

# CS5670: Computer Vision

## Panoramas



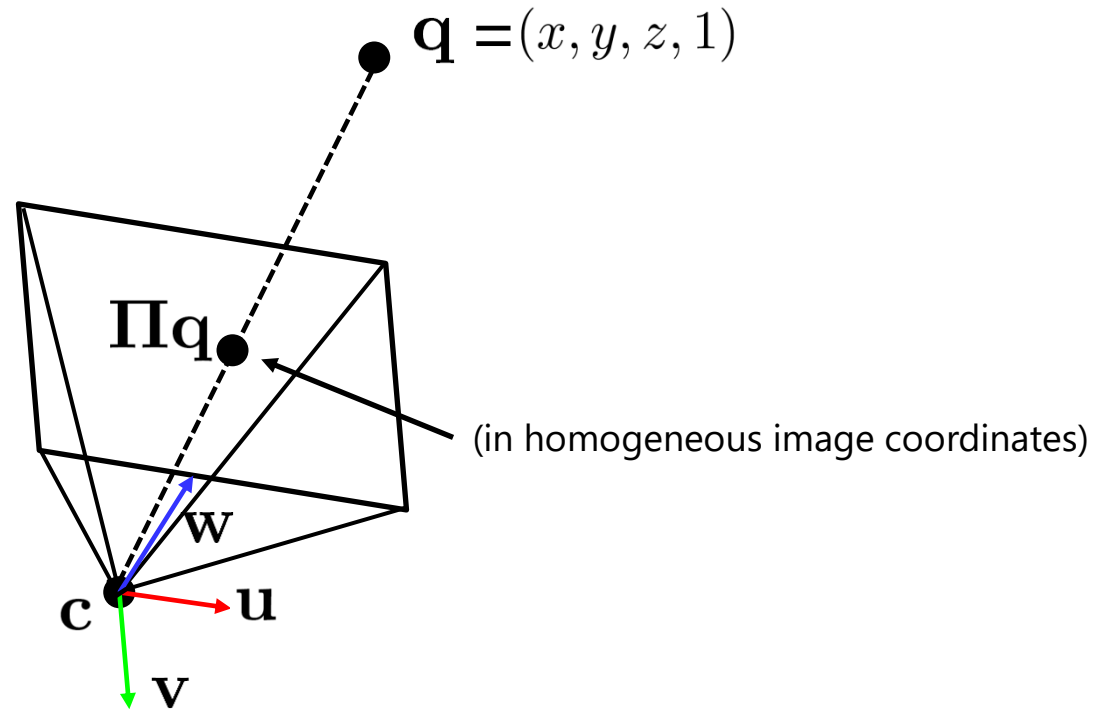
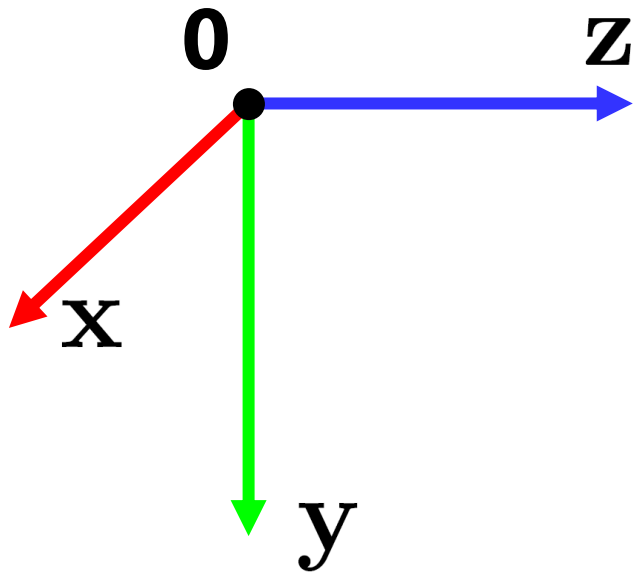
[Space Shuttle Discovery Flight Deck, Gigapan](#)

# Announcements

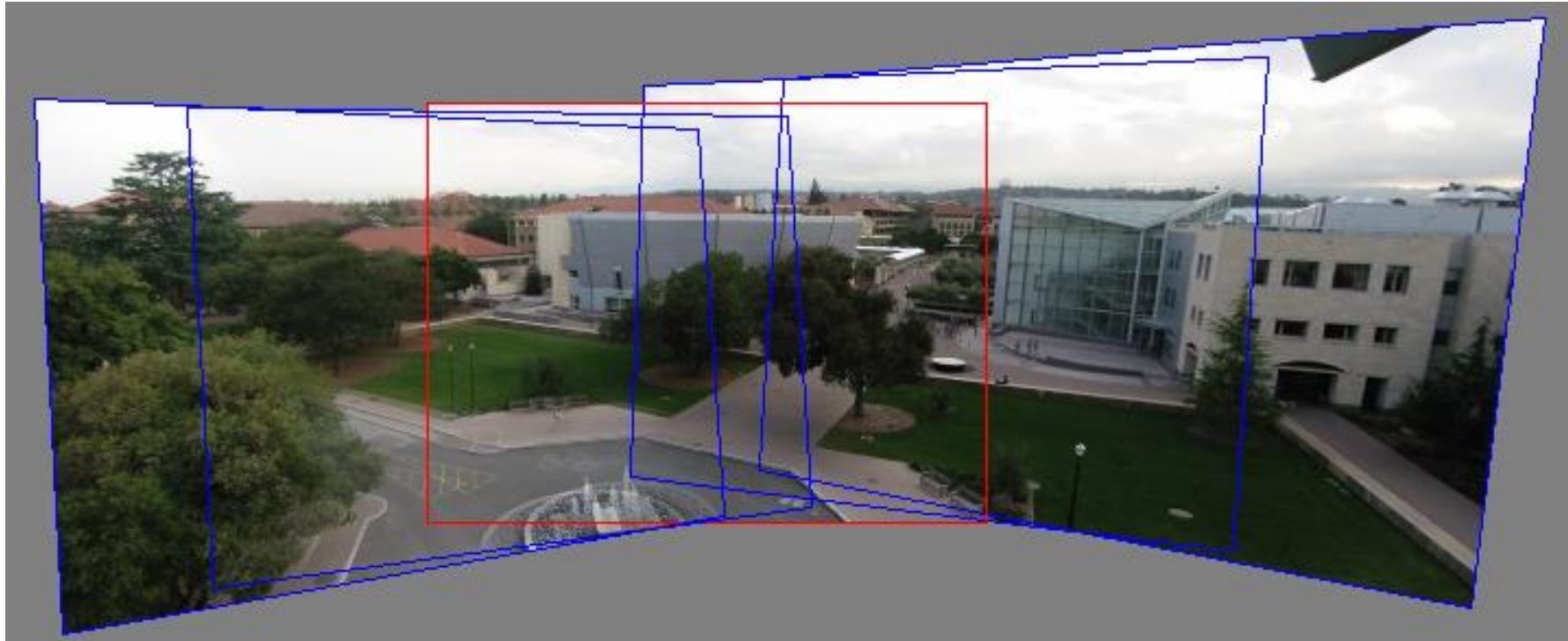
- Midterm exam due by the start of class today
- Project 3: Autostitch (Panorama Stitching)
  - Released today, March 8
  - Due on Friday, March 18, by 7pm
  - To be done in groups of 2
  - If you need help finding a team member, let me know
- No quiz on Thursday

# **Project 3 Demo [Zekun]**

# From last time: Projection matrix

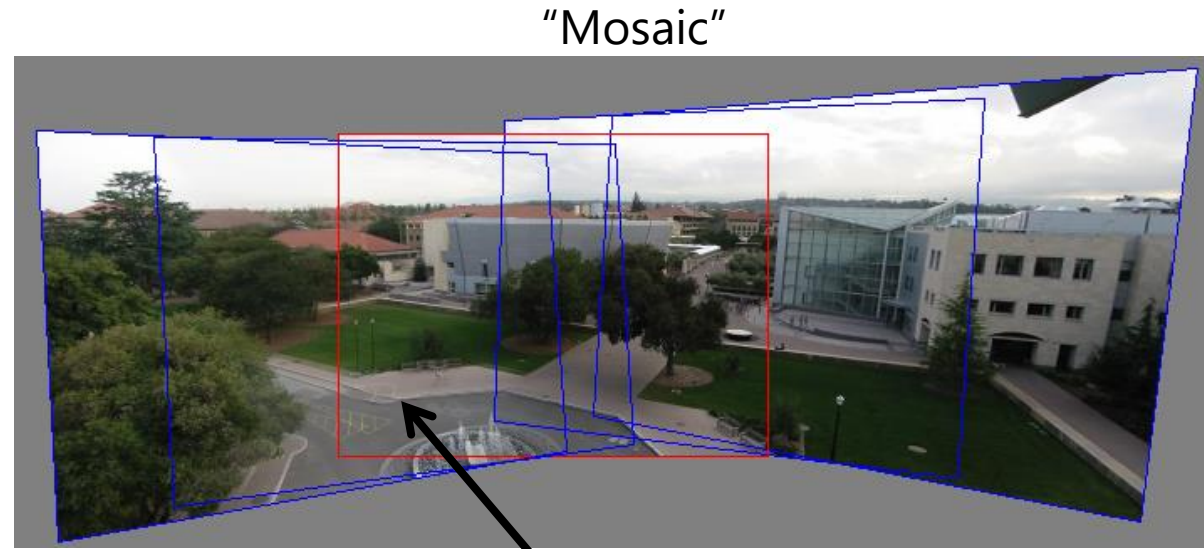
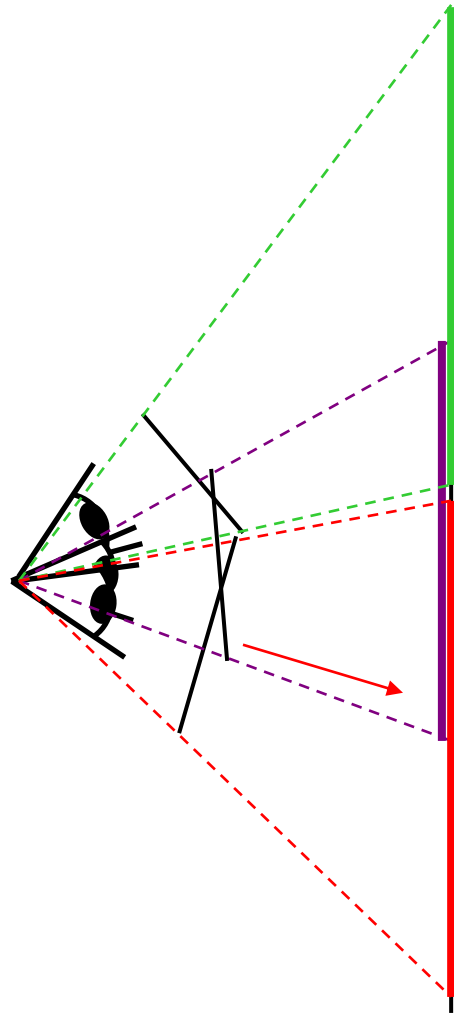


# Back to panoramas



Can we use homographies to create a 360 degree panorama?

# Idea: project images onto a common plane



each image is warped  
with a homography  $\mathbf{H}$

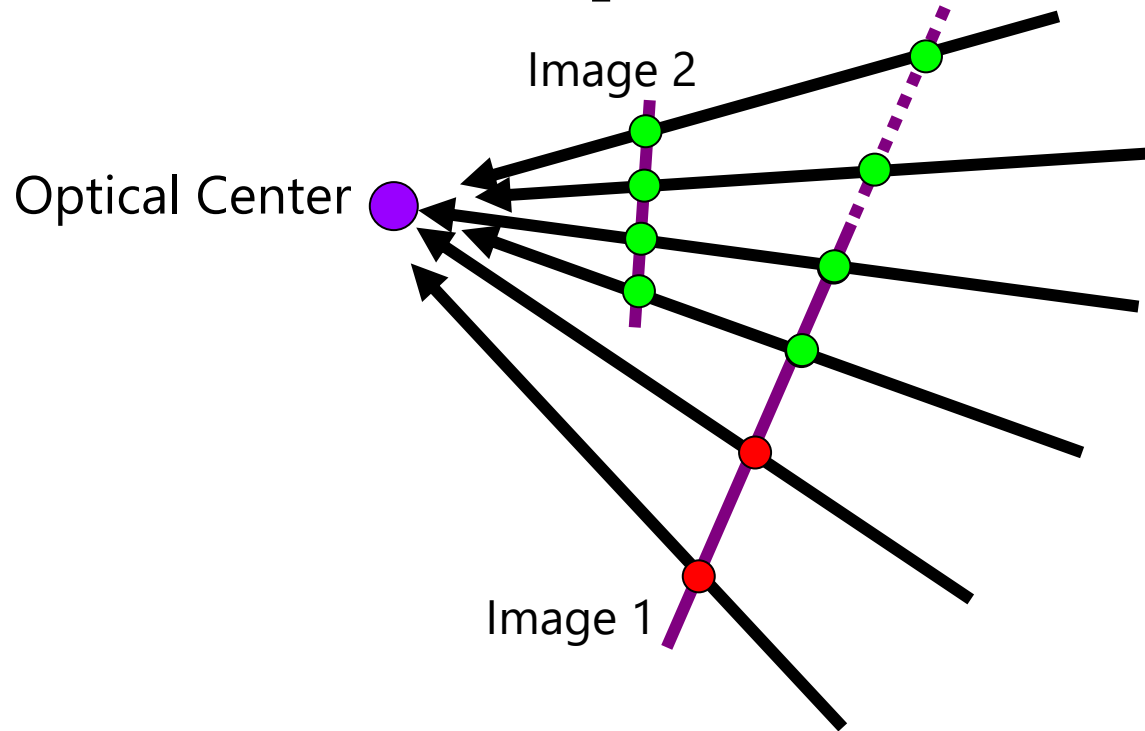
We'll see what this homography means next  
Can't create a 360 panorama this way... we'll fix this shortly

mosaic projection plane

# Creating a panorama

- Basic Procedure
  - Take a sequence of images from the same position
    - Rotate the camera about its optical center
  - Compute transformation between second image and first
  - Transform the second image to overlap with the first
  - Blend the two together to create a mosaic
  - If there are more images, repeat

# Geometric interpretation of mosaics

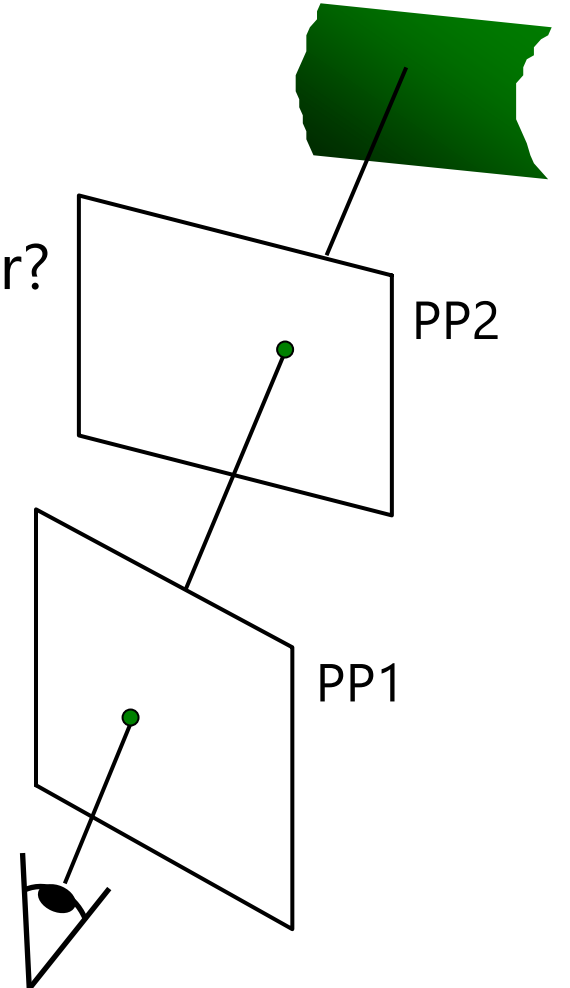


- If we capture all  $360^\circ$  of rays, we can create a  $360^\circ$  panorama
- The basic operation is *projecting* an image from one plane to another
- The projective transformation is scene-INDEPENDENT

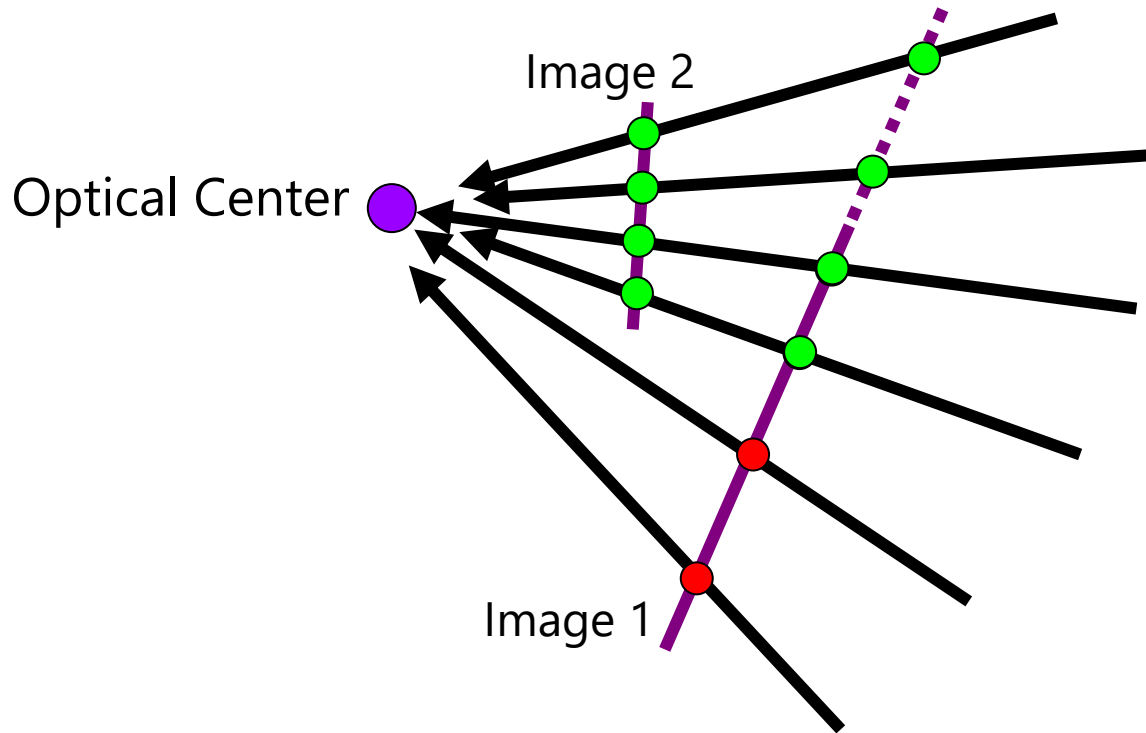


# Image reprojection

- Basic question
  - How to relate two images from the same camera center?
    - how to map a pixel from PP1 to PP2
- Answer
  - Cast a ray through each pixel in PP1
  - Draw the pixel where that ray intersects PP2



# What is the transformation?



**Step 1:** Convert pixels in image 2 to rays in camera 2's coordinate system.

$$\begin{bmatrix} X_2 \\ Y_2 \\ Z_2 \end{bmatrix} = \mathbf{K}_2^{-1} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$

**Step 2:** Convert rays in camera 2's coordinates to rays in camera 1's coordinates.

$$\begin{bmatrix} X_1 \\ Y_1 \\ Z_1 \end{bmatrix} = \mathbf{R}_2^T \mathbf{K}_2^{-1} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$

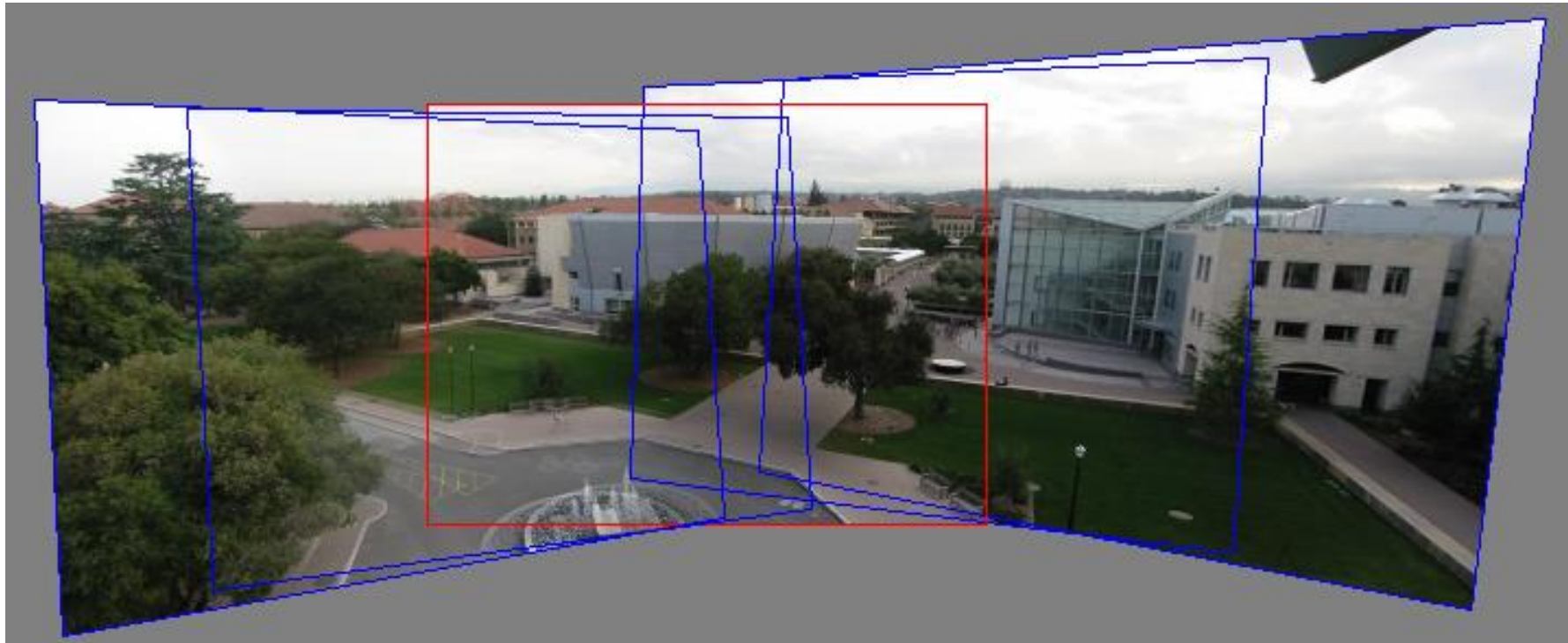
**Step 3:** Convert rays in camera 1's coordinates to pixels in image 1's coordinates.

$$\begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix} \sim \underbrace{\mathbf{K}_1 \mathbf{R}_2^T \mathbf{K}_2^{-1}}_{\substack{\text{3x3 homography} \\ \uparrow}} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$

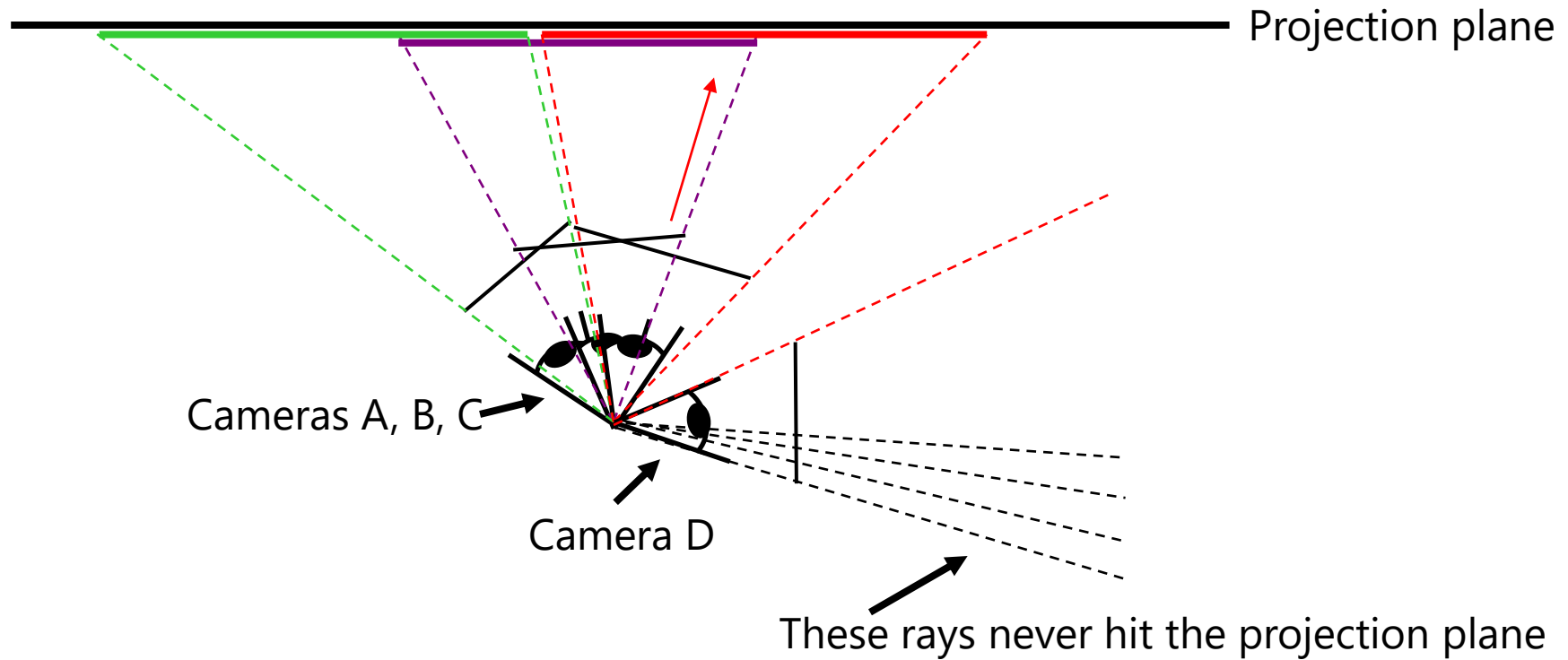
**How do we map points in image 2 into image 1?**

|                               |  |                |
|-------------------------------|--|----------------|
|                               | image 1                                  | image 2        |
| intrinsics                    | $\mathbf{K}_1$                           | $\mathbf{K}_2$ |
| extrinsics<br>(rotation only) | $\mathbf{R}_1 = \mathbf{I}_{3 \times 3}$ | $\mathbf{R}_2$ |

# Can we use homography to create a 360 panorama?

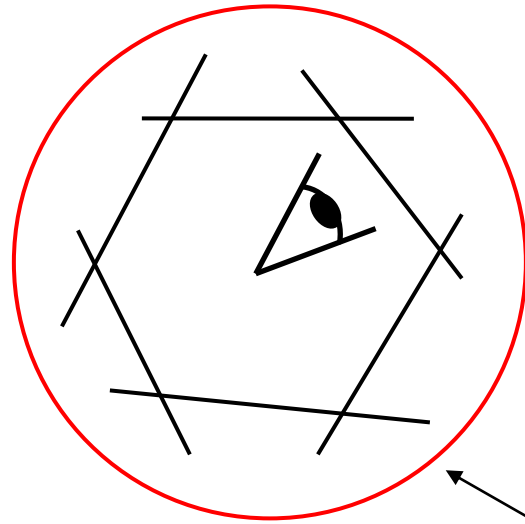


# Answer: No



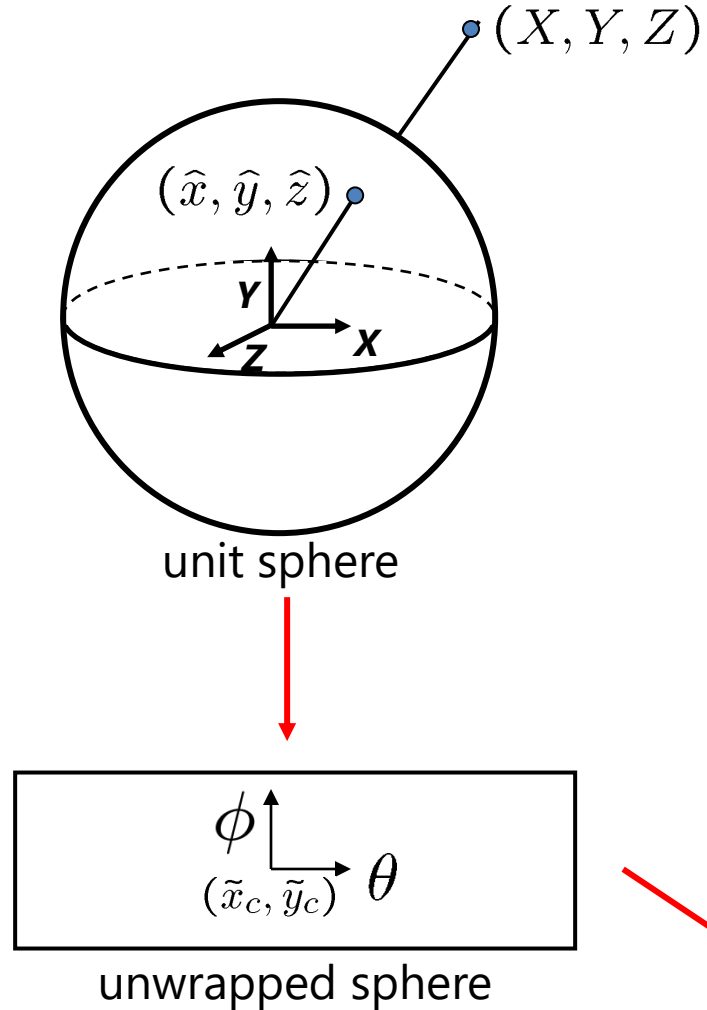
# Panoramas

- What if you want a 360° field of view?



mosaic Projection Sphere

# Spherical projection



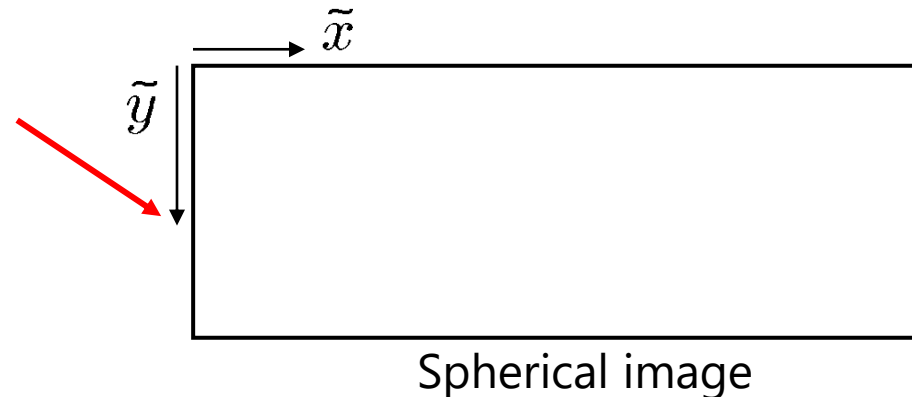
- Map 3D point  $(X, Y, Z)$  onto sphere

$$(\hat{x}, \hat{y}, \hat{z}) = \frac{1}{\sqrt{X^2 + Y^2 + Z^2}}(X, Y, Z)$$

- Convert to spherical coordinates  
 $(\sin\theta\cos\phi, \sin\phi, \cos\theta\cos\phi) = (\hat{x}, \hat{y}, \hat{z})$
- Convert to spherical image coordinates

$$(\tilde{x}, \tilde{y}) = (s\theta, s\phi) + (\tilde{x}_c, \tilde{y}_c)$$

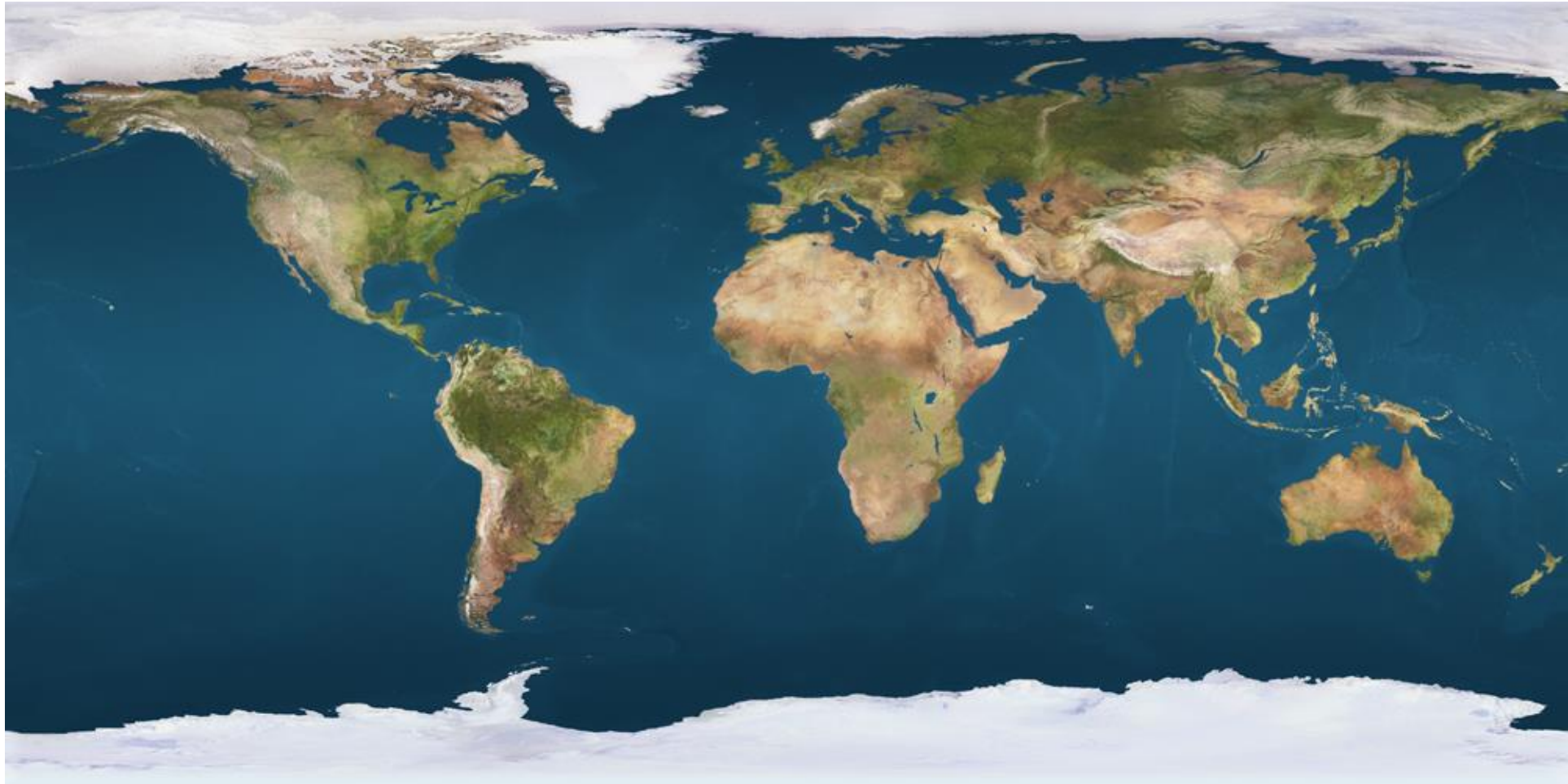
- $s$  defines size of the final image  
» often convenient to set  $s = \text{camera focal length}$



# Unwrapping a sphere



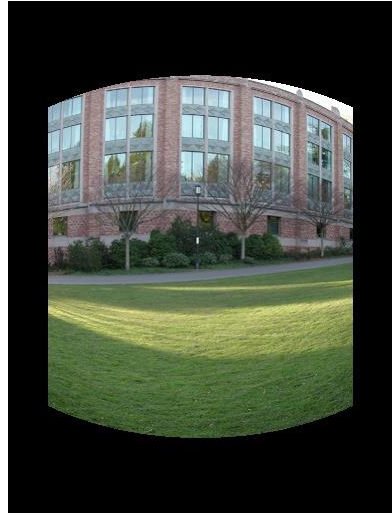
Credit: JHT's Planetary Pixel Emporium



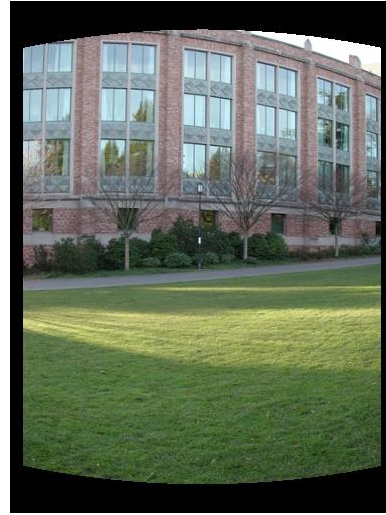
# Spherical reprojection



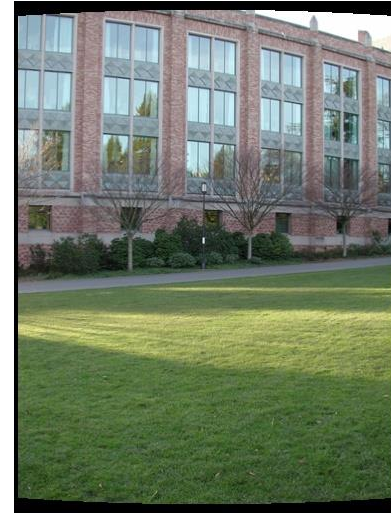
input



$f = 200$  (pixels)



$f = 400$



$f = 800$

- Map image to spherical coordinates
  - need to know the focal length



# Aligning spherical images



- Suppose we rotate the camera by  $\theta$  about the vertical axis
  - How does this change the spherical image?

# Aligning spherical images



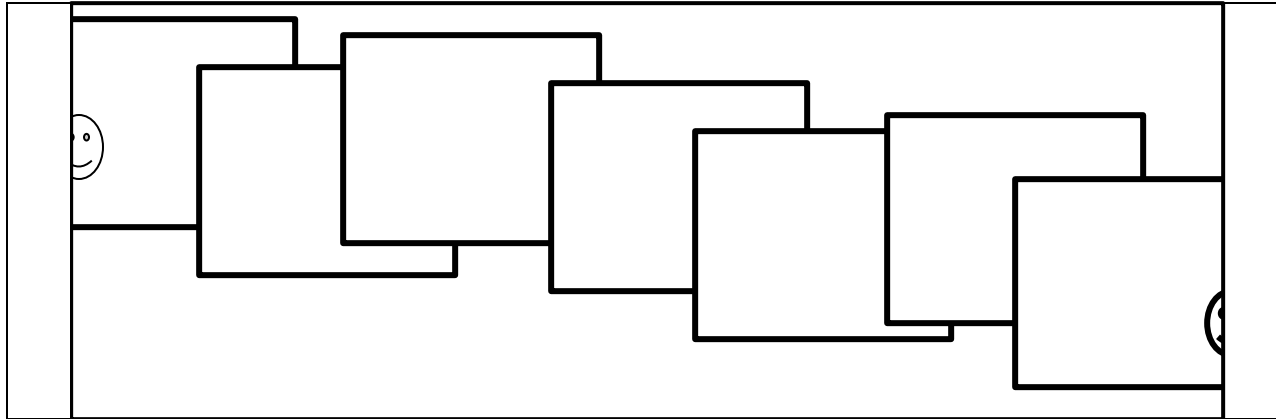
- Suppose we rotate the camera by  $\theta$  about the vertical axis
  - How does this change the spherical image?
    - Translation by  $\theta$
  - This means that we can align spherical images by translation

# Assembling the panorama



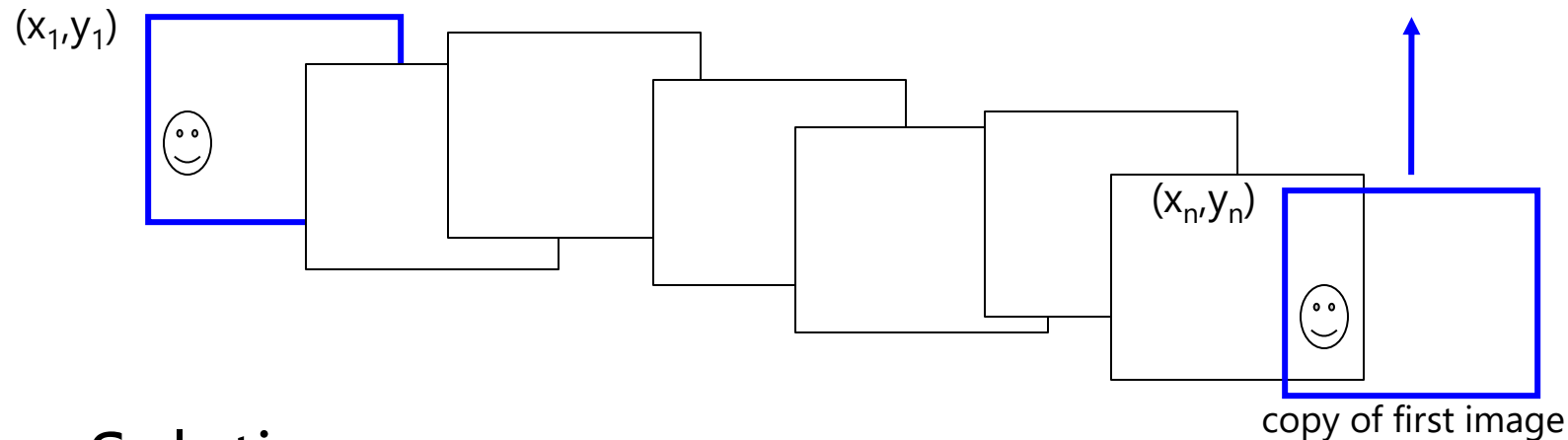
- Stitch pairs together, blend, then crop

# Problem: Drift



- Error accumulation
  - small errors accumulate over time

# Problem: Drift



- Solution
  - add another copy of first image at the end
  - this gives a constraint:  $y_n = y_1$
  - there are a bunch of ways to solve this problem
    - add displacement of  $(y_1 - y_n)/(n - 1)$  to each image after the first
    - **apply an affine warp:  $y' = y + ax$  [you will implement this for P3]**
    - run a big optimization problem, incorporating this constraint
      - best solution, but more complicated
      - known as "bundle adjustment"

# Project 3

1. Take pictures on a tripod (or handheld)
2. Warp to spherical coordinates (not needed if using homographies to align images)
3. Extract features
4. Align neighboring pairs using feature matching + RANSAC
5. Write out list of neighboring translations
6. Correct for drift
7. Read in warped images and blend them
8. Crop the result and import into a viewer

- Roughly based on **Autostitch**

- By Matthew Brown and David Lowe

- <http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html>

# Spherical panoramas



Microsoft Lobby: <http://www.acm.org/pubs/citations/proceedings/graph/258734/p251-szeliski>

# Different projections are possible



Cube-map



# Blending

- We've aligned the images – now what?

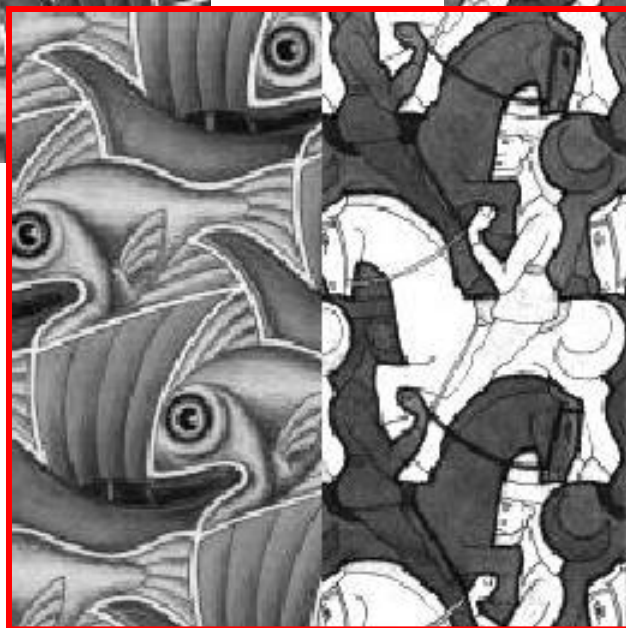
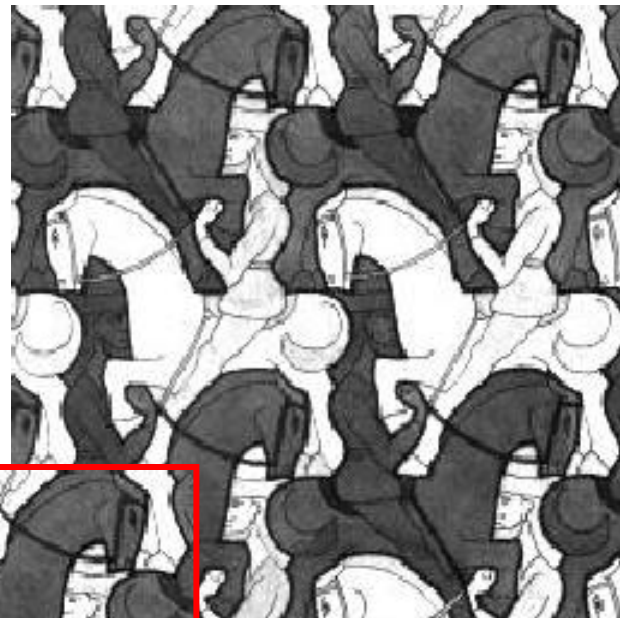
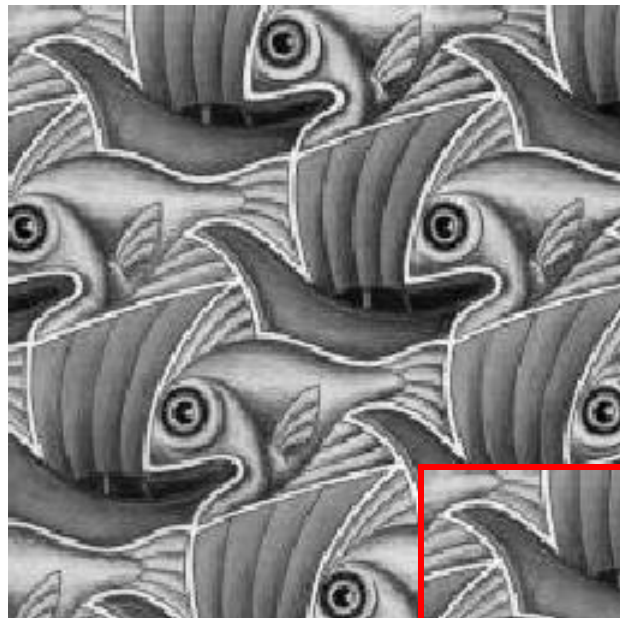


# Blending

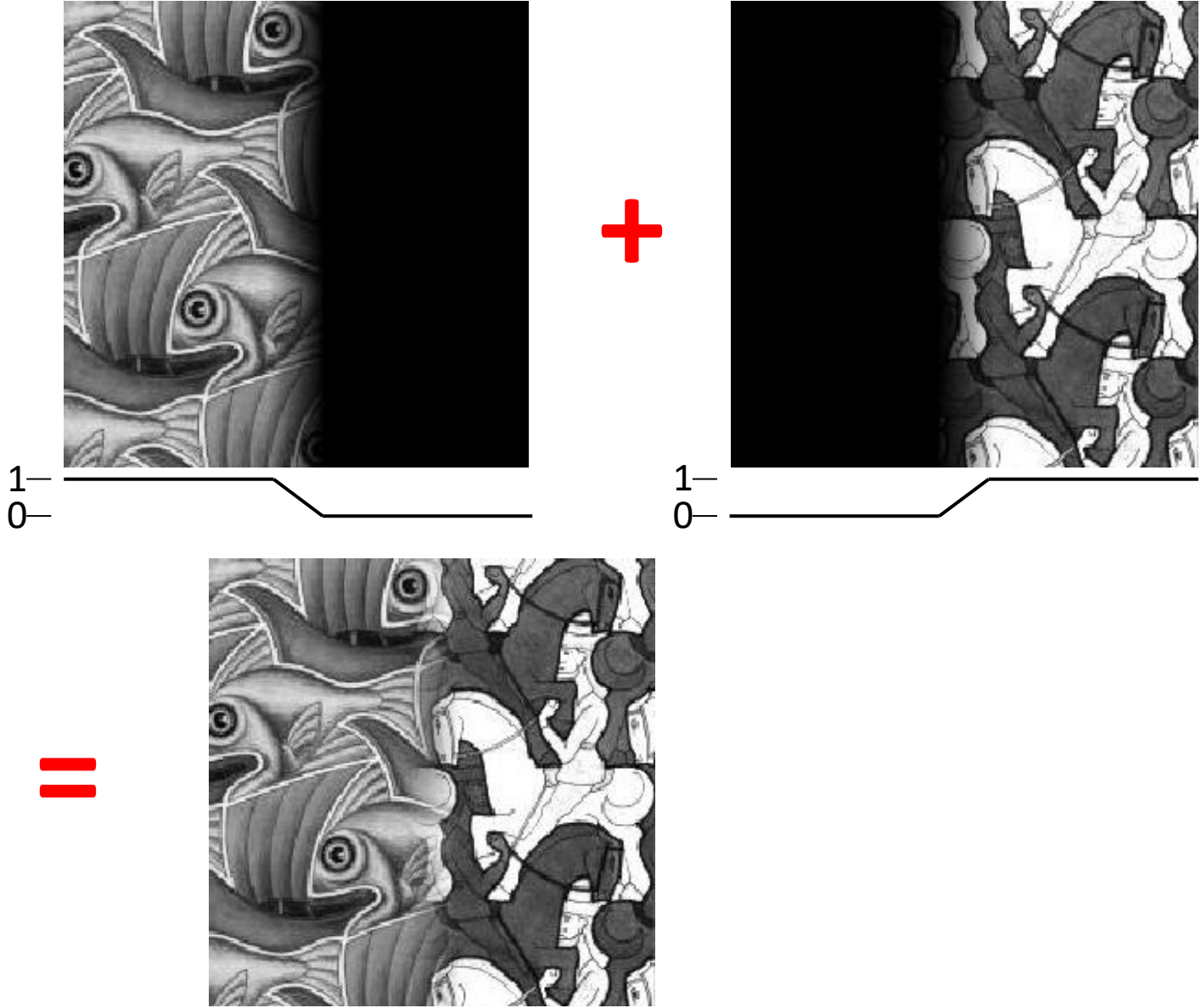
- Want to seamlessly blend them together



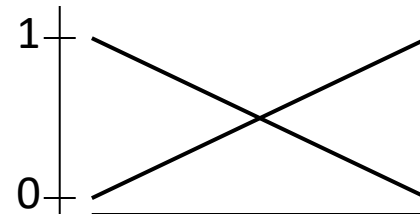
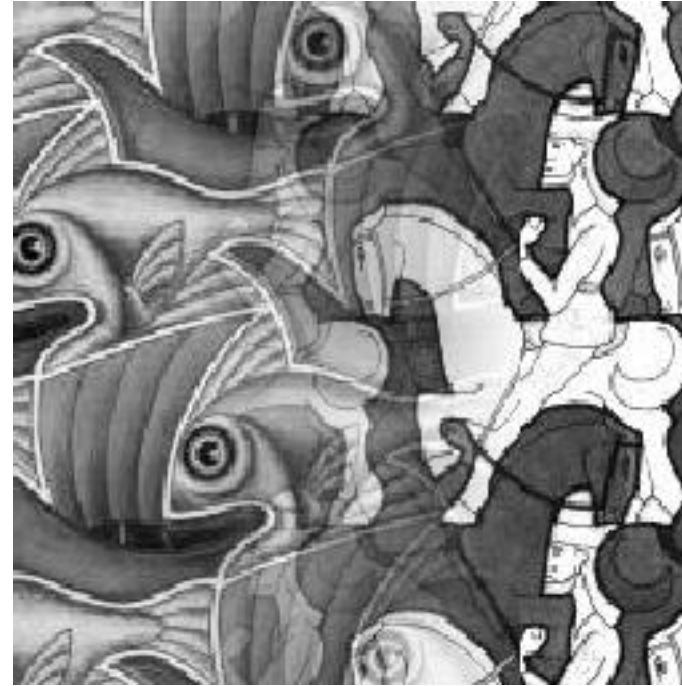
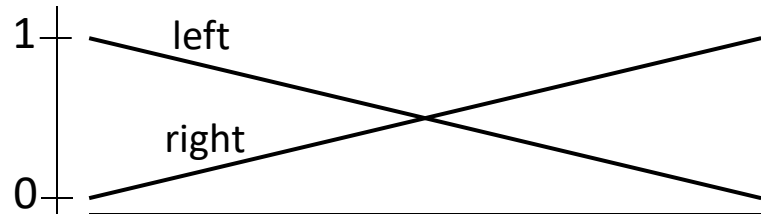
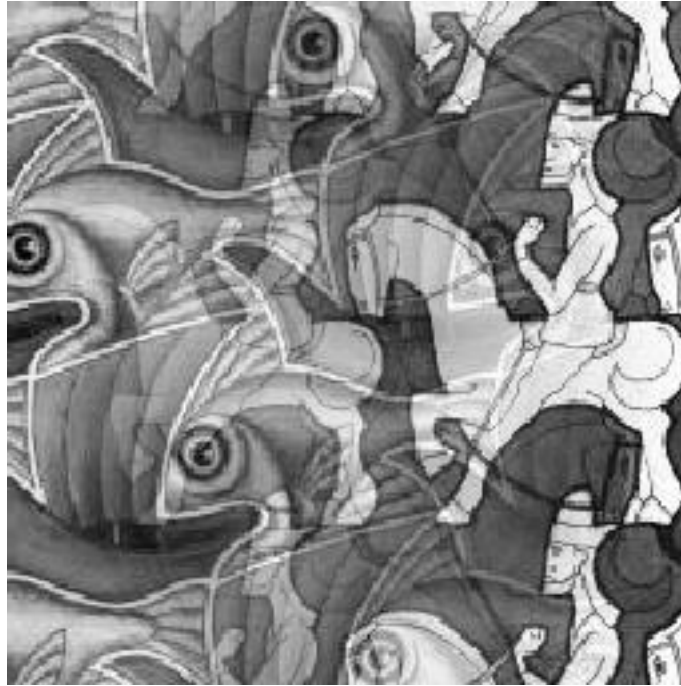
# Image Blending



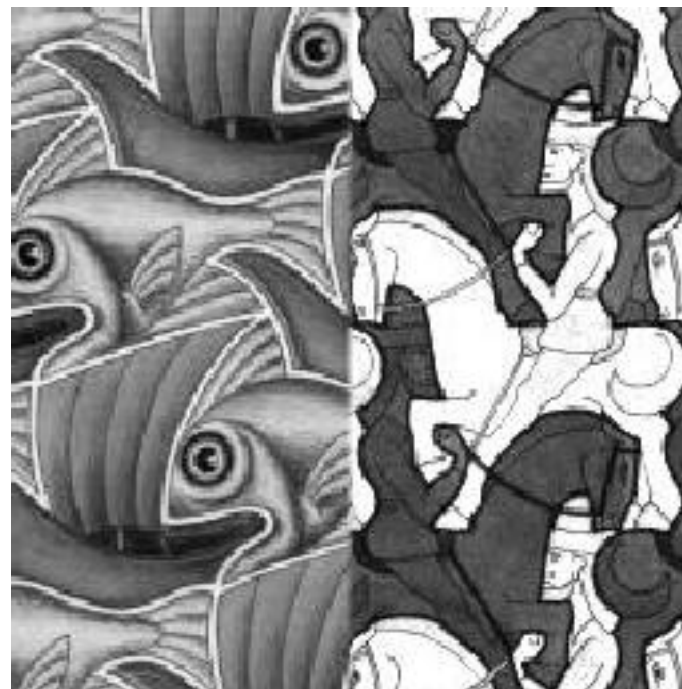
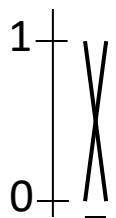
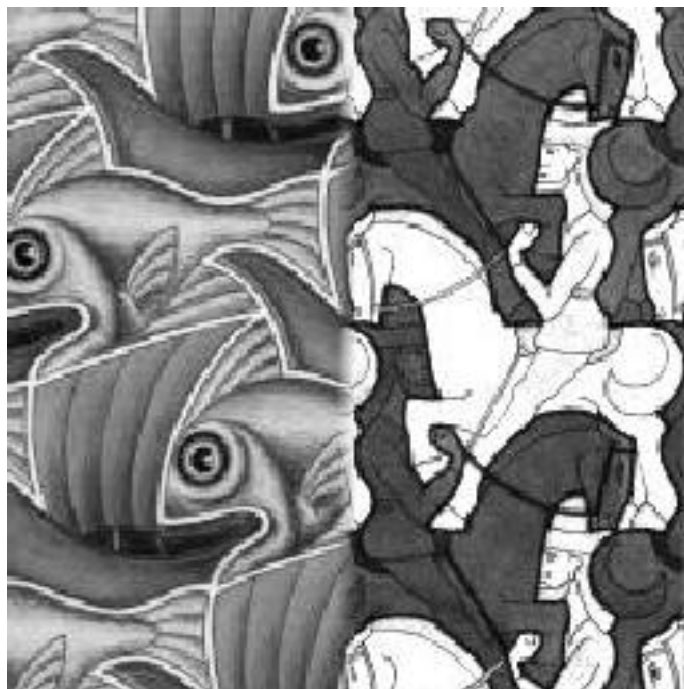
# Feathering



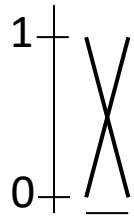
# Effect of window size



# Effect of window size



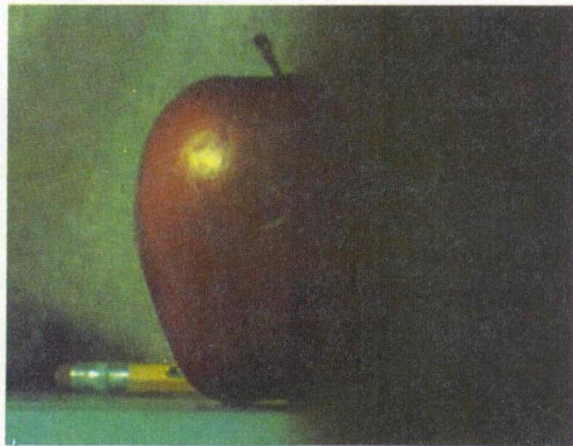
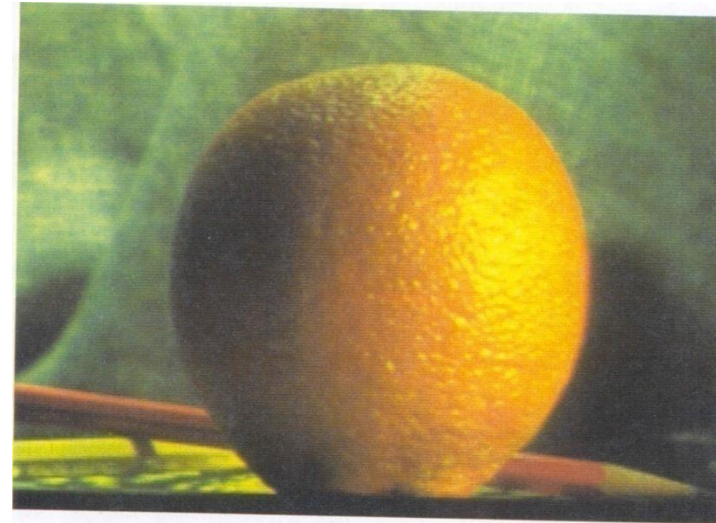
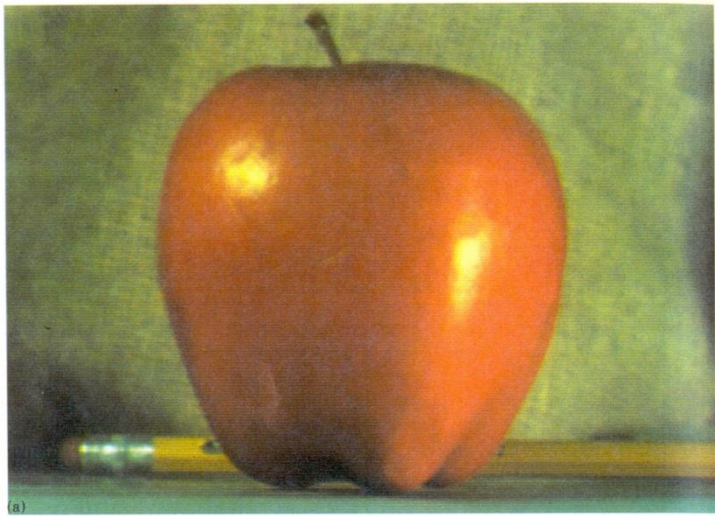
# Good window size



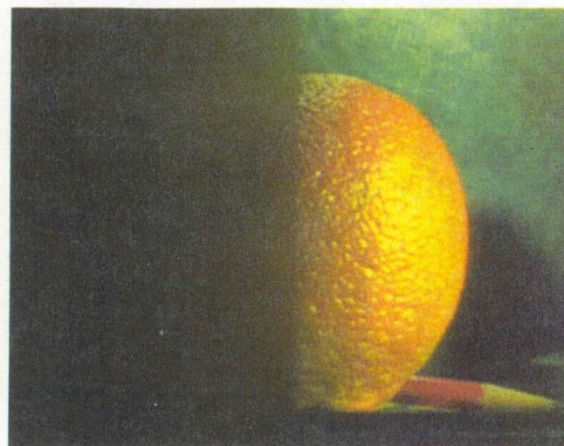
“Optimal” window: smooth but not ghosted

- Doesn't always work...

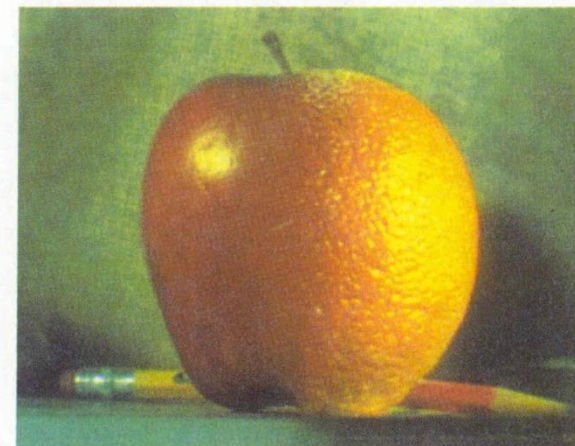
# Pyramid blending



(d)



(h)



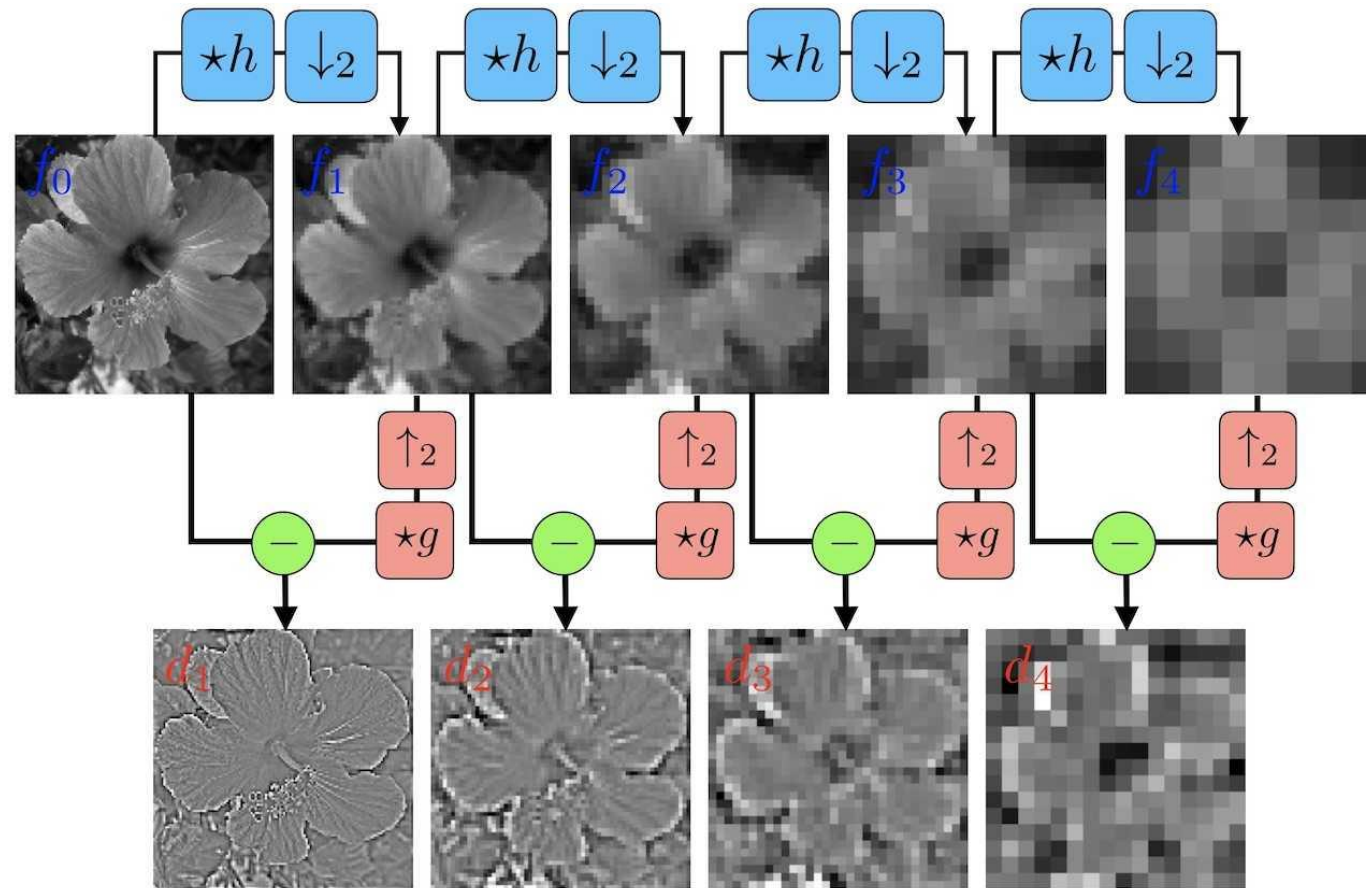
(l)

Create a Laplacian pyramid, blend each level

- Burt, P. J. and Adelson, E. H., [A multiresolution spline with applications to image mosaics](#), ACM Transactions on Graphics, 42(4), October 1983, 217-236.



# The Laplacian Pyramid



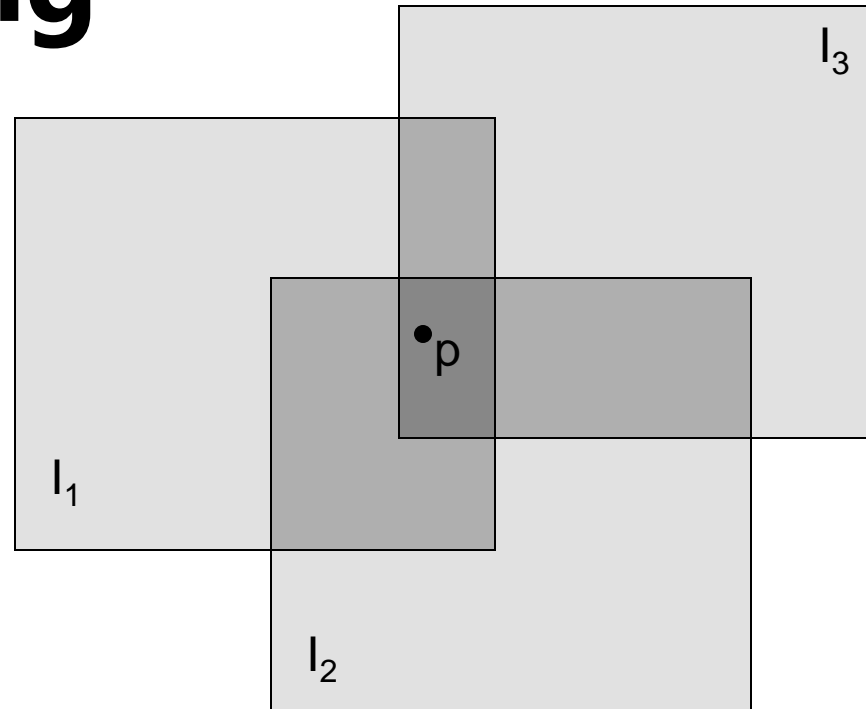
Forward transform:

$$f_j = (f_{j-1} \star h) \downarrow_2$$
$$d_j = f_j - (f_{j-1} \uparrow_2) \star g$$

Backward transform:

$$f_j = d_j + (f_{j-1} \uparrow_2) \star g$$

# Alpha Blending



see Blinn (CGA, 1994) for details:

[Compositing, Part 1: Theory](#)

Encoding blend weights:  $I(x,y) = (\alpha R, \alpha G, \alpha B, \alpha)$

color at  $p = \frac{(\alpha_1 R_1, \alpha_1 G_1, \alpha_1 B_1) + (\alpha_2 R_2, \alpha_2 G_2, \alpha_2 B_2) + (\alpha_3 R_3, \alpha_3 G_3, \alpha_3 B_3)}{\alpha_1 + \alpha_2 + \alpha_3}$

Implement this in two steps:

1. accumulate: add up the ( $\alpha$  premultiplied)  $RGB\alpha$  values at each pixel
2. normalize: divide each pixel's accumulated  $RGB$  by its  $\alpha$  value

Q: what if  $\alpha = 0$ ?

# Poisson Image Editing



For more info: [Perez et al, SIGGRAPH 2003](#)

# Some panorama examples



"Before SIGGRAPH Deadline" Photo credit: Doug Zongker

# Some panorama examples

- Every image on Google Streetview



# Magic: ghost removal



M. Uyttendaele, A. Eden, and R. Szeliski.  
*Eliminating ghosting and exposure artifacts in image mosaics.*  
ICCV 2001

# Magic: ghost removal



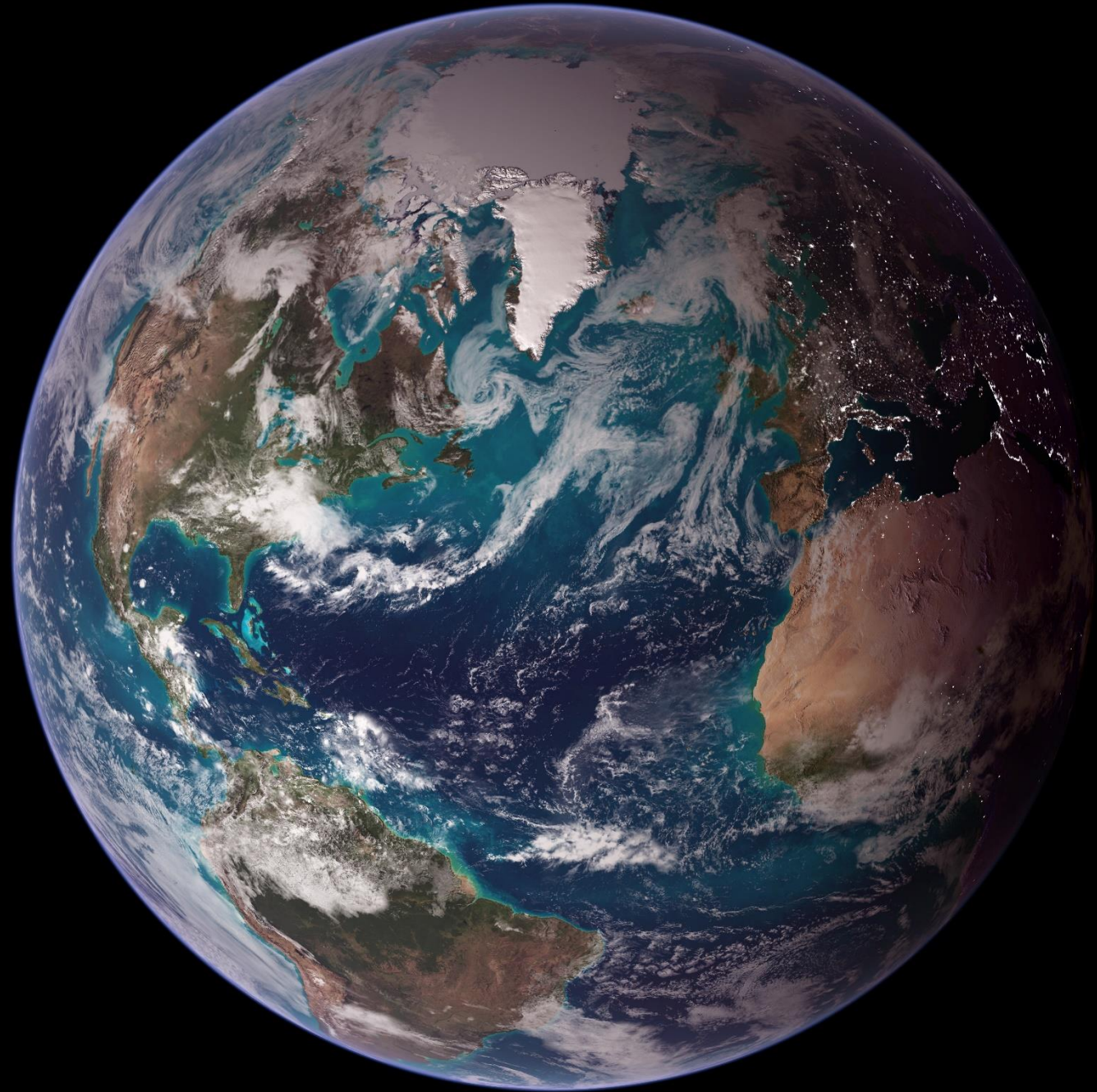
M. Uyttendaele, A. Eden, and R. Szeliski.  
*Eliminating ghosting and exposure artifacts in image mosaics.*  
ICCV 2001

# Other types of mosaics



- Can mosaic onto *any* surface if you know the geometry
  - See NASA's [Visible Earth project](#) for some stunning earth mosaics







[https://www.nasa.gov/centers/wallops/news/frozen\\_sos.ht](https://www.nasa.gov/centers/wallops/news/frozen_sos.html)  
ml

# Science on a Sphere



[https://news.vcu.edu/article/Science On a Sphere now at VCU offers a world of possibilities](https://news.vcu.edu/article/Science%20On%20a%20Sphere%20now%20at%20VCU%20offers%20a%20world%20of%20possibilities)

**Questions?**

# Alternative to feathering

- **Cut and fuse**

# Interactive Digital Photomontage



Aseem Agarwala, Mira Dontcheva  
Maneesh Agrawala, Steven Drucker, Alex Colburn  
Brian Curless, David Salesin, Michael Cohen

