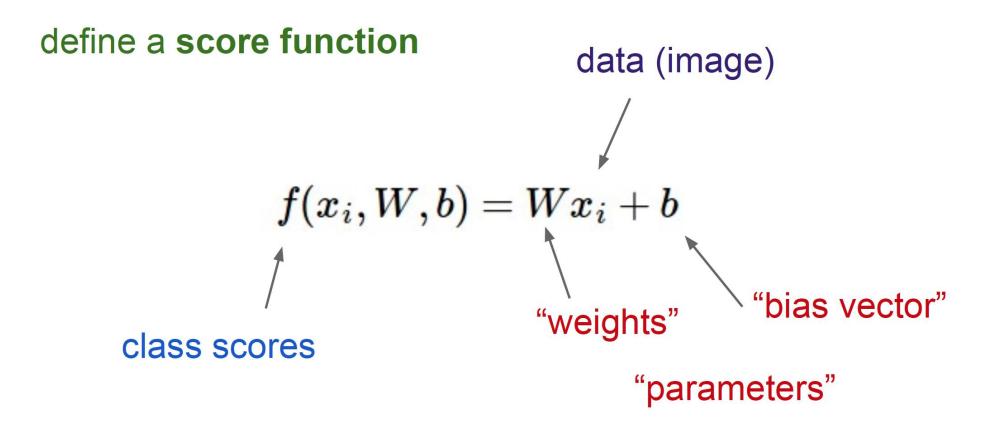


## **Parametric Approach: Linear Classifier**



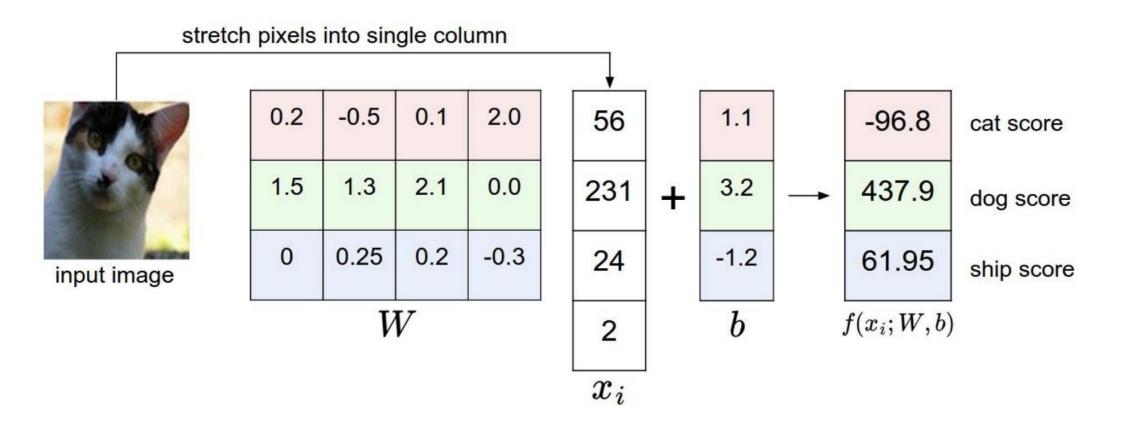
Slide adapted from Andrej Karpathy and Fei-Fei Li http://vision.stanford.edu/teaching/cs231n/

## **Linear Classifier**



## **Interpretation: Algebraic**

Example with an image with 4 pixels, and 3 classes (cat/dog/ship)

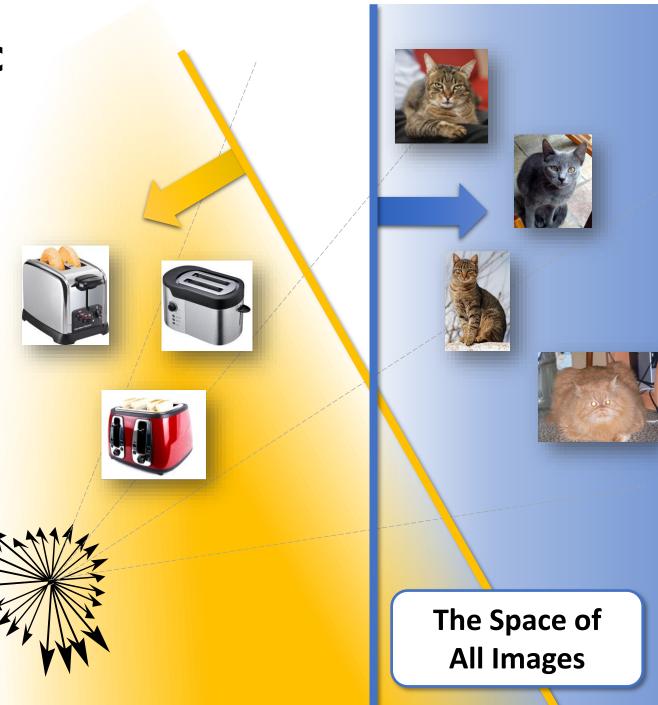


# **Interpretation: Geometric**

• Parameters define a hyperplane for each class:

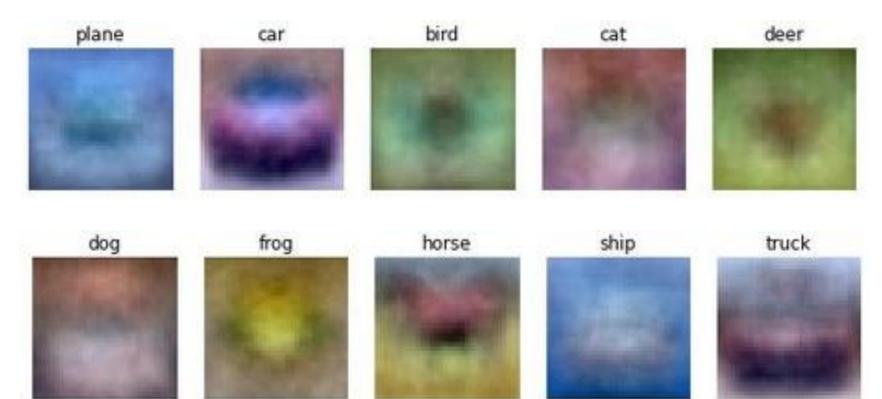
$$f(x_i, W, b) = Wx_i + b$$

• We can think of each class score as defining a distribution that is proportional to distance from the corresponding hyperplane



## **Interpretation: Template matching**

ullet We can think of the rows in  $\,W\,$  as templates for each class



Rows of W in  $f(x_i, W, b) = Wx_i + b$ 

# Hard Cases for a Linear Classifier

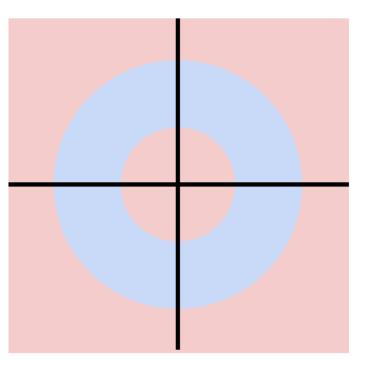
#### Class 1:

First and third quadrants

#### Class 2: Second and fourth quadrants

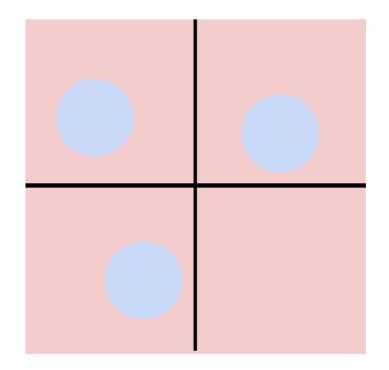
Class 1: 1 <= L2 norm <= 2

Class 2: Everything else



Class 1: Three modes

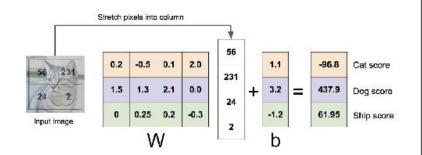
#### Class 2: Everything else



#### Linear Classifier: Three Viewpoints

f(x,W) = Wx

Algebraic Viewpoint

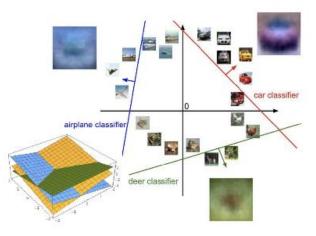


<u>Visual Viewpoint</u> One template per class



Hyperplanes cutting up space

**Geometric Viewpoint** 



#### **So far**: Defined a (linear) <u>score function</u> f(x,W) = Wx + b

Example class scores for 3 images for some W:

How can we tell whether this W is good or bad?

<u>Cat image by Nikita</u> is licensed under <u>CC-BY 2.0</u> <u>Car image</u> is <u>CCO 1.0</u> public domain <u>Frod image</u> is in the public domain



airplane	-3.45	-0.51	3.42
automobile	-8.87	6.04	4.64
bird	0.09	5.31	2.65
cat	2.9	-4.22	5.1
deer	4.48	-4.19	2.64
dog	8.02	3.58	5.55
frog	3.78	4.49	-4.34
horse	1.06	-4.37	-1.5
ship	-0.36	-2.09	-4.79
truck	-0.72	-2.93	6.14

## Recap

- Learning methods
  - k-Nearest Neighbors
  - Linear classification
- Classifier outputs a **score function** giving a score to each class
- How do we define how good a classifier is based on the training data? (Spoiler: define a *loss function*)

## **Linear classification**



airplane	-3.45	-0.51	3.42
automobile	-8.87	6.04	4.64
bird	0.09	5.31	2.65
cat	2.9	-4.22	5.1
deer	4.48	-4.19	2.64
dog	8.02	3.58	5.55
frog	3.78	4.49	-4.34
horse	1.06	-4.37	-1.5
ship	-0.36	-2.09	-4.79
truck	-0.72	-2.93	6.14

Cat image by Nikita is licensed under CC-BY 2.0; Car image is CC0 1.0 public domain; Frog image is in the public domain

#### Output scores

#### TODO:

- Define a loss function that quantifies our unhappiness with the scores across the training data.
- 2. Come up with a way of efficiently finding the parameters that minimize the loss function.
  (optimization)

## **Loss functions**

cat

car

frog

Suppose: 3 training examples, 3 classes. With some W the scores f(x, W) = Wx are:

5.1

-1.7



4.9

2.0

2.5

-3.1

A loss function tells how good our current classifier is

Given a dataset of examples  $\{(x_i, y_i)\}_{i=1}^N$ 

Where  $oldsymbol{x_i}$  is image and  $oldsymbol{y_i}$  is (integer) label

Loss over the dataset is a sum of loss over examples:

$$L = \frac{1}{N} \sum_{i} L_i(f(x_i, W), y_i)$$

## Loss function, cost/objective function

- Given ground truth labels  $(y_i)$ , scores  $f(x_i, \mathbf{W})$ 
  - how unhappy are we with the scores?
- Loss function or objective/cost function measures unhappiness
- During training, want to find the parameters W that minimize the loss function

## Simpler example: binary classification

- Two classes (e.g., "cat" and "not cat")
  - AKA "positive" and "negative" classes



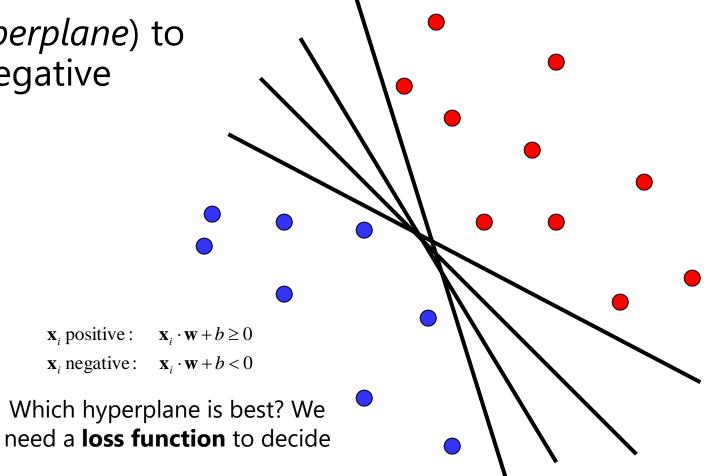




not cat

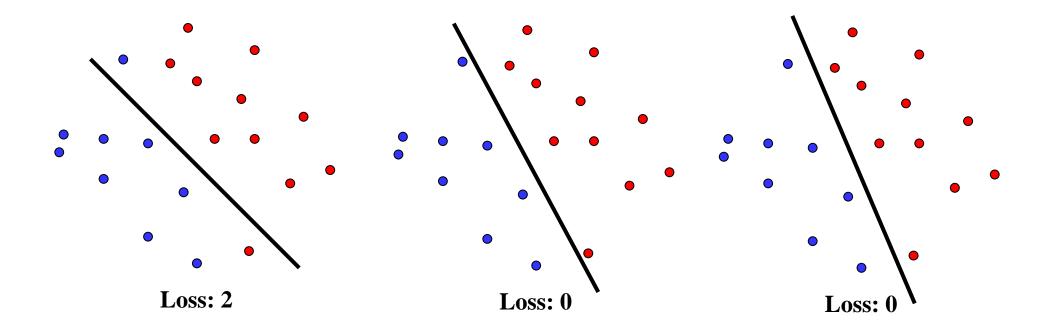
## **Linear classifiers**

• Find linear function (*hyperplane*) to separate positive and negative examples



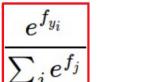
# What is a good loss function?

- One possibility: Number of misclassified examples
  - Problems: discrete, can't break ties
  - We want the loss to lead to good generalization
  - We want the loss to work for more than 2 classes



## **Softmax classifier**

 Interpret Scores as unnormalized log probabilities of classes  $f(x_i, W) = Wx_i$  (score function)



softmax function

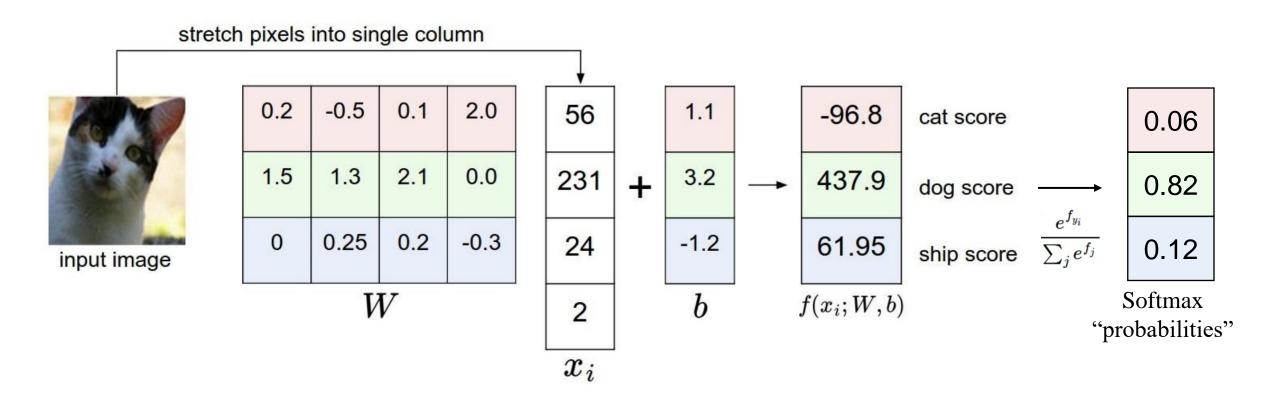
Squashes values into *probabilities* ranging from 0 to 1

 $P(y_i \mid x_i; W)$ 

Example with three classes:  $[1,-2,0] \rightarrow [e^1, e^{-2}, e^0] = [2.71, 0.14, 1] \rightarrow [0.7, 0.04, 0.26]$ 

## **Softmax classifier**

Example with an image with 4 pixels, and 3 classes (cat/dog/ship)

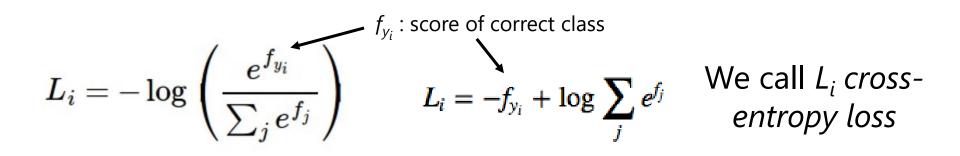


## **Cross-entropy loss**

 $f(x_i, W) = Wx_i$  (score function)

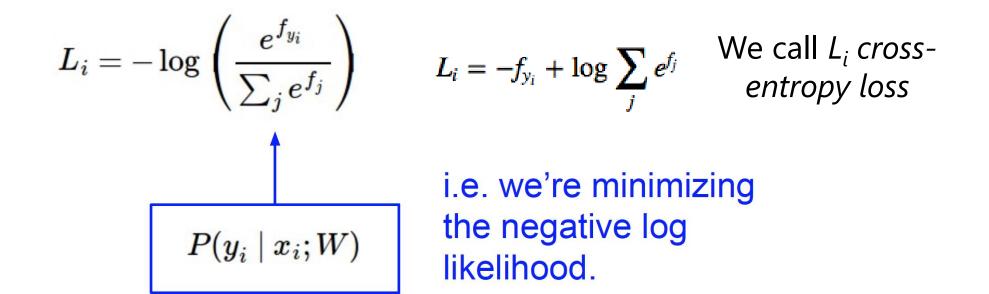
#### **Cross-entropy loss**

 $f(x_i, W) = W x_i$  (score function)



#### **Cross-entropy loss**

 $f(x_i, W) = W x_i$  (score function)



#### Losses

- Cross-entropy loss is just one possible loss function
  - One nice property is that it reinterprets scores as probabilities, which have a natural meaning
- SVM (max-margin) loss functions also used to be popular
  - But currently, cross-entropy is the most common classification loss

# Summary

- Have score function and loss function
  - Currently, score function is based on linear classifier
  - Next, will generalize to convolutional neural networks
- Find W and b to minimize loss

$$L = \frac{1}{N} \sum_{i} -\log\left(\frac{e^{f_{y_i}}}{\sum_{j} e^{f_j}}\right) + \lambda \sum_{k} \sum_{l} W_{k,l}^2$$
  
Average of cross-entropy loss  
over all training examples

#### **Questions?**