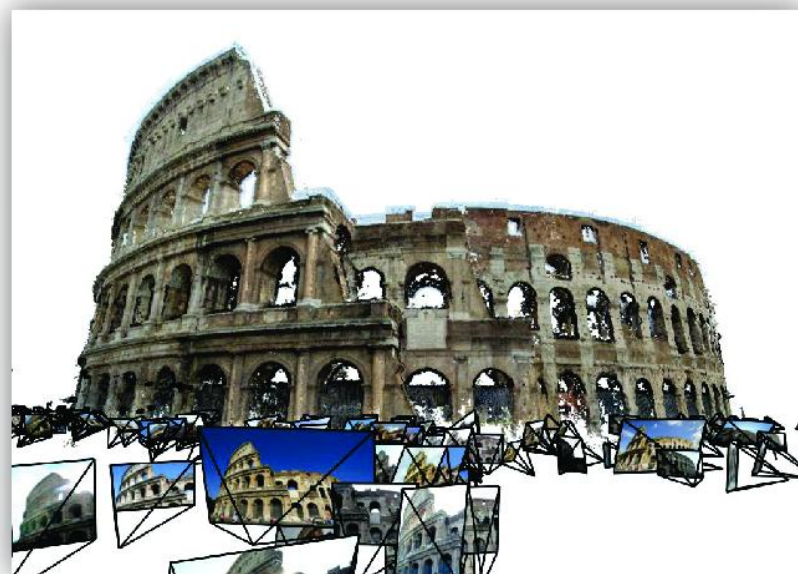
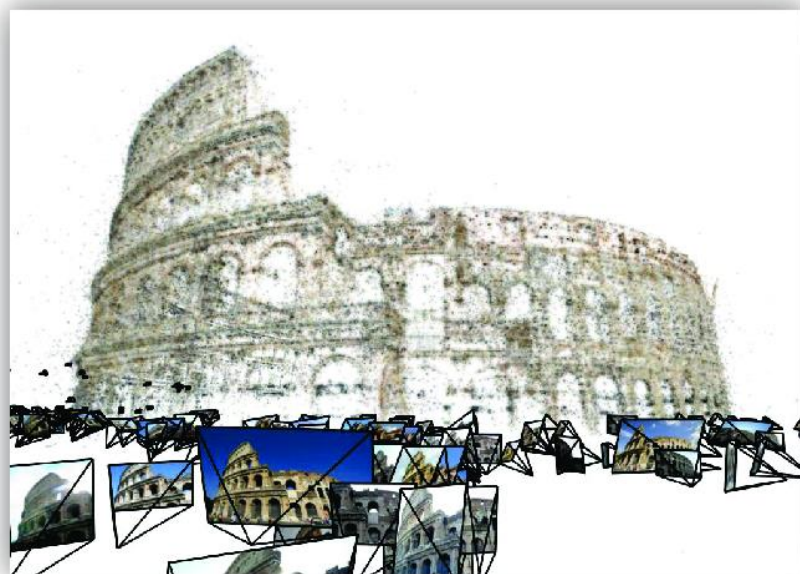


# CS5670: Computer Vision

Noah Snavely

## Multi-view stereo



# Announcements

- Project 3 (“Autostitch”) due Monday 4/17 by 11:59pm

# Recommended Reading

Szeliski Chapter 11.6

Multi-View Stereo: A Tutorial

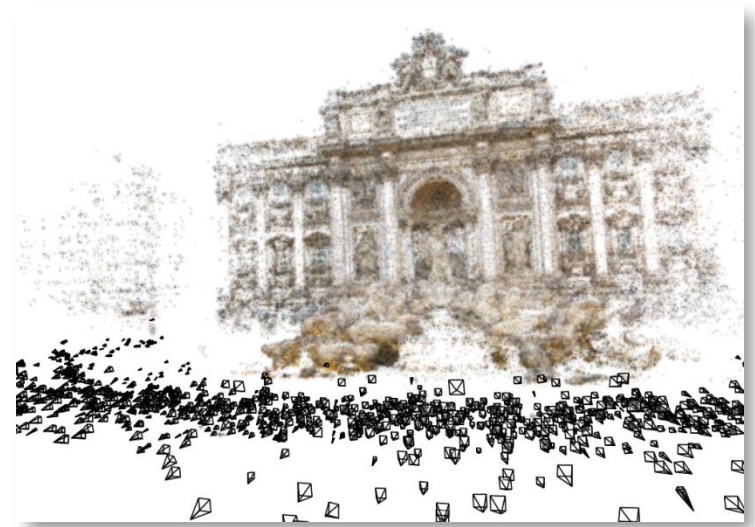
Furukawa and Hernandez, 2015

[http://www.cse.wustl.edu/~furukawa/papers/fnt\\_mvs.pdf](http://www.cse.wustl.edu/~furukawa/papers/fnt_mvs.pdf)

# Multi-view Stereo



Stereo



Multi-view stereo

# Multi-view Stereo



[Point Grey's](#) Bumblebee XB3

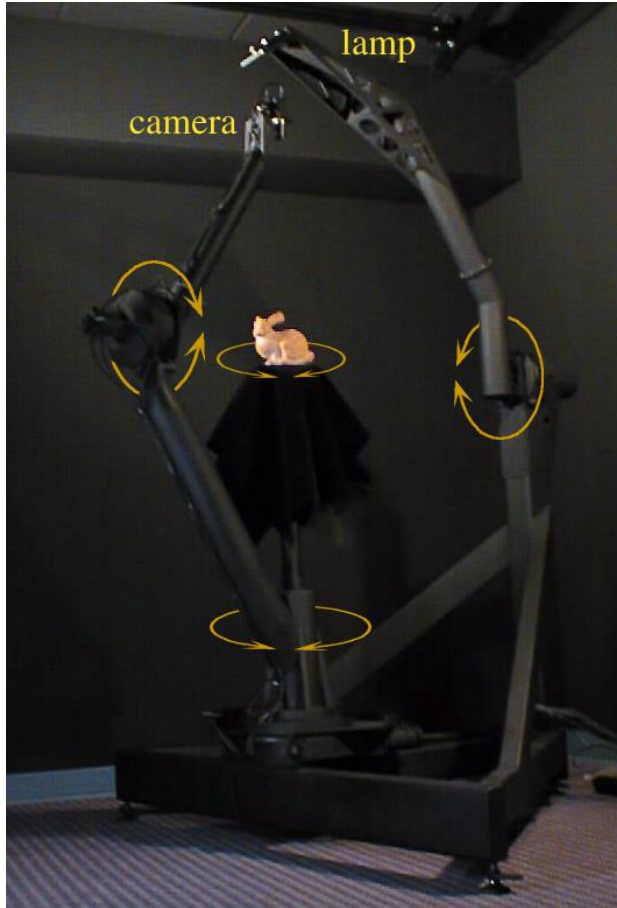


[Point Grey's](#) ProFusion 25



CMU's [3D Room](#)

# Multi-view Stereo



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### Search













Photos Groups People

statue of liberty

Full text Tags only

✓ We found **80,865** results matching **statue** and **of** and **liberty**.

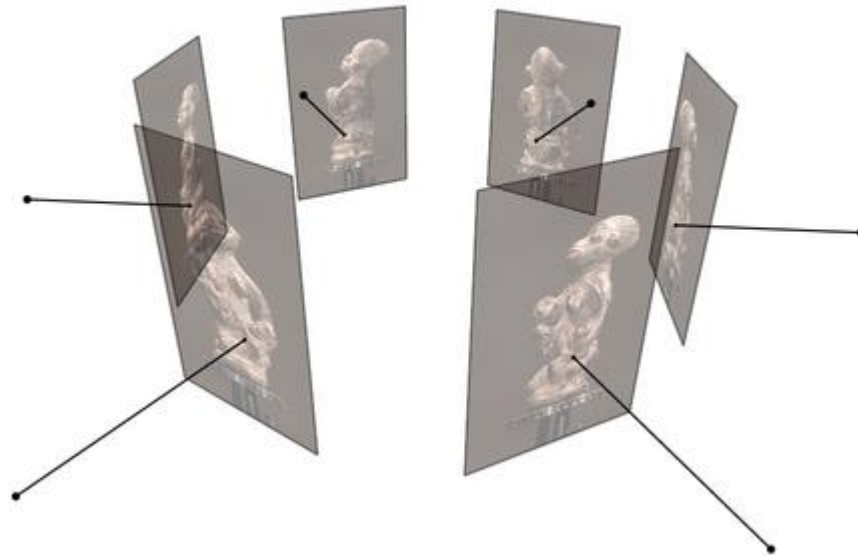
View: Most relevant • Most recent • Most interesting Show: Details • Thumbnails

 From <a href="#">mbell1975</a>	 From <a href="#">sbcreate11</a>	 From <a href="#">Marion Doss</a>	 From <a href="#">Barry Wright</a>
 From <a href="#">phileole</a>	 From <a href="#">almk</a>	 From <a href="#">sbcreate11</a>	 From <a href="#">sbcreate11</a>
 From <a href="#">sjgardiner</a>	 From <a href="#">sjgardiner</a>	 From <a href="#">elesa.ah</a>	 From <a href="#">nicoatridge</a>

# Multi-view Stereo

Input: calibrated images from several viewpoints

Output: 3D object model

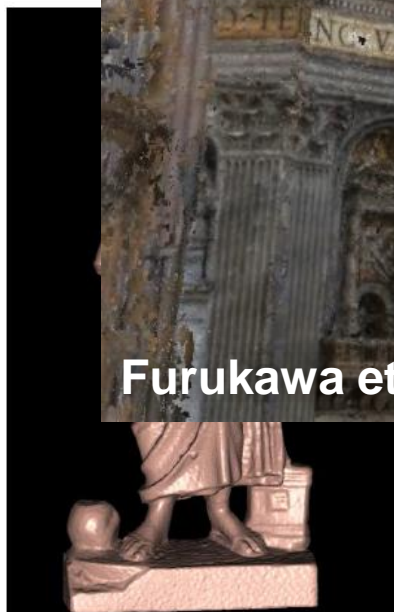


Figures by Carlos Hernandez



Furukawa et al., 2010

Faugeras, Keriven  
1998



Hernandez, Schmitt  
2004



Pons, Keriven, Faugeras  
2005



Furukawa, Ponce  
2006



Goesele et al.  
2007





# Applications



Data SIO, NOAA, U.S. Navy, NGA, GEBCO

Google earth



でんじろんさん

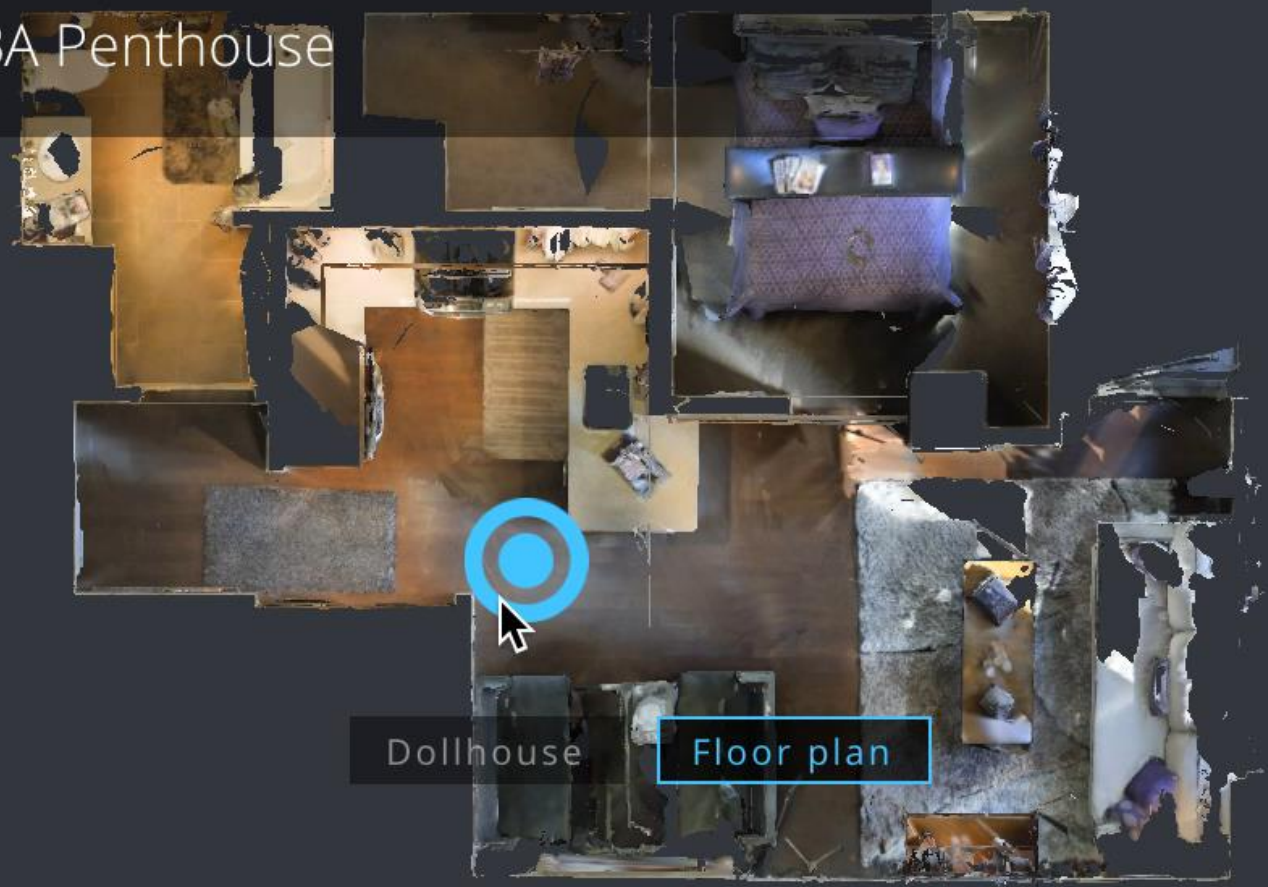
by じろう でん 266,  





< 1BR, 1BA Penthouse

Terms



Dollhouse

Floor plan



# Whistle in the Form of Female Figure *600 AD - 900 AD*

Details Los Angeles County Museum of Art



Los Angeles County Museum of Art



Sculpture



Mexico

Share

Compare

Saved <sup>0</sup>

Discover

Google



JUMP

Google



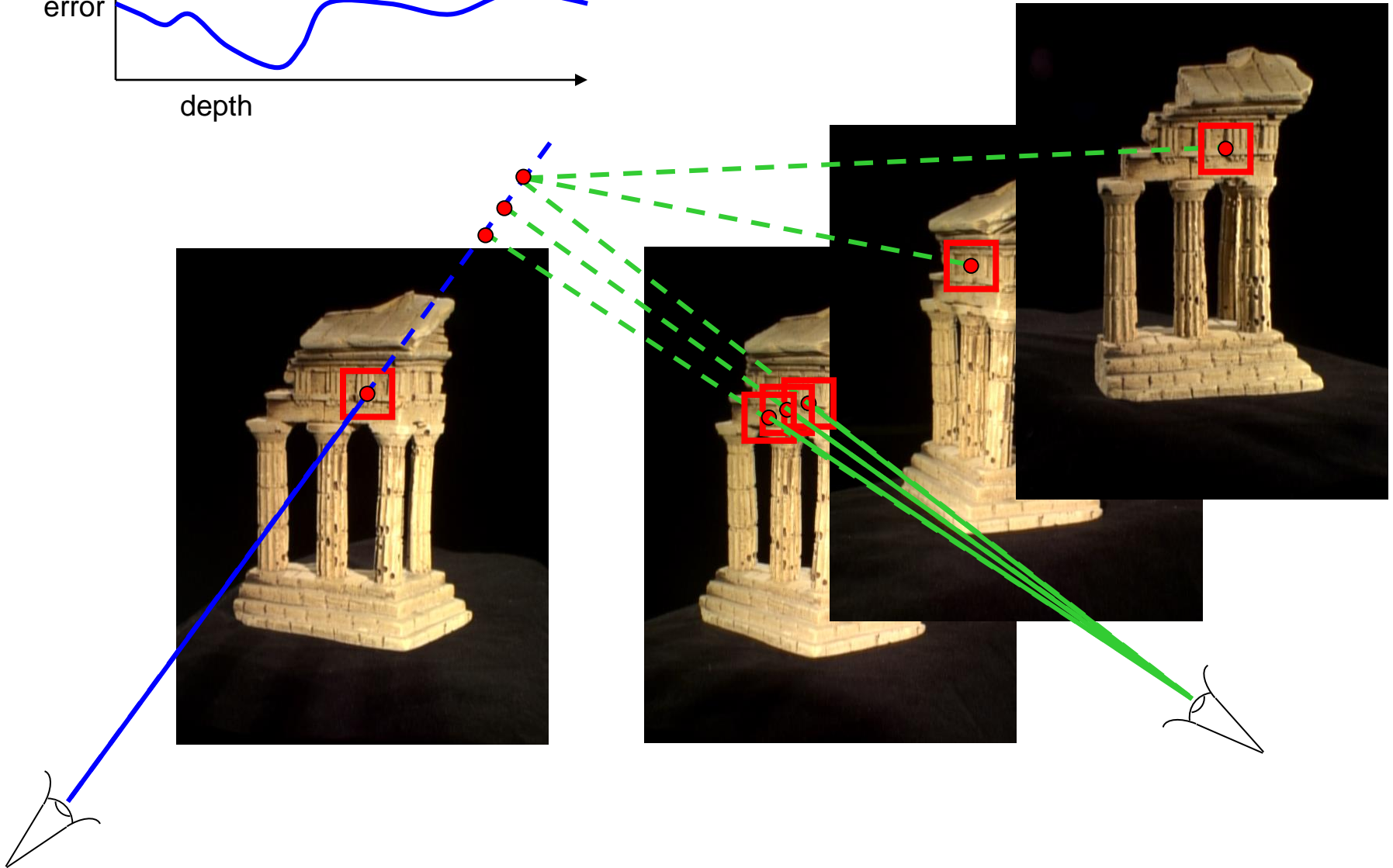
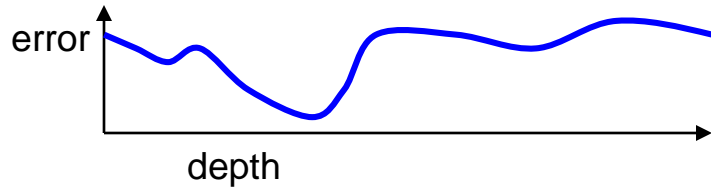


c|net





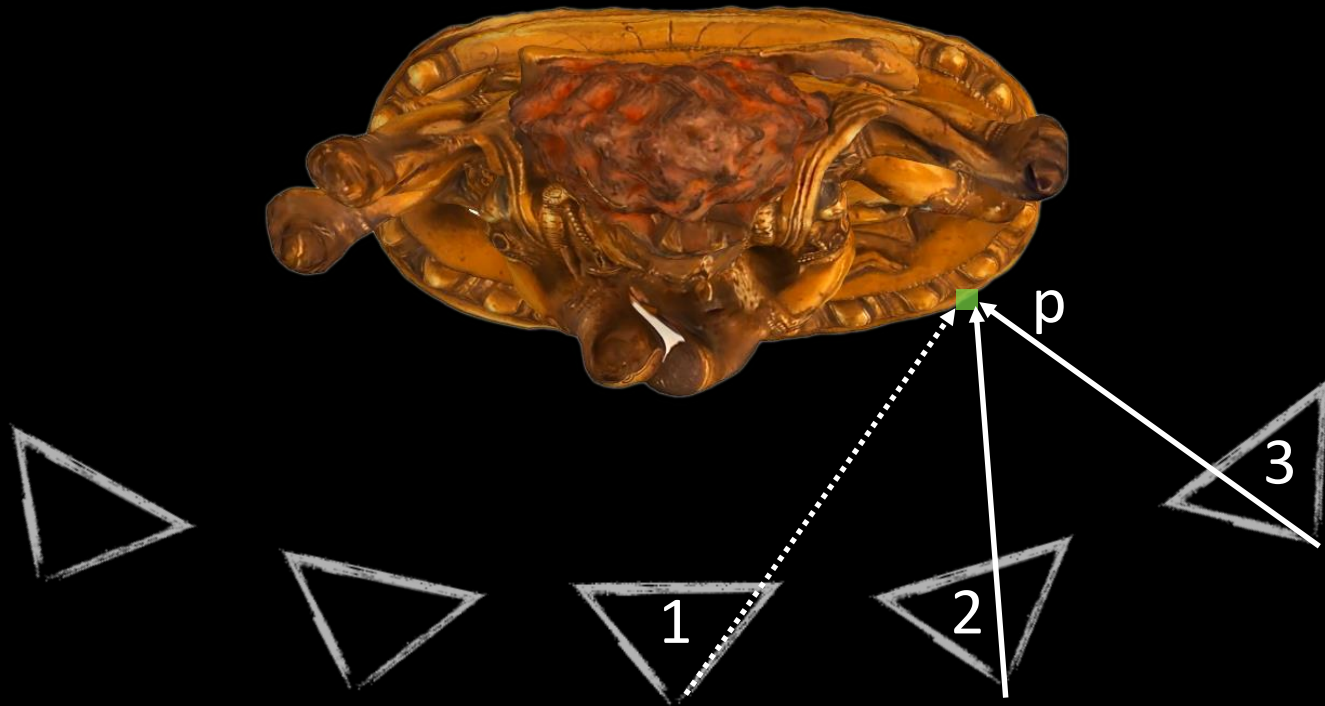
# Stereo: another view



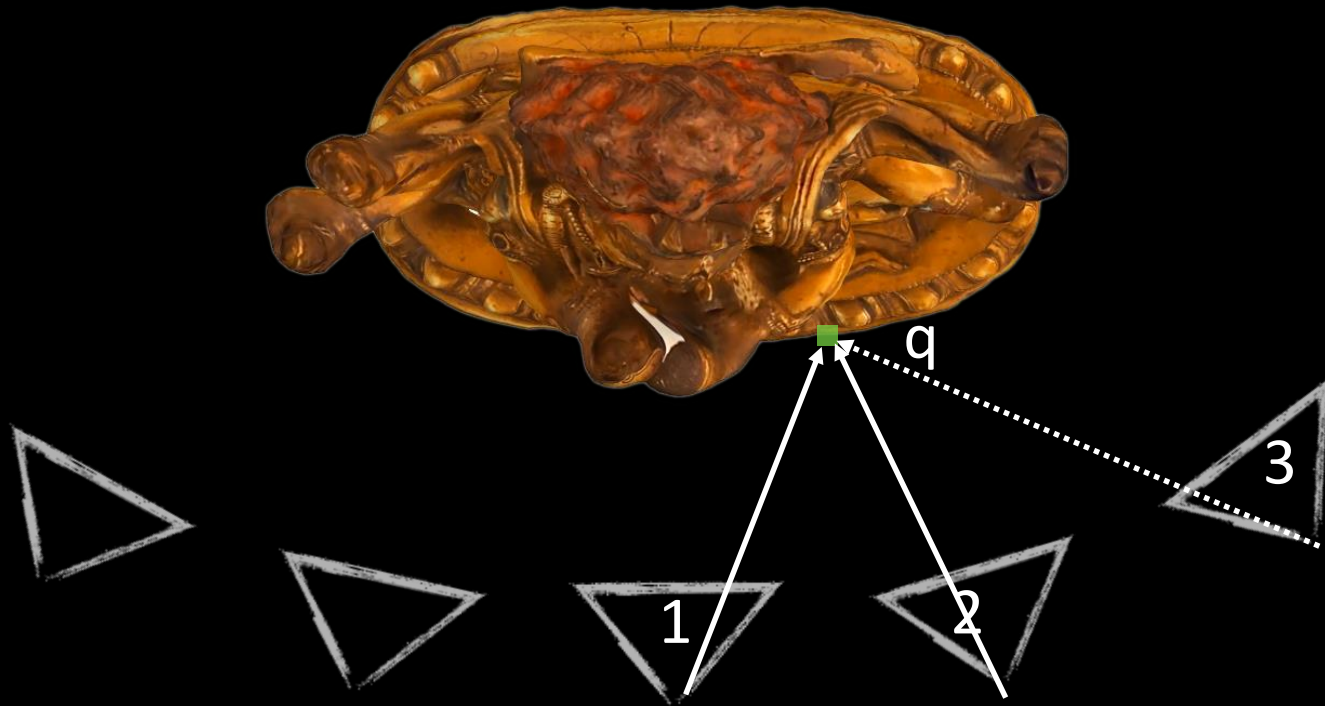


# Why MVS?

- Different points on the object's surface will be more clearly visible in some subset of cameras
  - Could have high-res closeups of some regions
  - Some surfaces are foreshortened from certain views



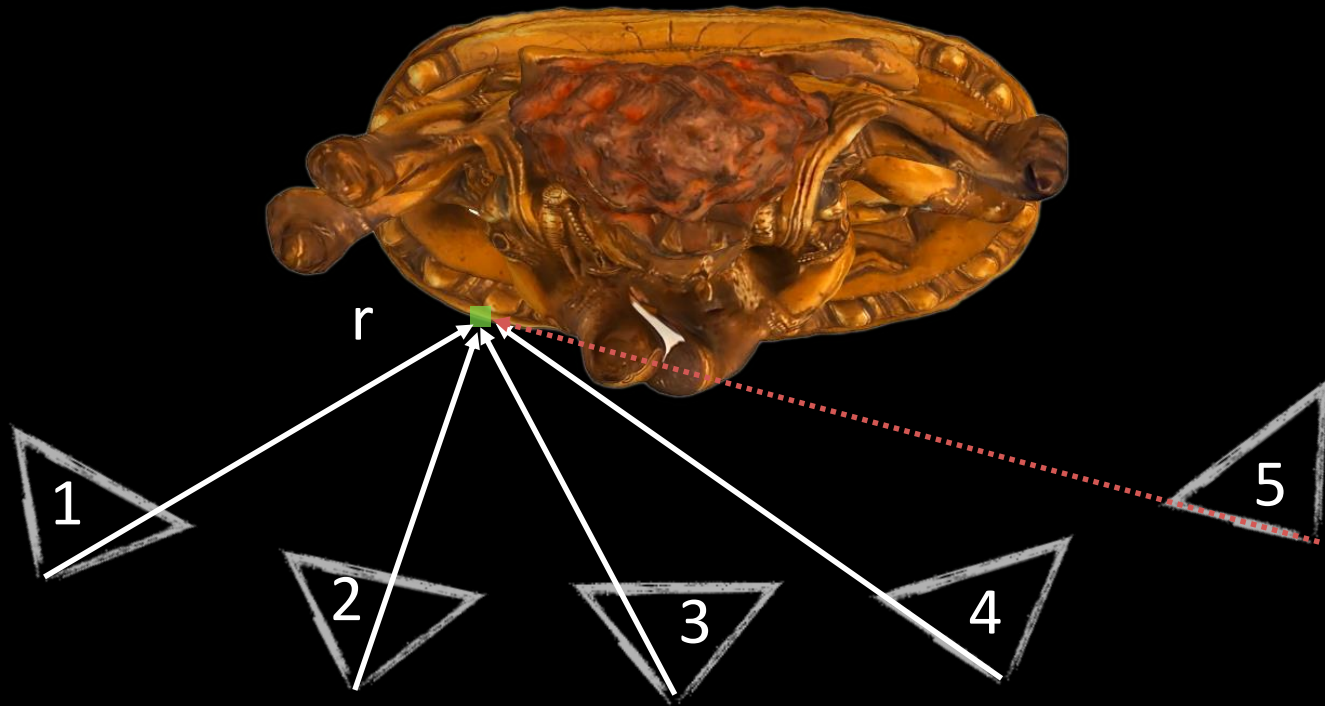
Cameras 2 and 3 can more clearly see point  $p$ .



Cameras 1 and 2 can more clearly see point  $q$ .

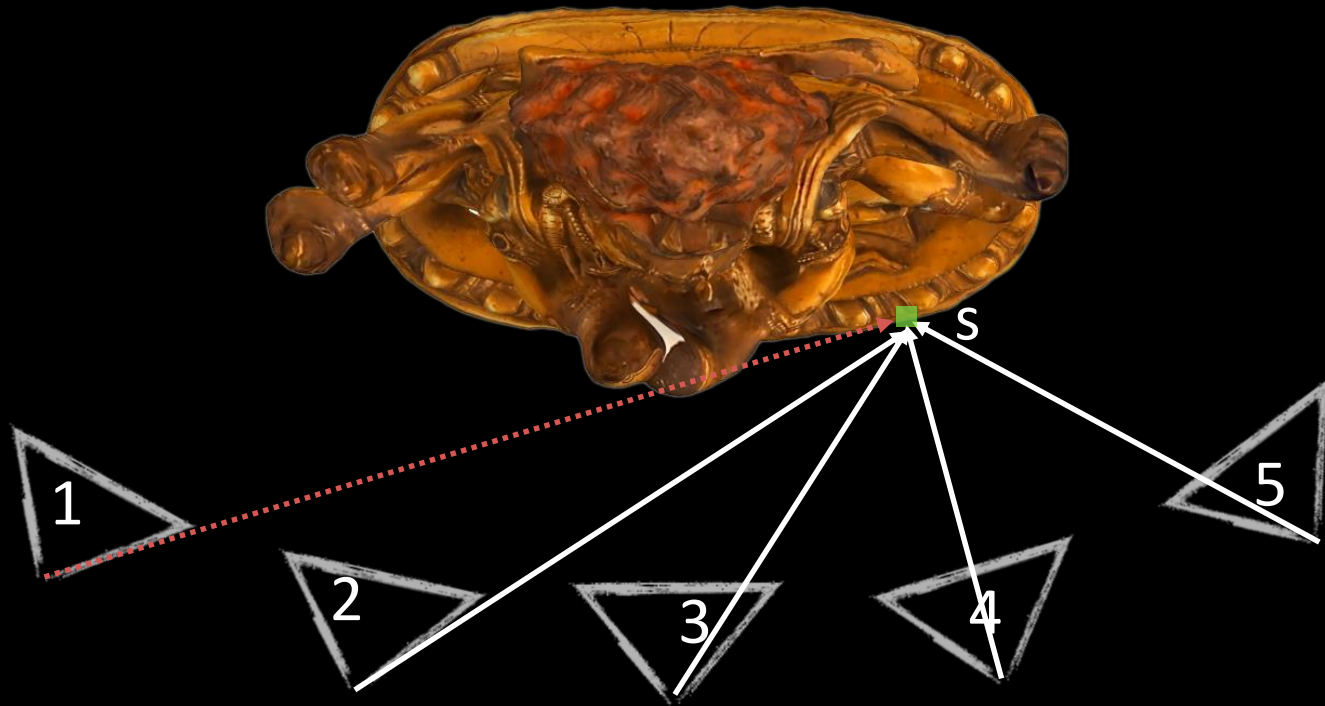
# Why MVS?

- Different points on the object's surface will be more clearly visible in some subset of cameras
  - Could have high res closeups of some regions
  - Some surfaces are foreshortened from certain views
- Some points may be occluded entirely in certain views



Camera 5 can't see point r.

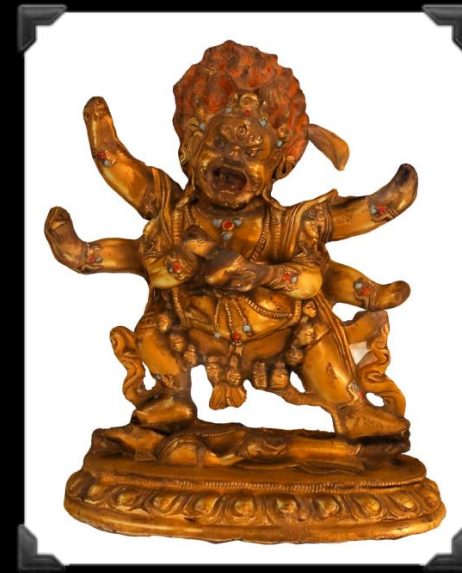


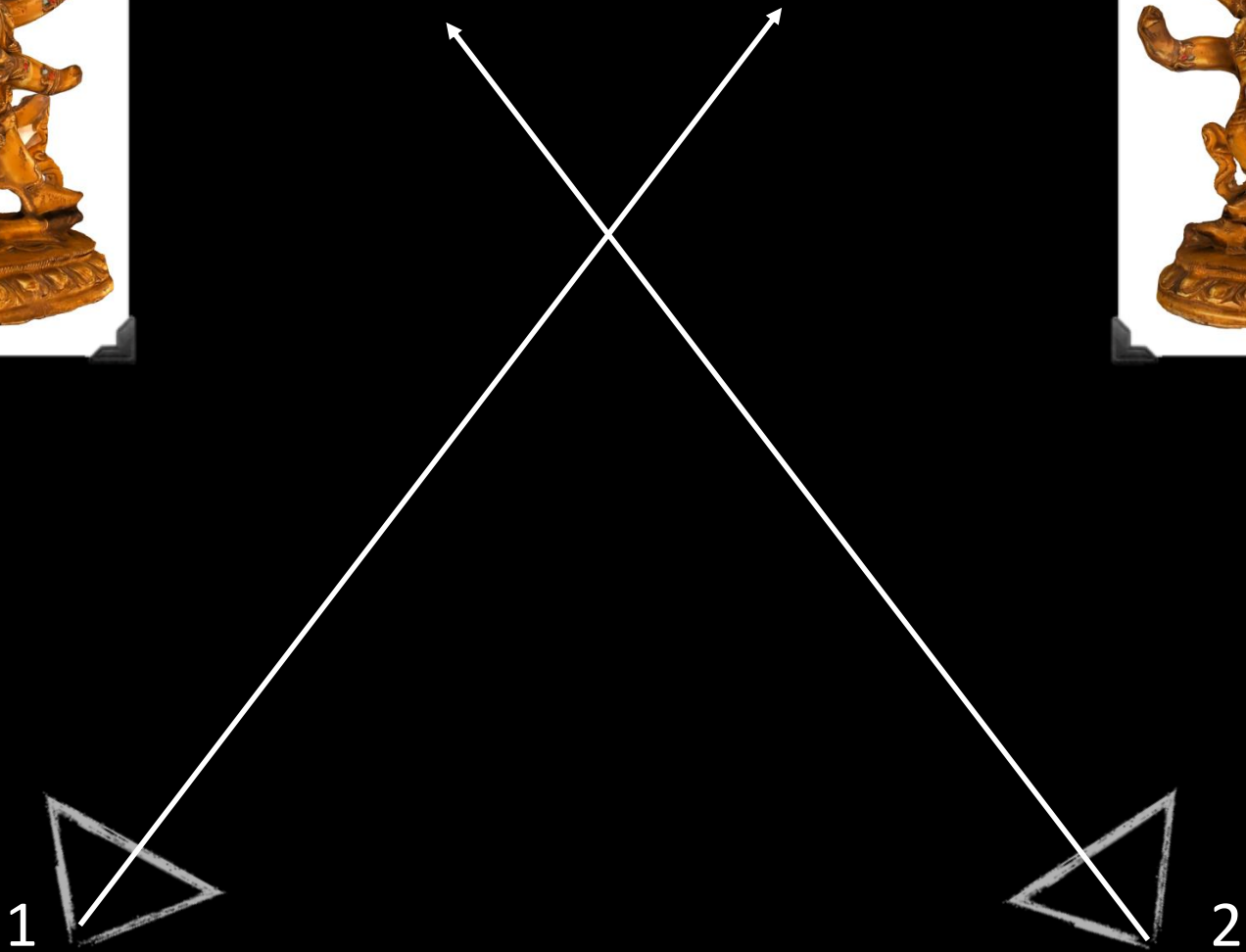
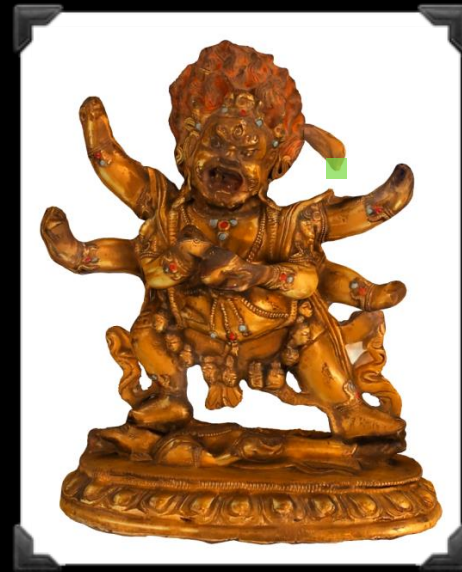


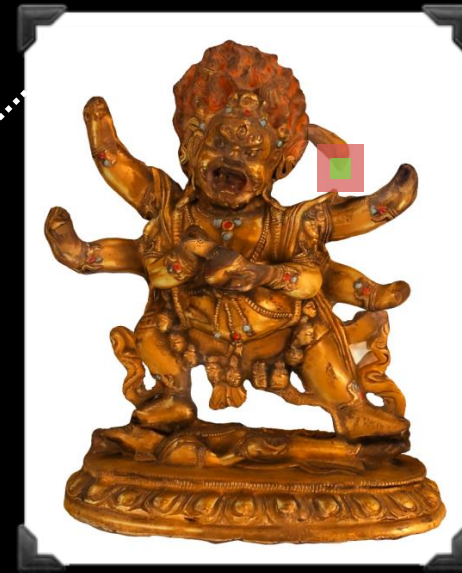
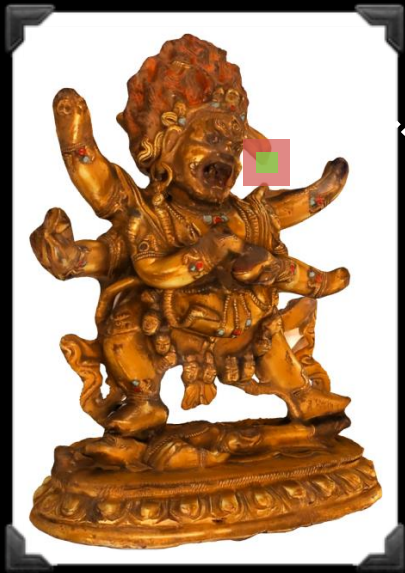
Camera 1 can't see point s.

# Why MVS?

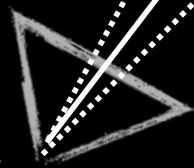
- Different points on the object's surface will be more clearly visible in some subset of cameras
  - Could have high res closeups of some regions
  - Some surfaces are foreshortened from certain views
- Some points may be occluded entirely in certain views
- More measurements per point can reduce error



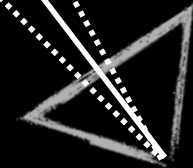




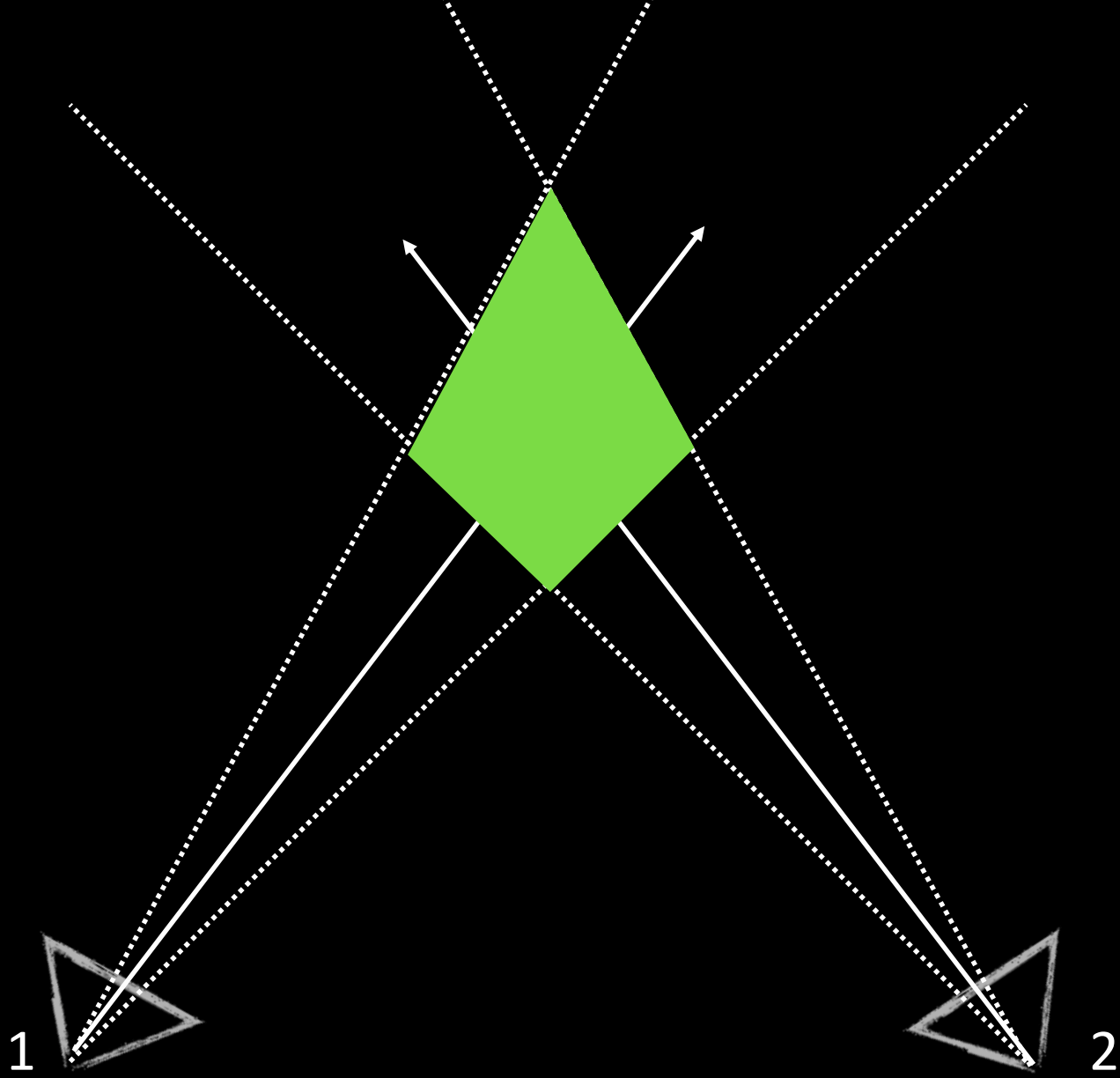
1



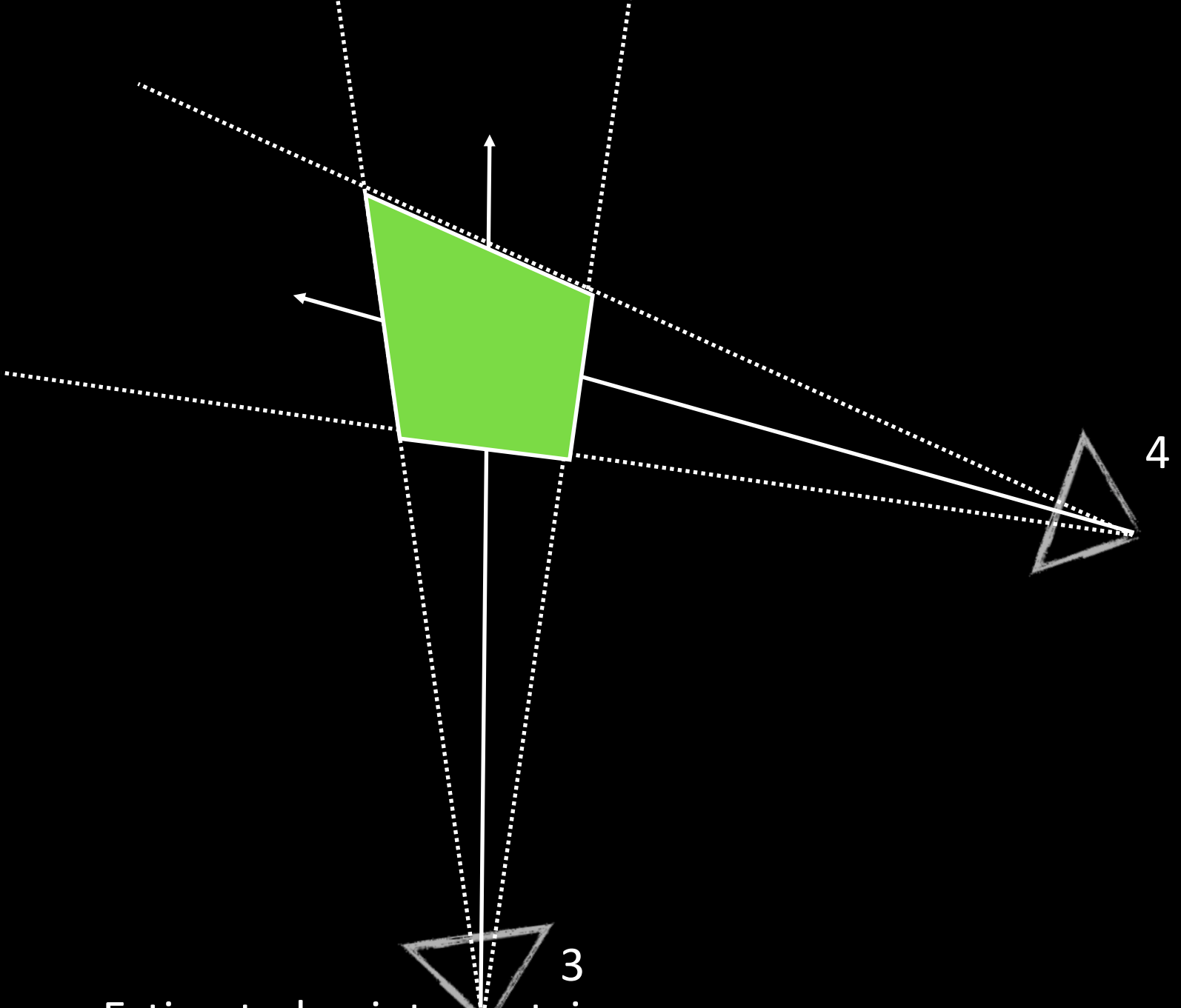
2



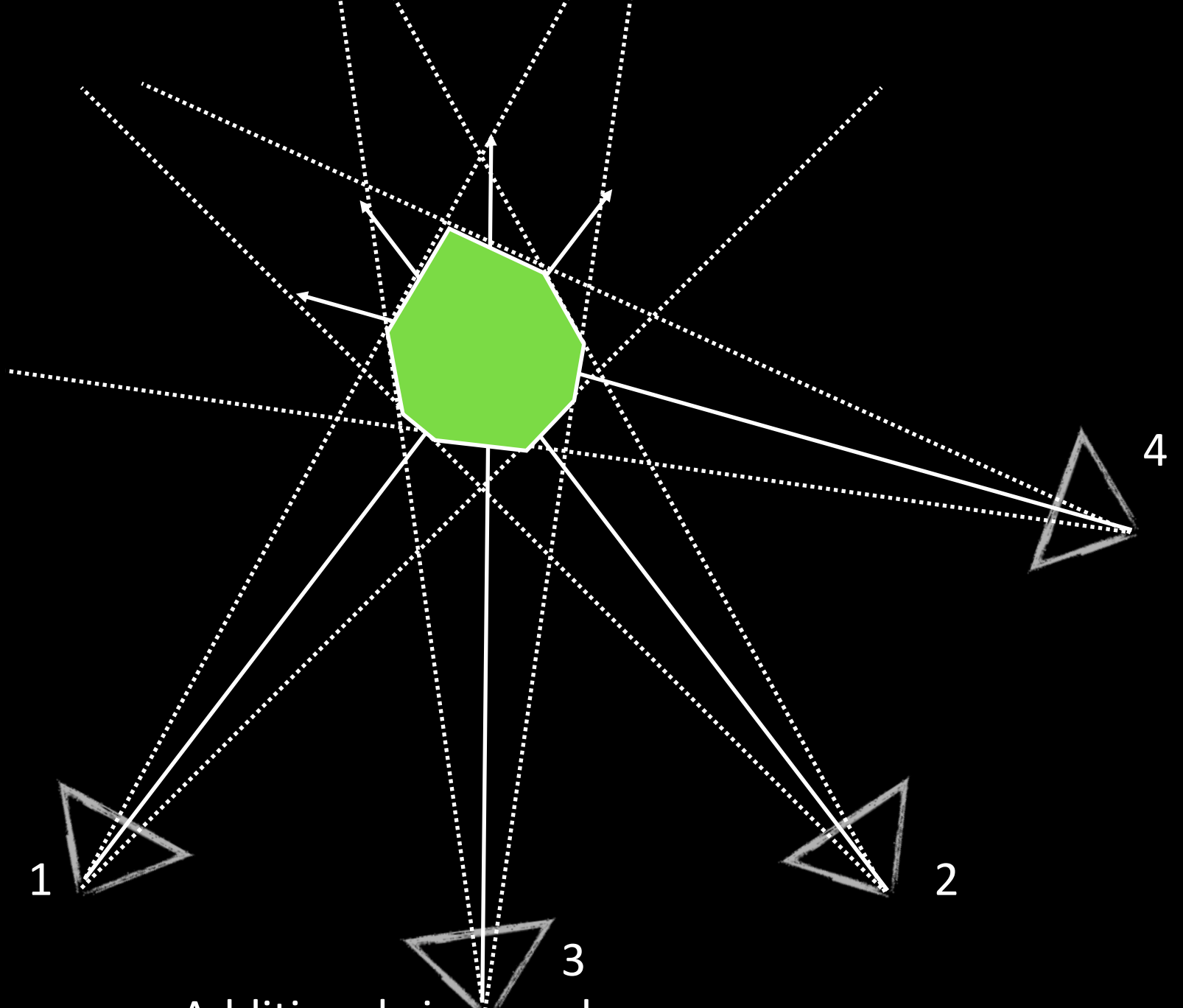
Estimated points contain some error.



Estimated points contain some error.



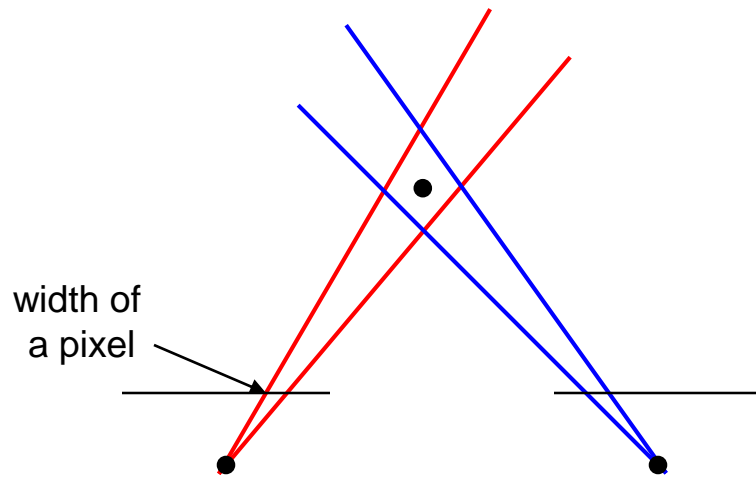
Estimated points contain some error.



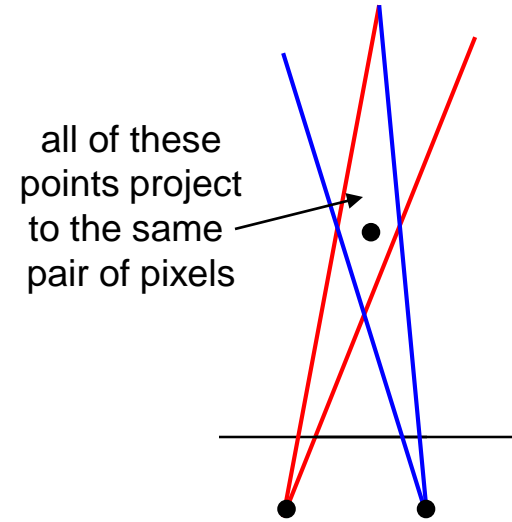
Additional views reduce error.



# Choosing the stereo baseline



**Large Baseline**



**Small Baseline**

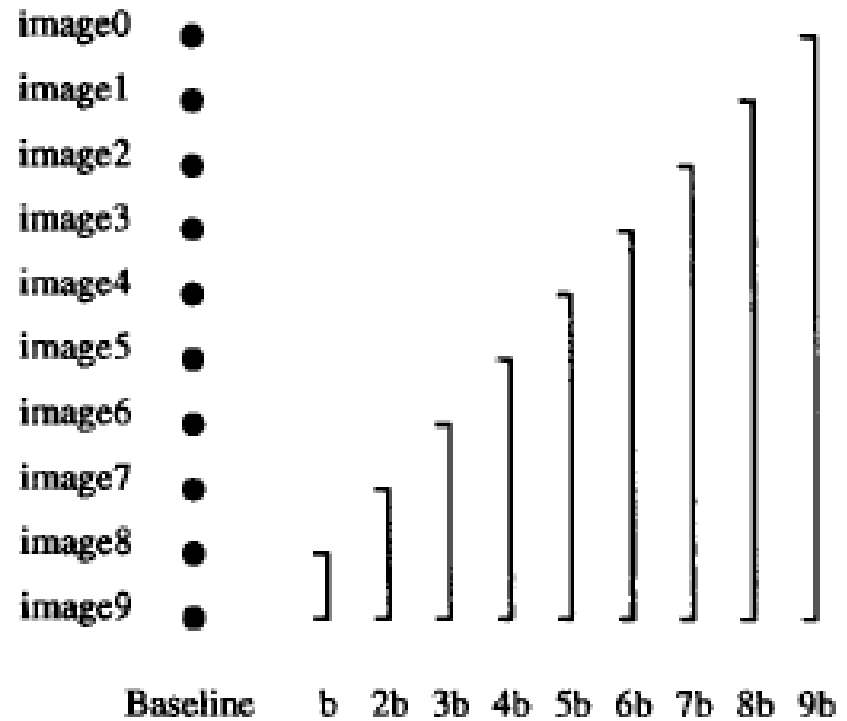
What's the optimal baseline?

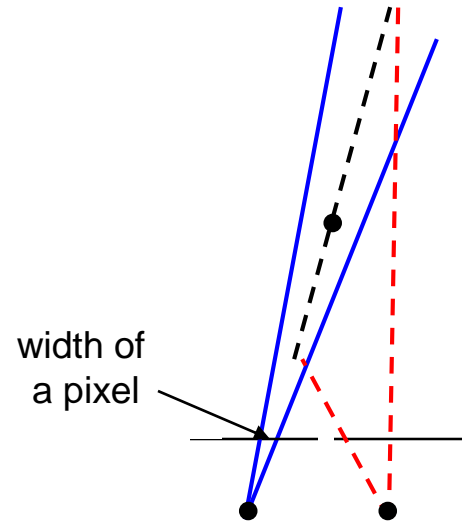
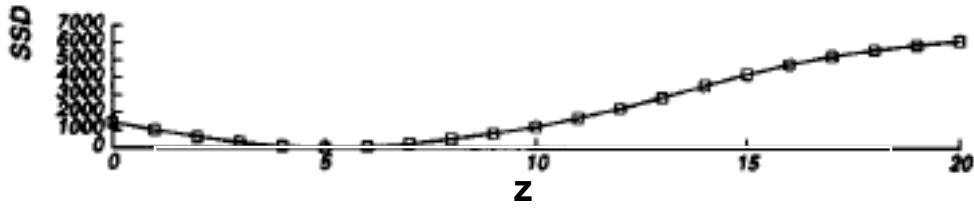
- Too small: large depth error
- Too large: difficult search problem

# The Effect of Baseline on Depth Estimation

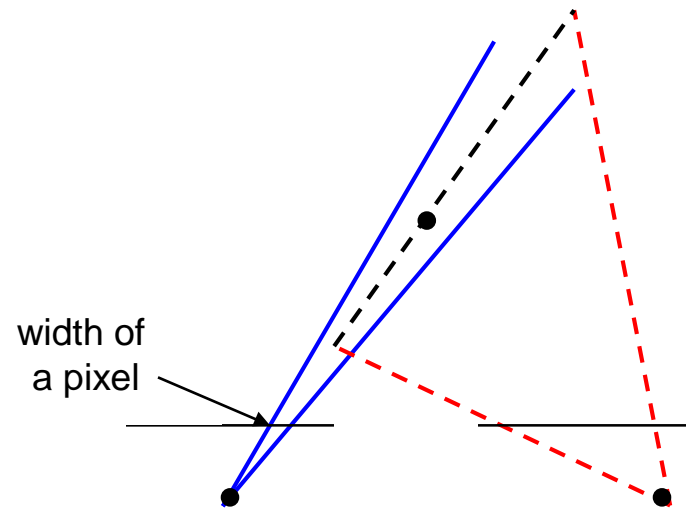
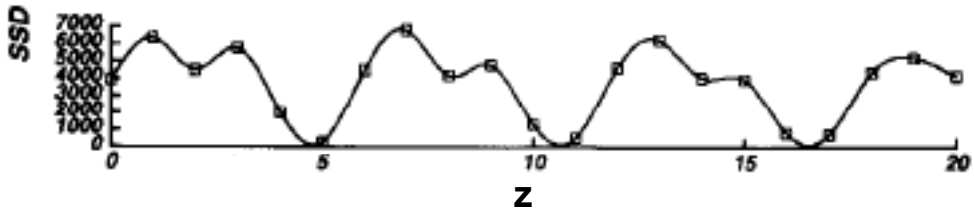


Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.





pixel matching score



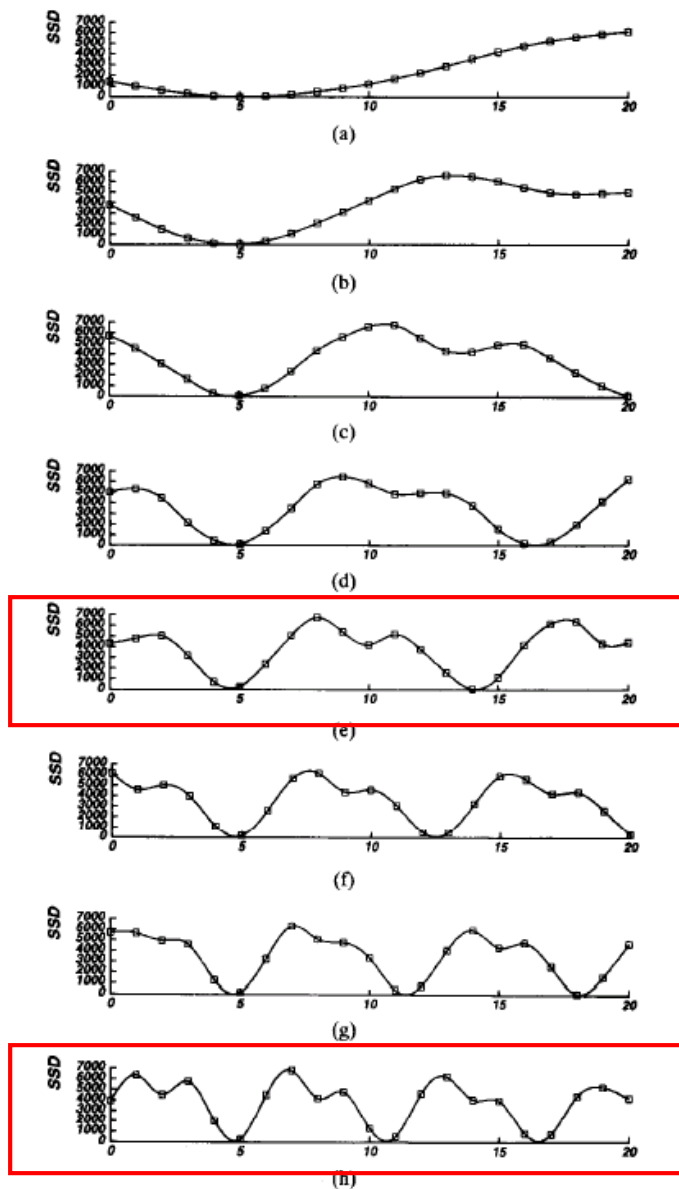


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

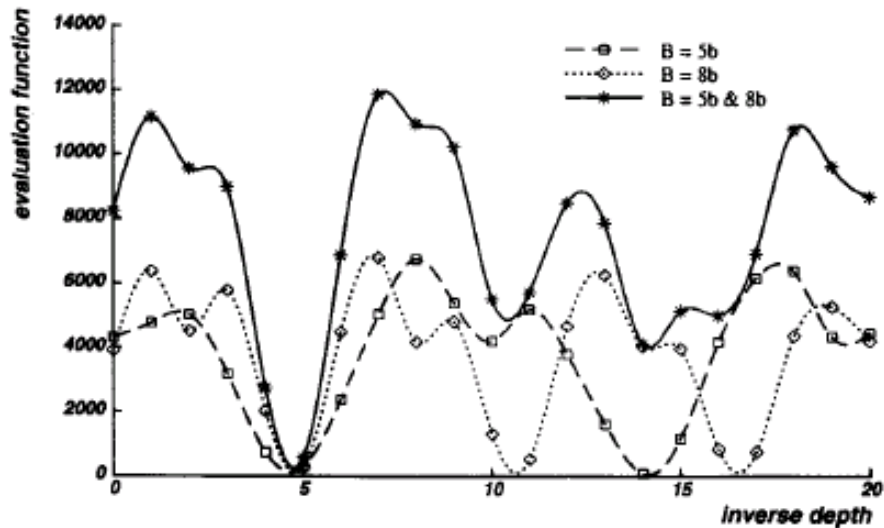


Fig. 6. Combining two stereo pairs with different baselines.

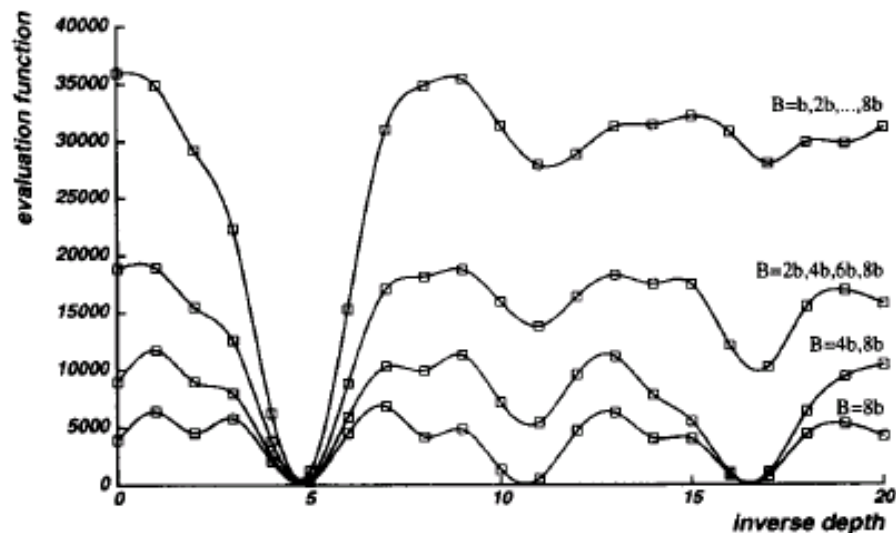


Fig. 7. Combining multiple baseline stereo pairs.

# Multibaseline Stereo

## Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - replace two-view SSD with SSSD over all baselines

## Limitations



# Problem: *visibility*

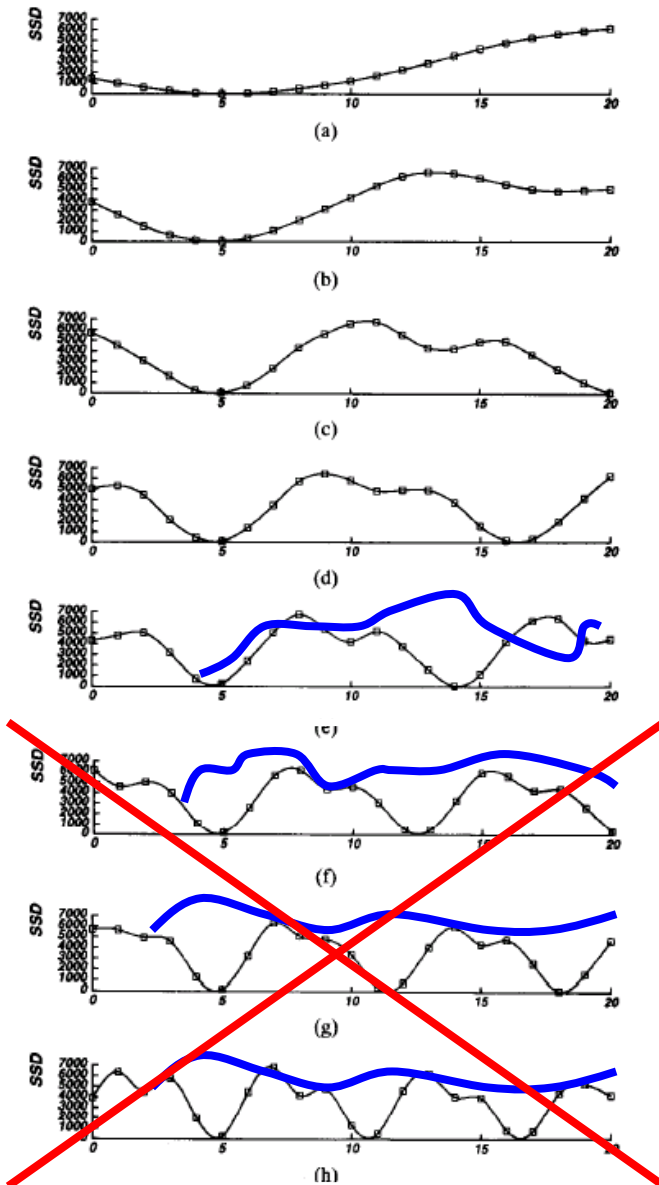


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

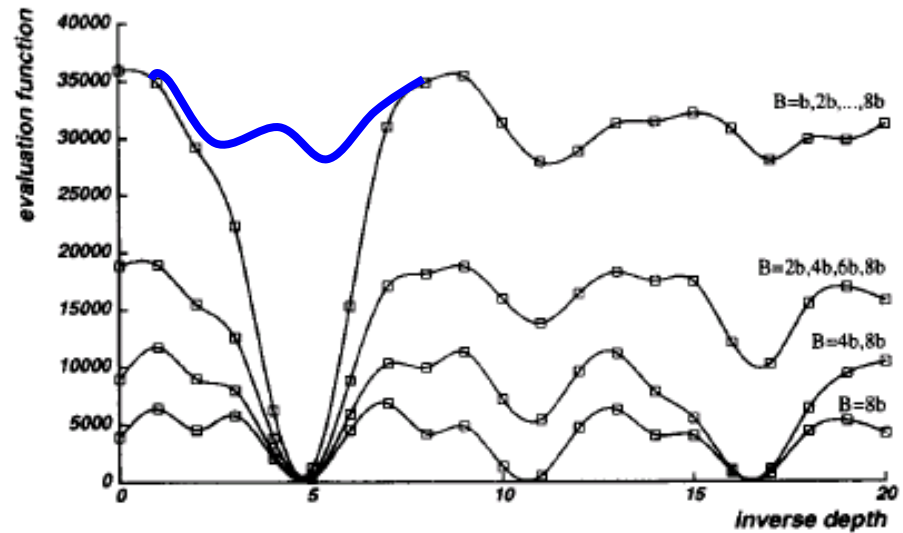


Fig. 7. Combining multiple baseline stereo pairs.

## Some Solutions

- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD, Ignore NCC values > threshold [Hernandez & Schmitt 03]

# Popular matching scores

- SSD (Sum Squared Distance)

$$\sum_{x,y} |W_1(x,y) - W_2(x,y)|^2$$

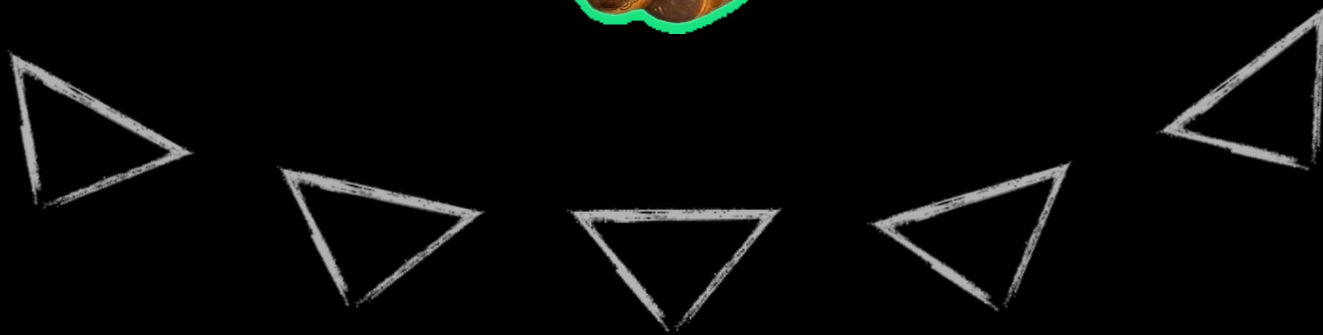
- NCC (Normalized Cross Correlation)

$$\frac{\sum_{x,y} (W_1(x,y) - \overline{W_1})(W_2(x,y) - \overline{W_2})}{\sigma_{W_1} \sigma_{W_2}}$$

– where  $\overline{W_i} = \frac{1}{n} \sum_{x,y} W_i$        $\sigma_{W_i} = \sqrt{\frac{1}{n} \sum_{x,y} (W_i - \overline{W_i})^2}$

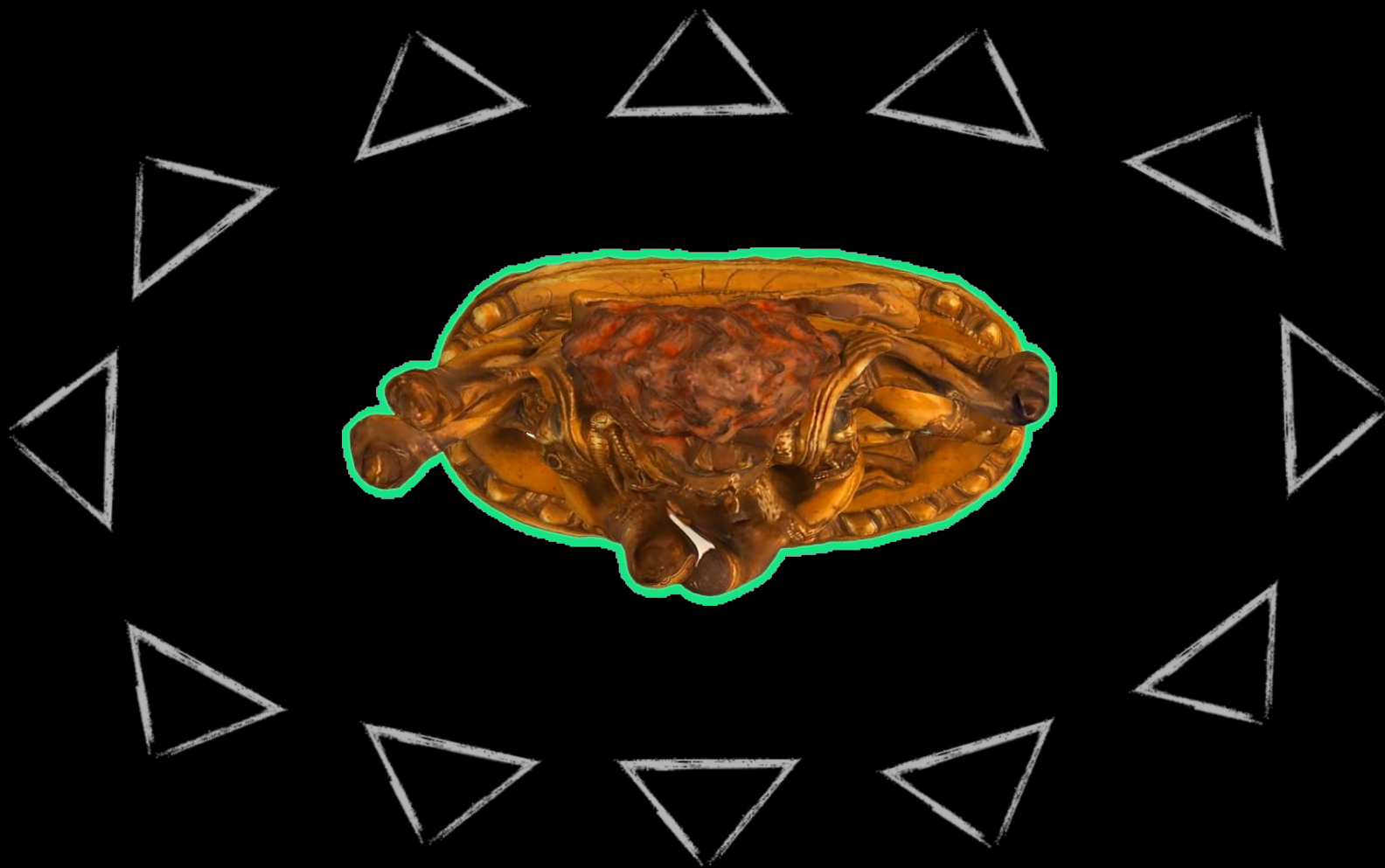
– what advantages might NCC have?

Single depth map often isn't  
enough

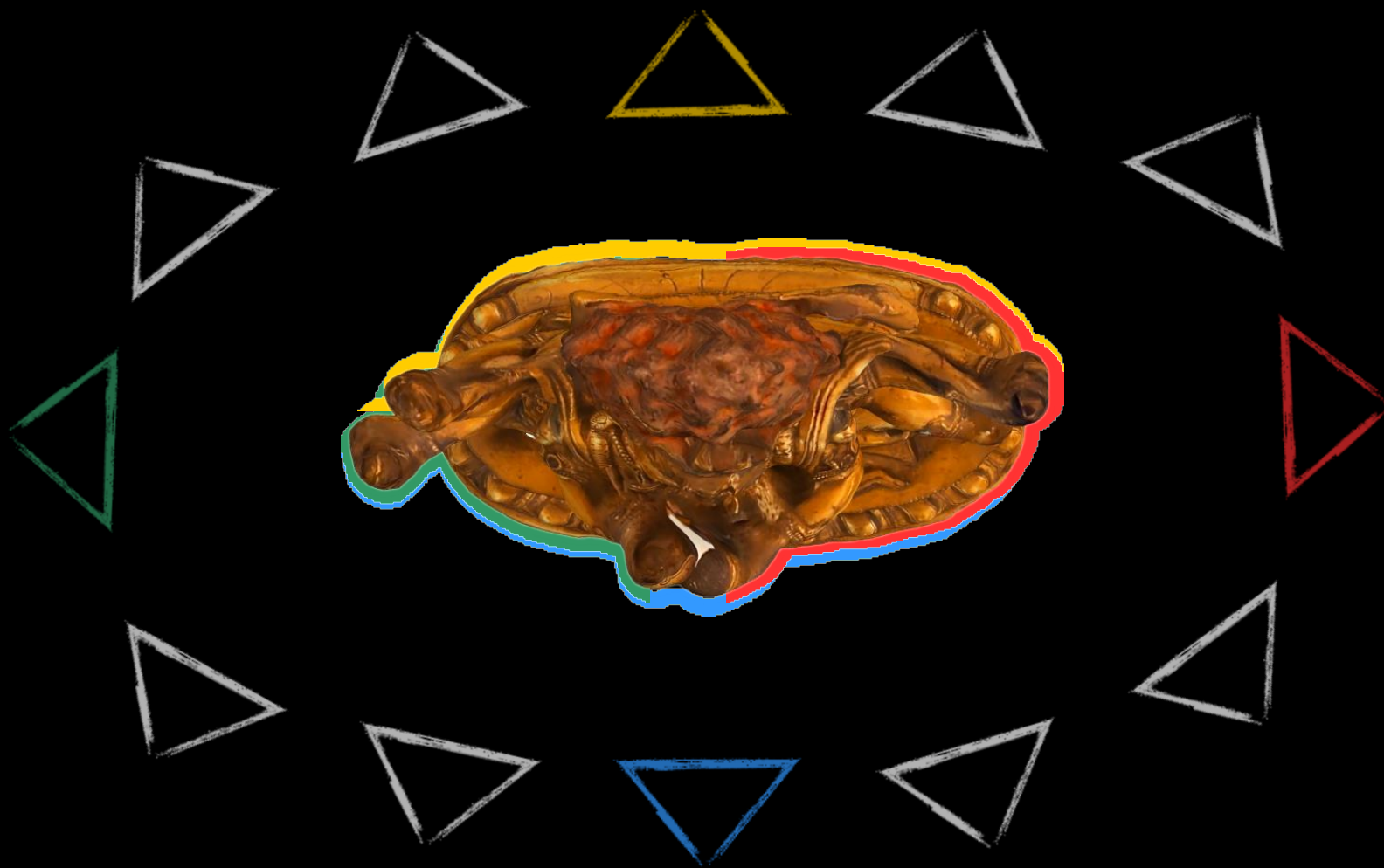




Really want full coverage

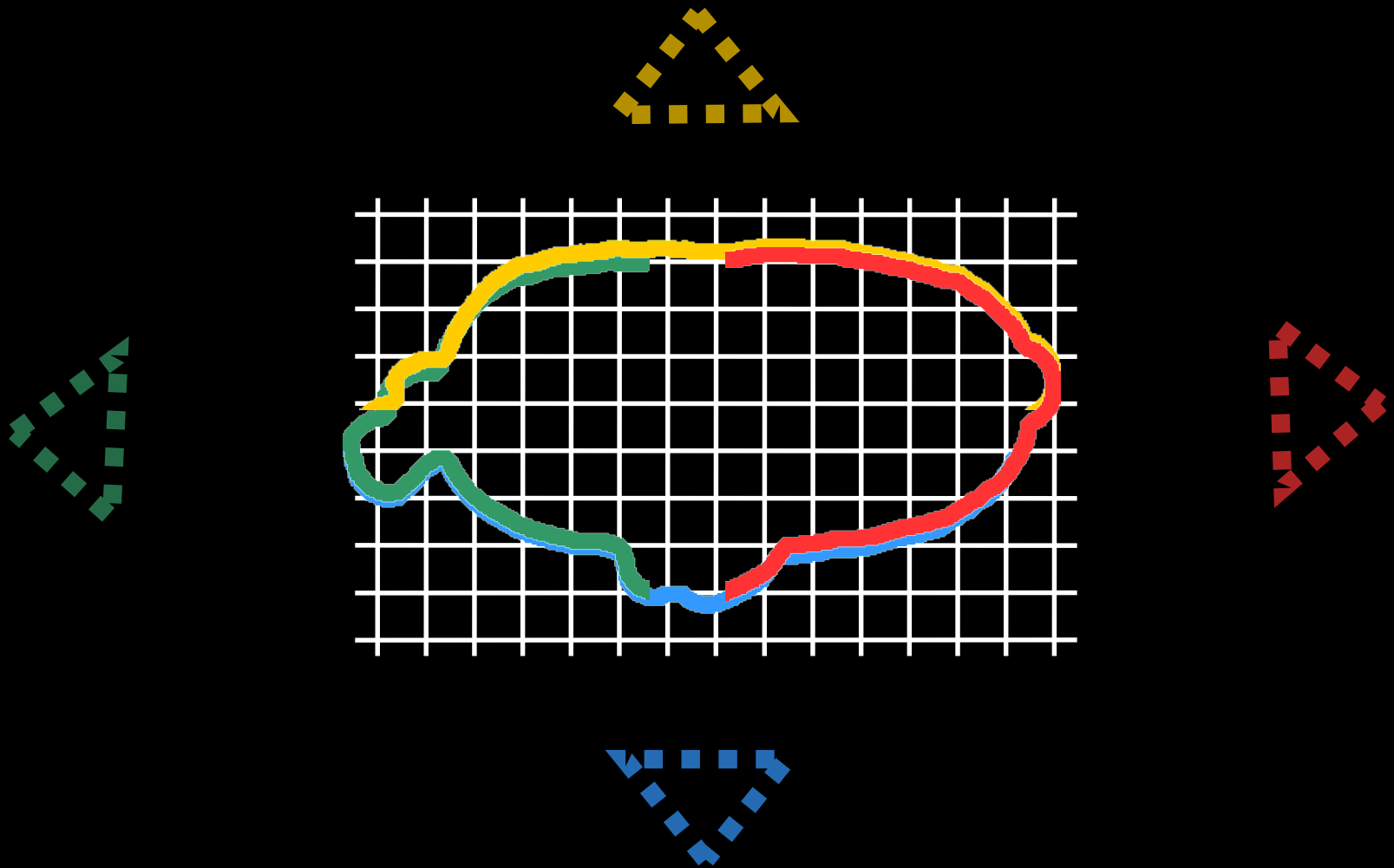


# Idea: Combine many depth maps



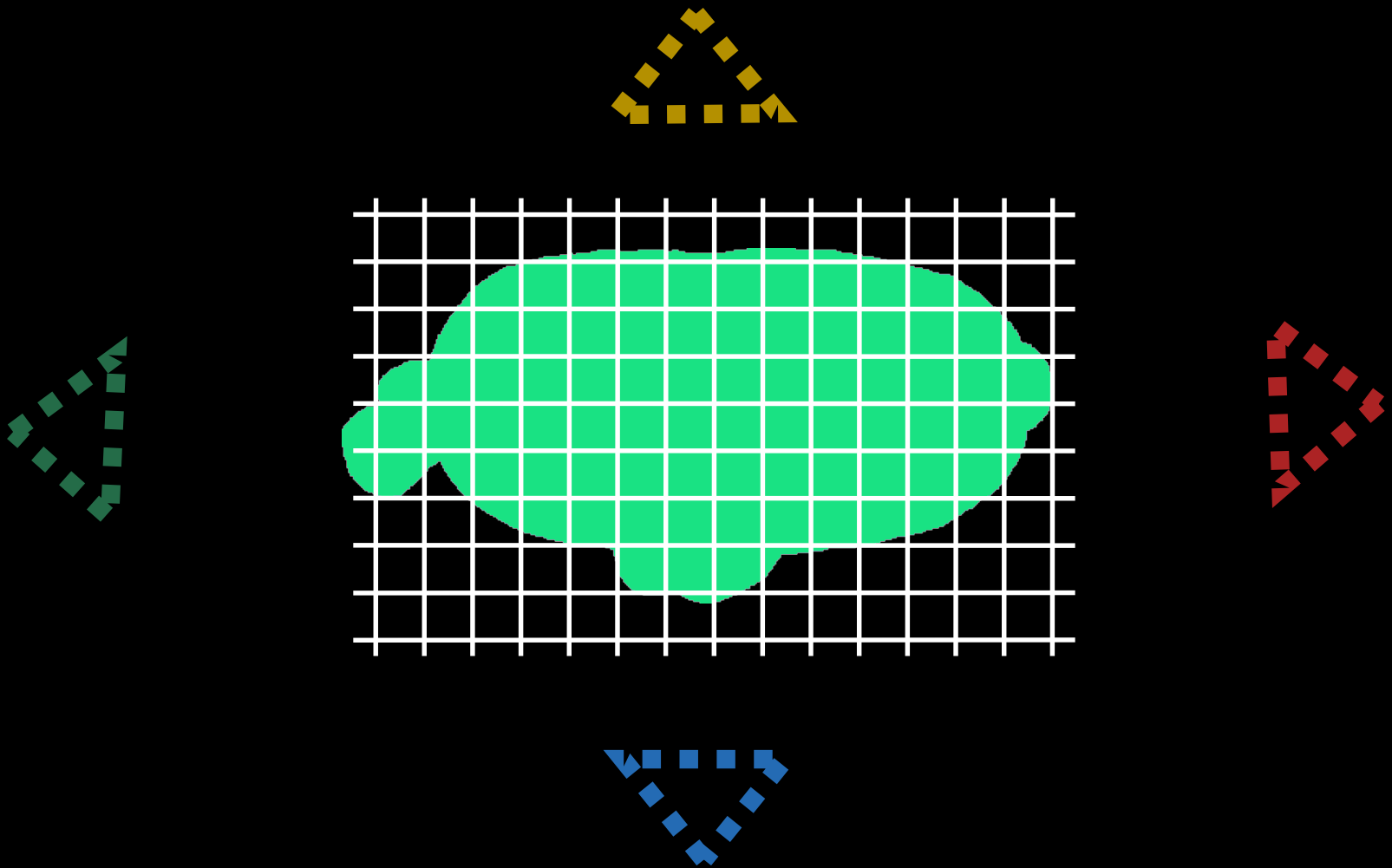
Many depth maps, each with error. How can we fuse these?

# Volumetric fusion



A common world-space coordinate system.

# Volumetric fusion

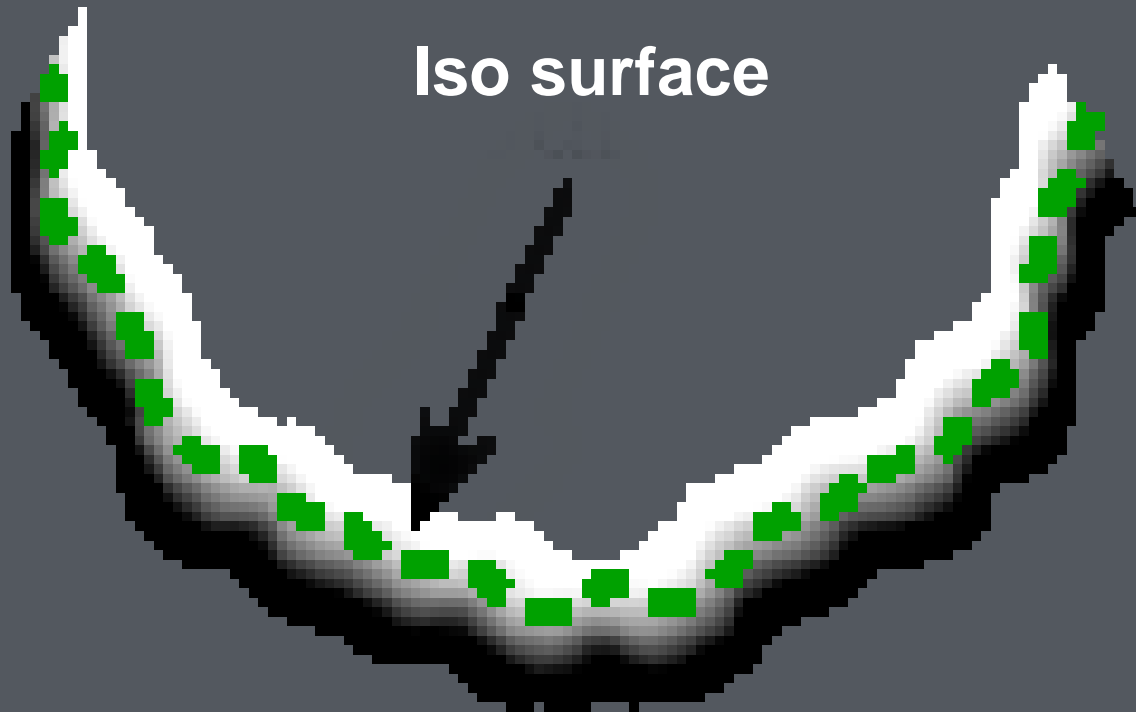


A common world-space coordinate system.





Iso surface



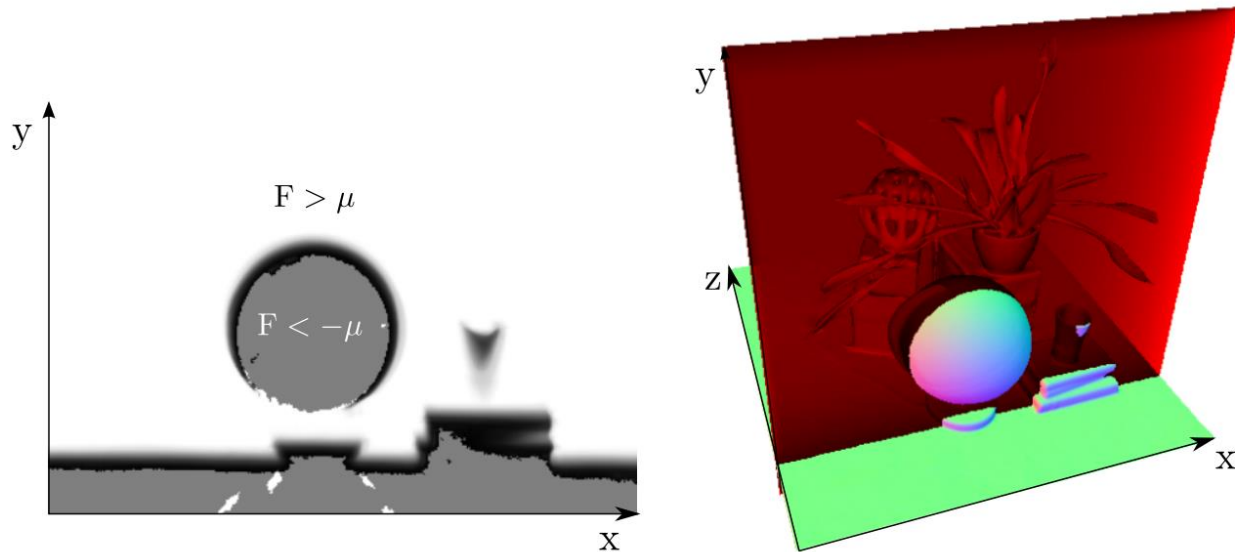
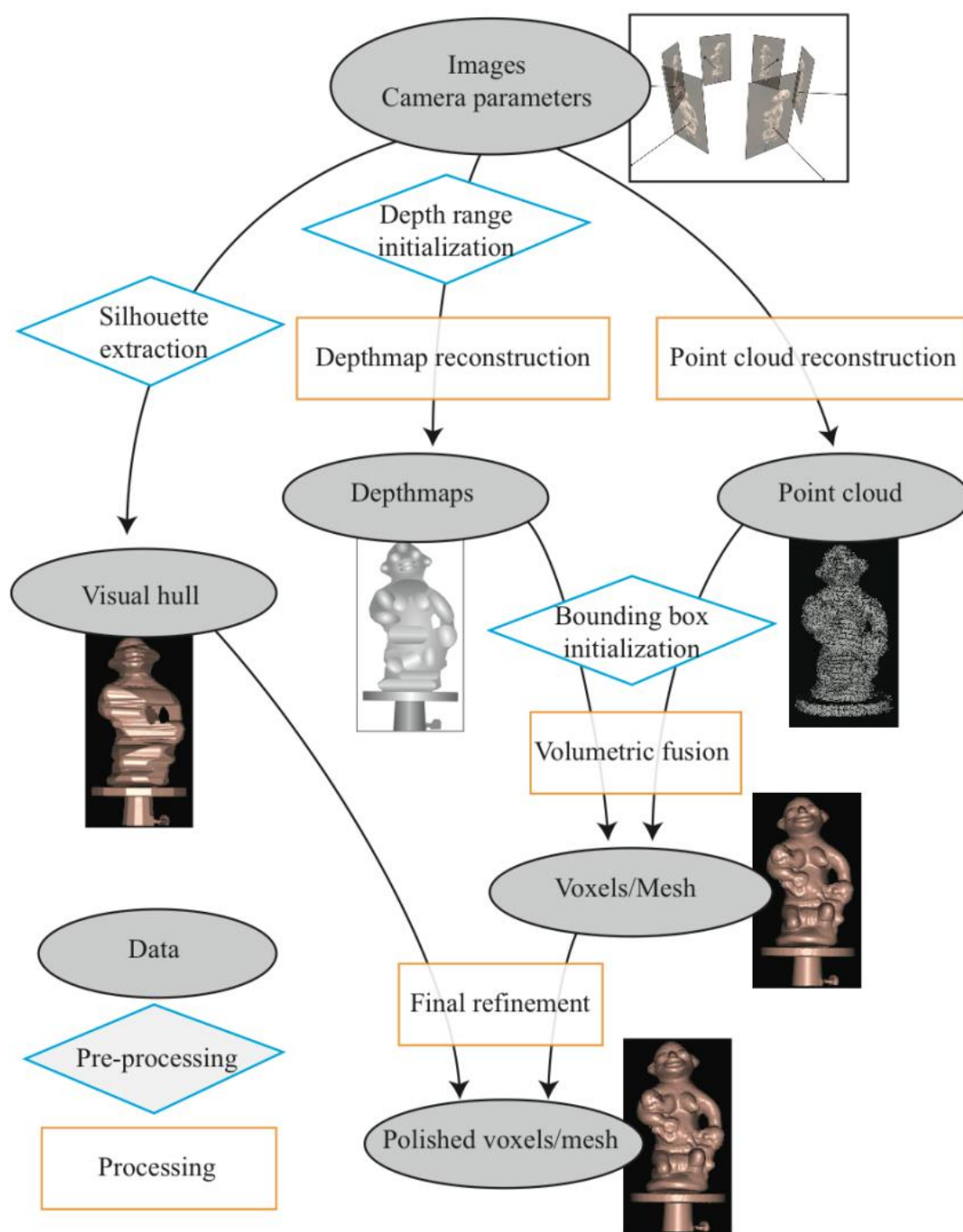
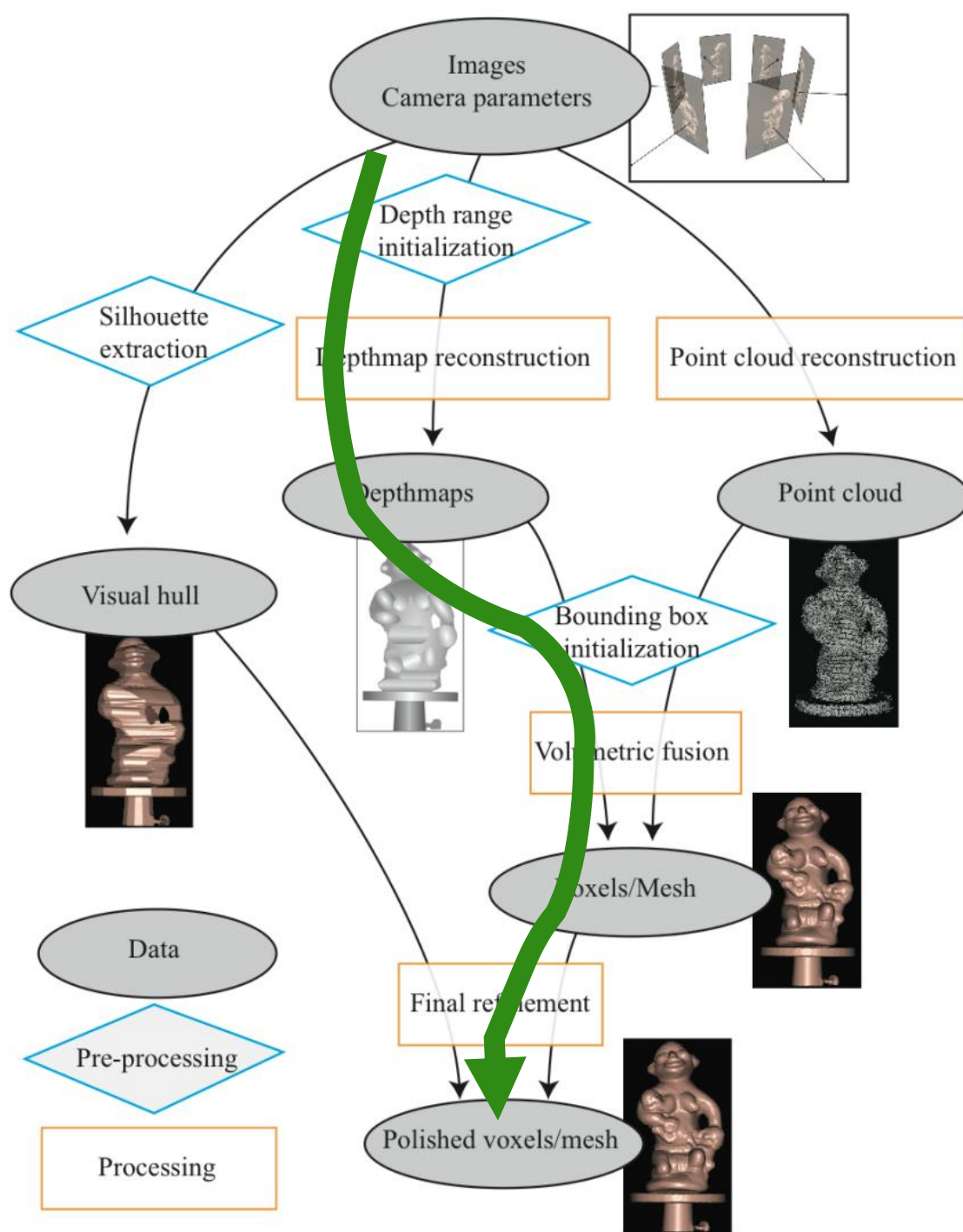


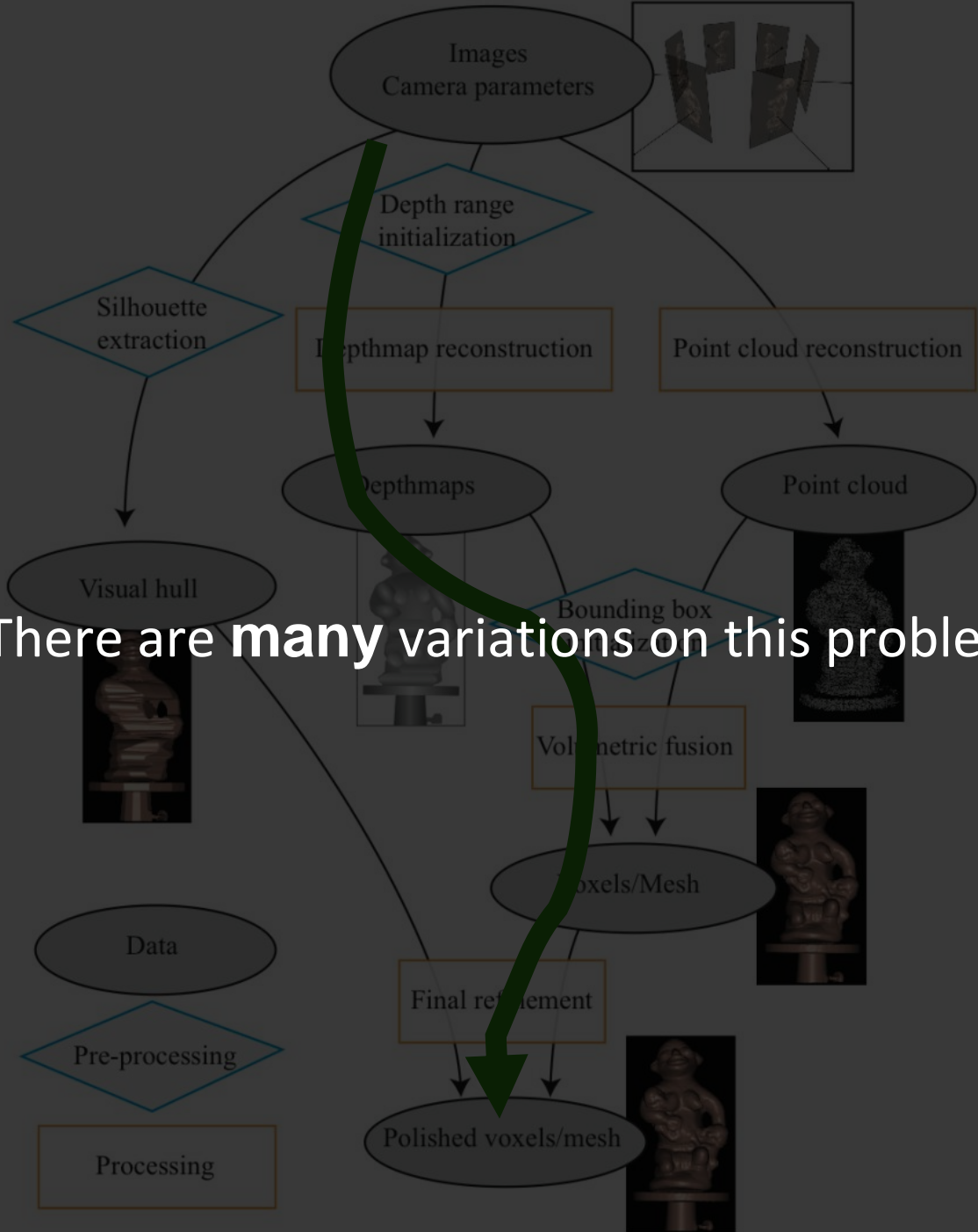
Figure 4: A slice through the truncated signed distance volume showing the truncated function  $F > \mu$  (white), the smooth distance field around the surface interface  $F = 0$  and voxels that have not yet had a valid measurement (grey) as detailed in eqn. 9.





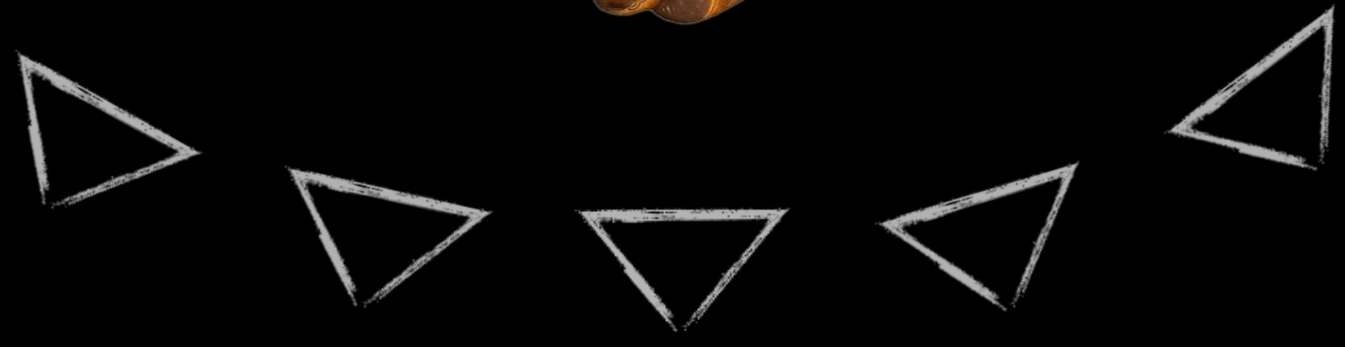


There are **many** variations on this problem.

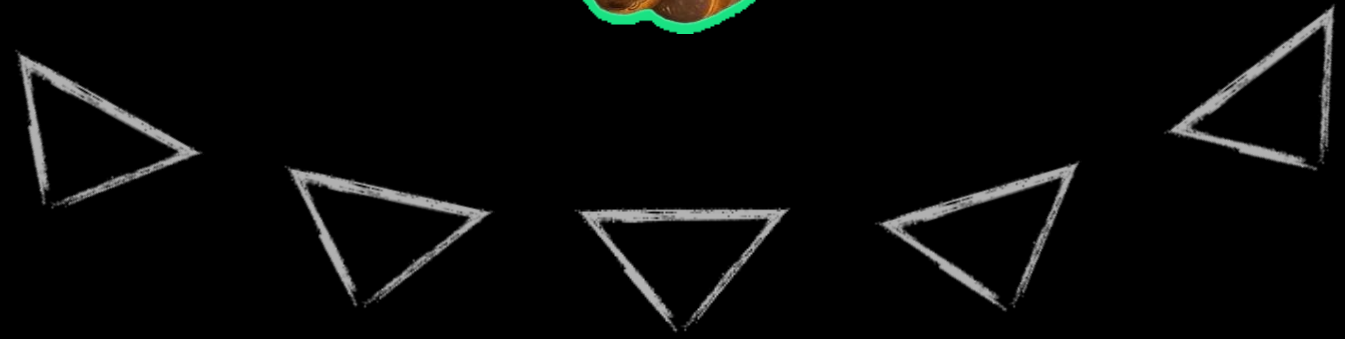


Questions?

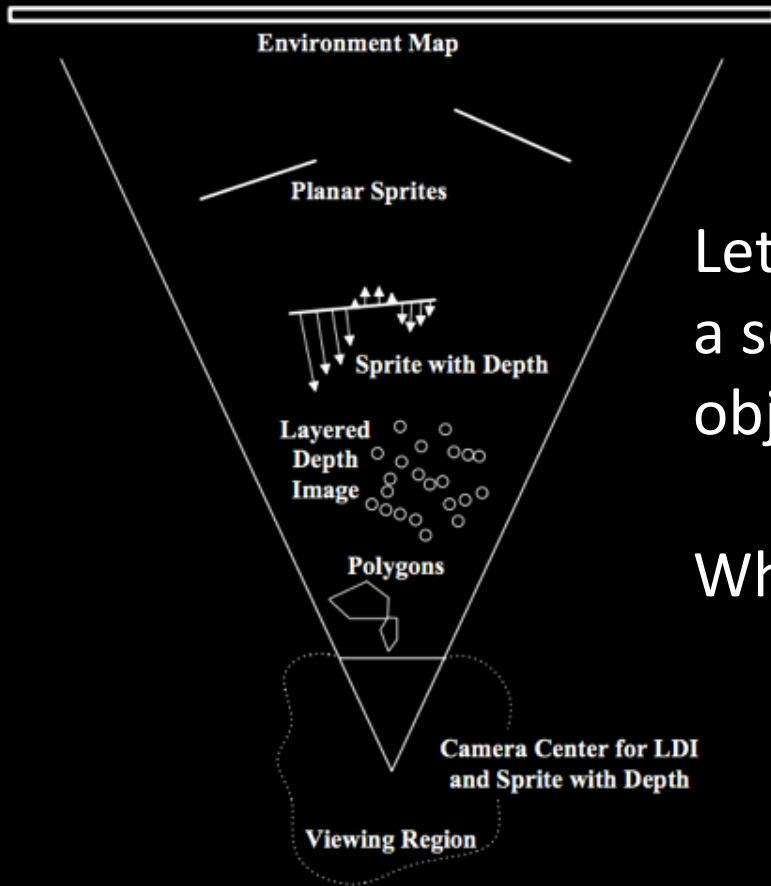
# Are depth maps enough?



# Are depth maps enough?



# Depends on your application...

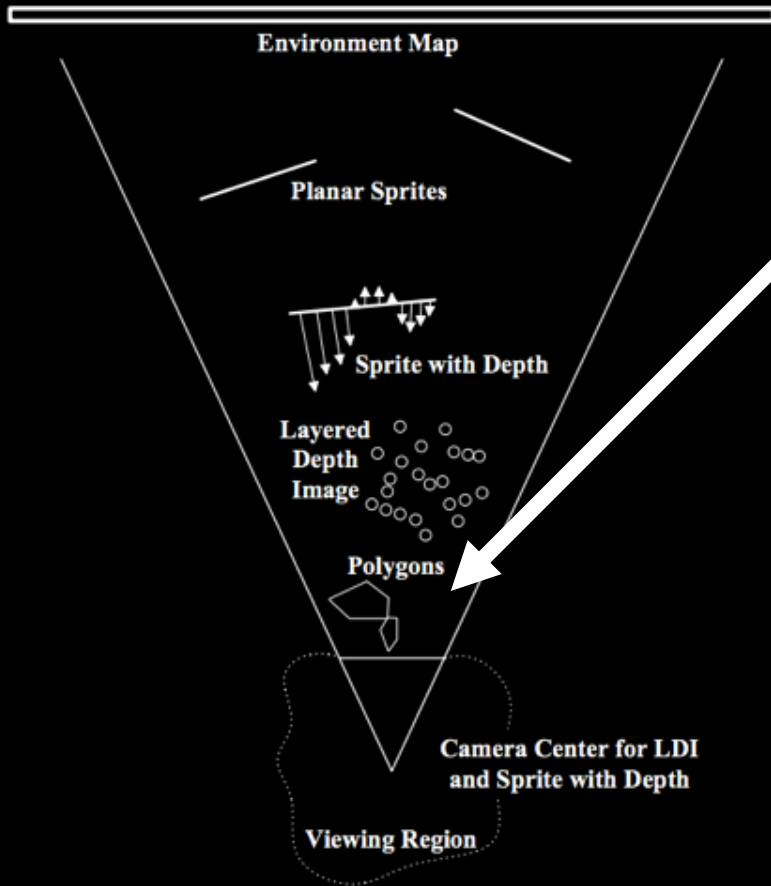


Let's assume you want to render a scene containing your real-world object.

What should you capture?

**Figure 1** Different image based primitives can serve well depending on distance from the camera

# Depends on your application...

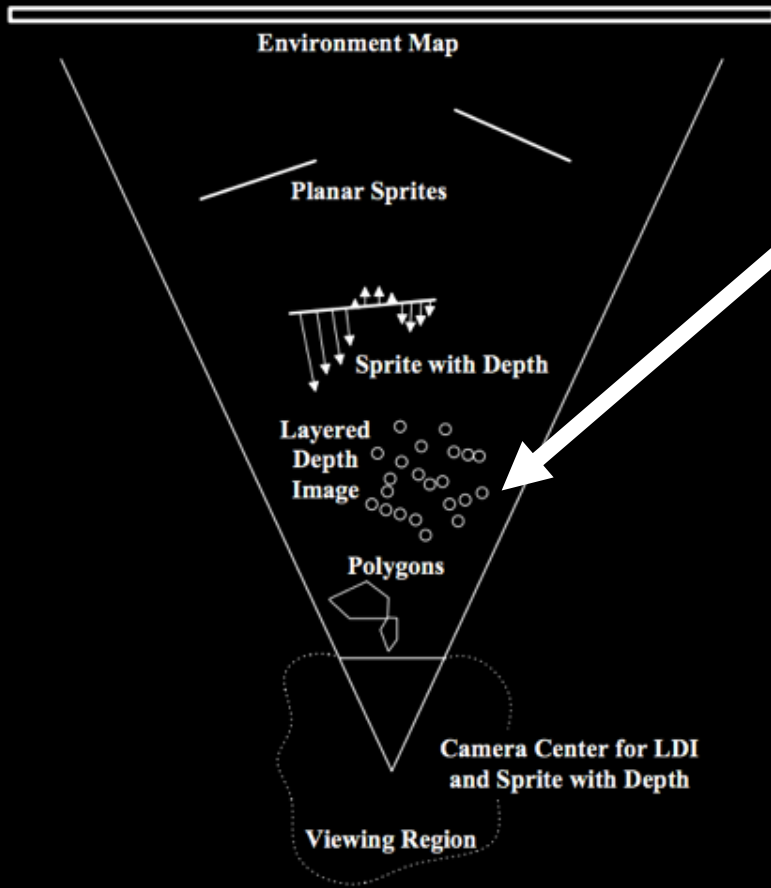


The object is right in front of you and you want to look all around it.

**Figure 1** Different image based primitives can serve well depending on distance from the camera



# Depends on your application...



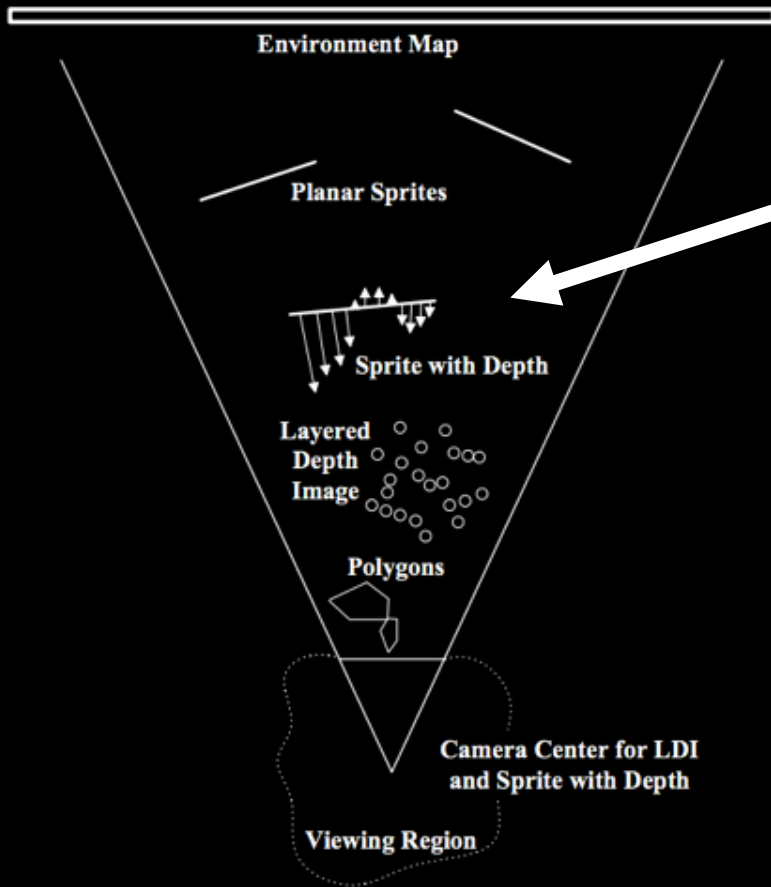
Obvious dis-occlusions if a single depth map is used.

**Figure 1** Different image based primitives can serve well depending on distance from the camera



Dis-occlusion →

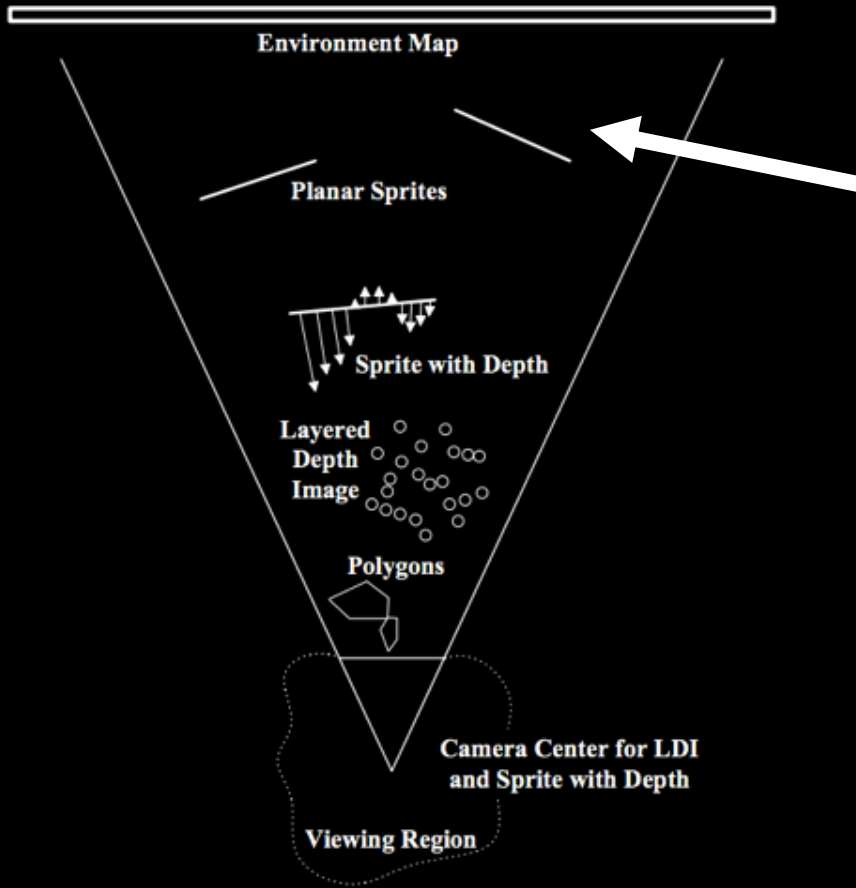
# Depends on your application...



Close enough that you can tell it shouldn't be flat, but **dis-occlusions** are minimal.

Figure 1 Different image based primitives can serve well depending on distance from the camera

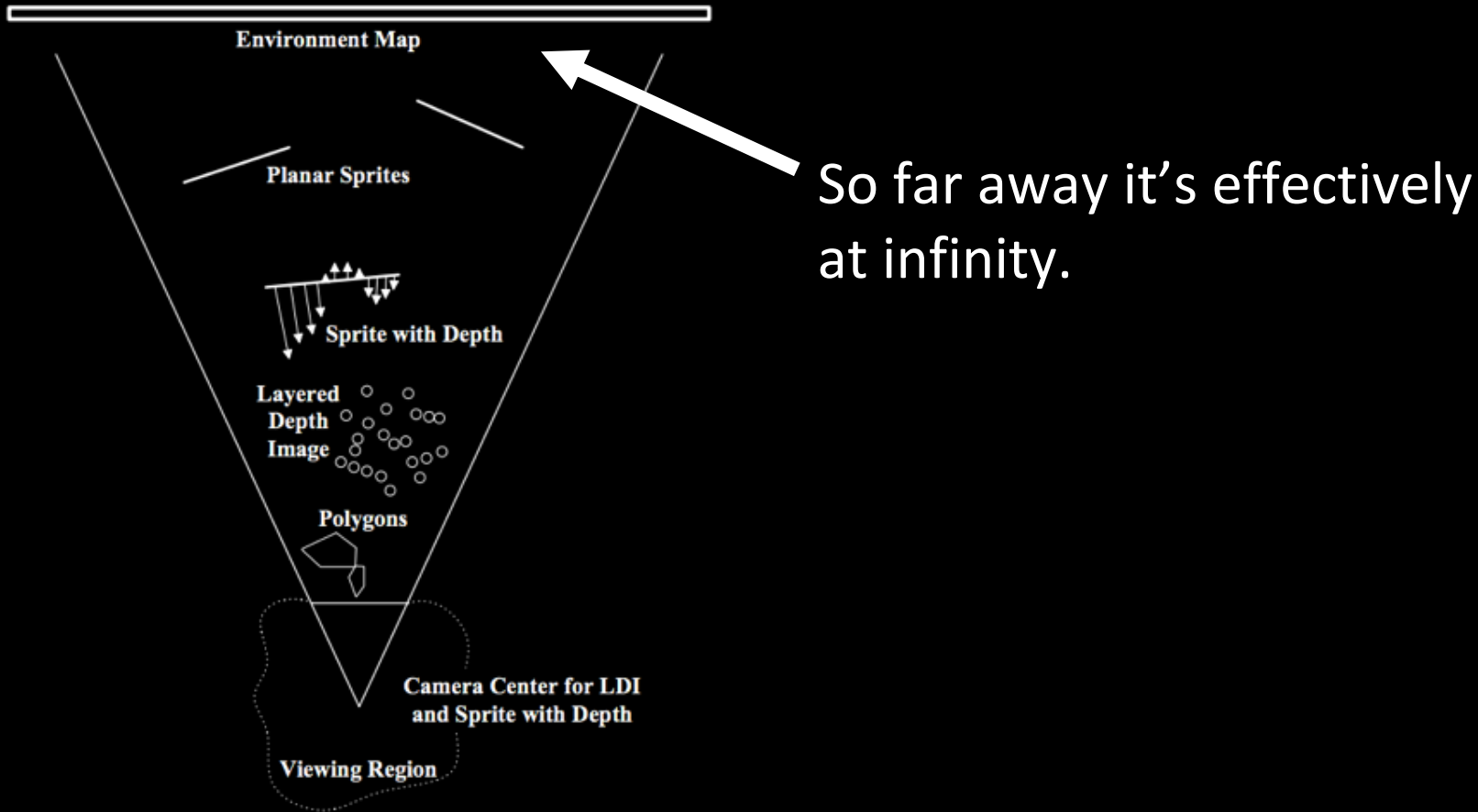
# Depends on your application...



Far enough away that a plane can approximate it.

**Figure 1** Different image based primitives can serve well depending on distance from the camera

# Depends on your application...

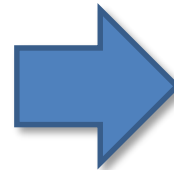
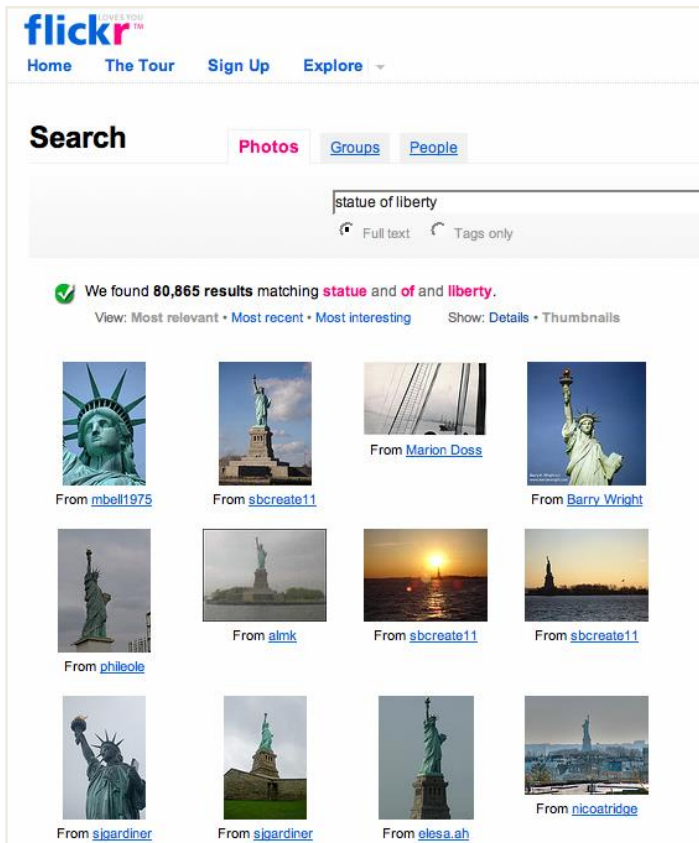


**Figure 1** Different image based primitives can serve well depending on distance from the camera

Questions?

# Multi-view stereo from Internet Collections

[\[Goesele, Snavely, Curless, Hoppe, Seitz, ICCV 2007\]](#)



# Challenges

- appearance variation



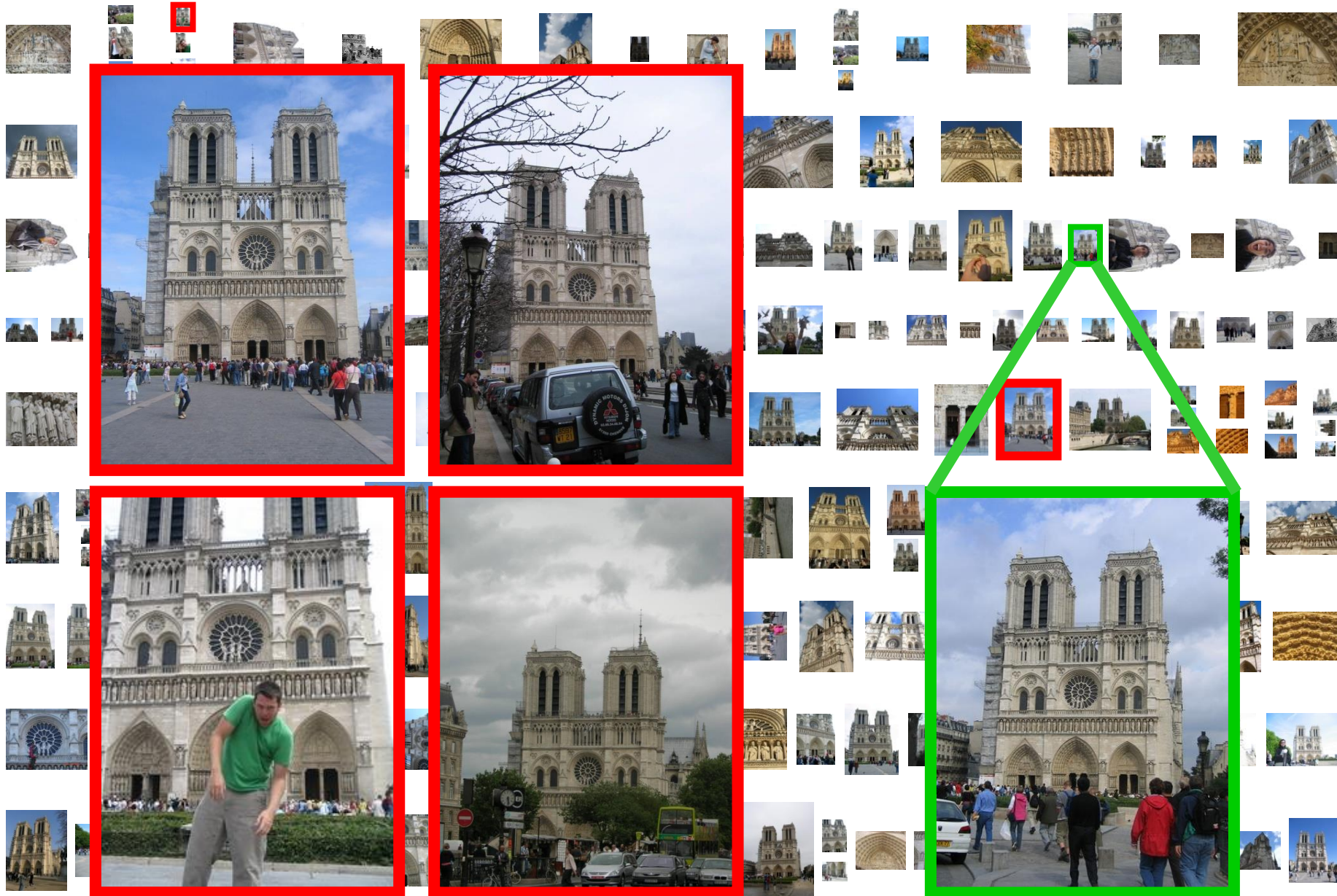
- resolution



- massive collections

82,754 results for photos matching **notre** and **dame** and **paris**.





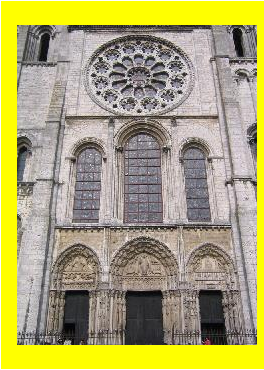


4 best neighboring views



reference view

- Automatically select neighboring views for each point in the image
- Desiderata: good matches AND good baselines

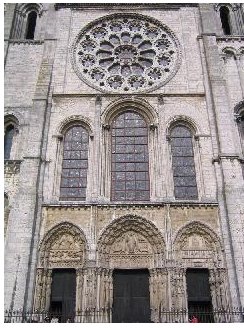


4 best neighboring views



reference view

- Automatically select neighboring views for each point in the image
- Desiderata: good matches AND good baselines



4 best neighboring views

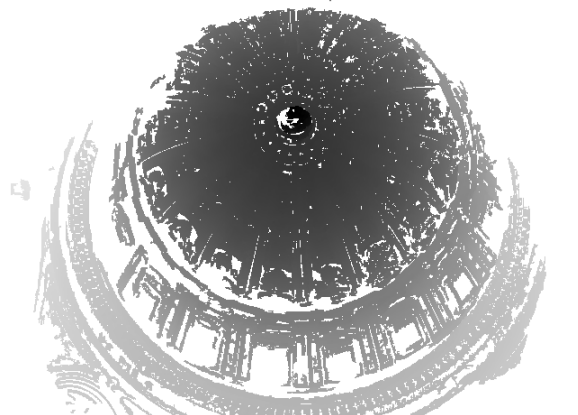
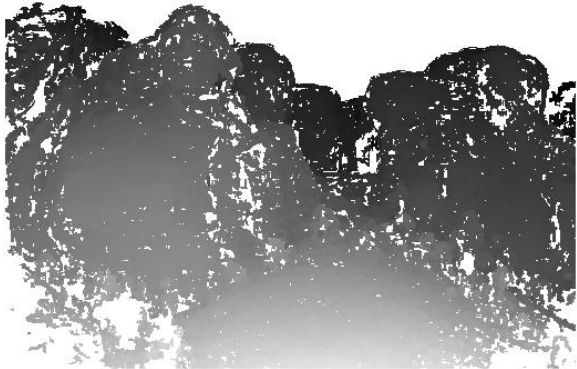


reference view

## Local view selection

- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines

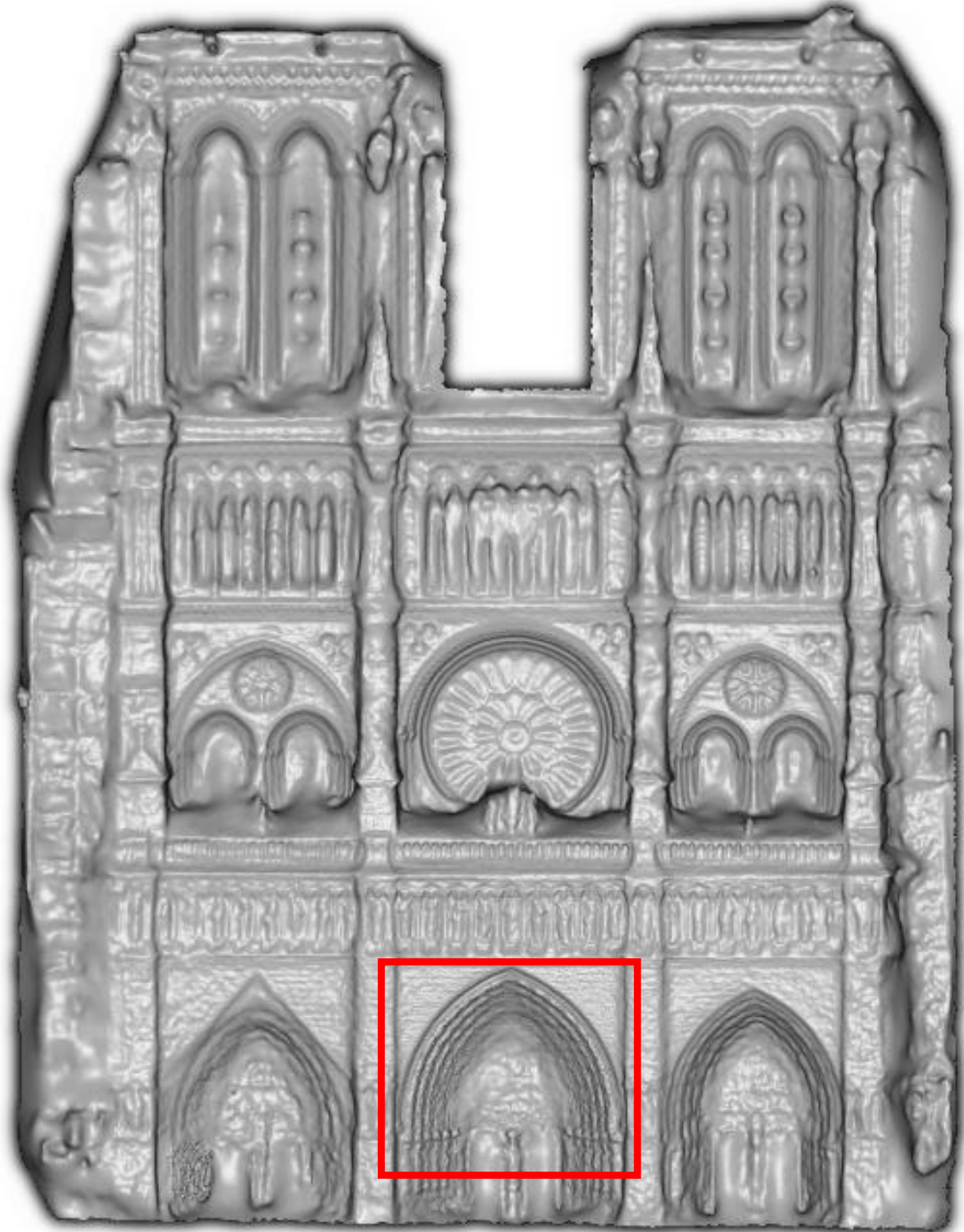
# Results

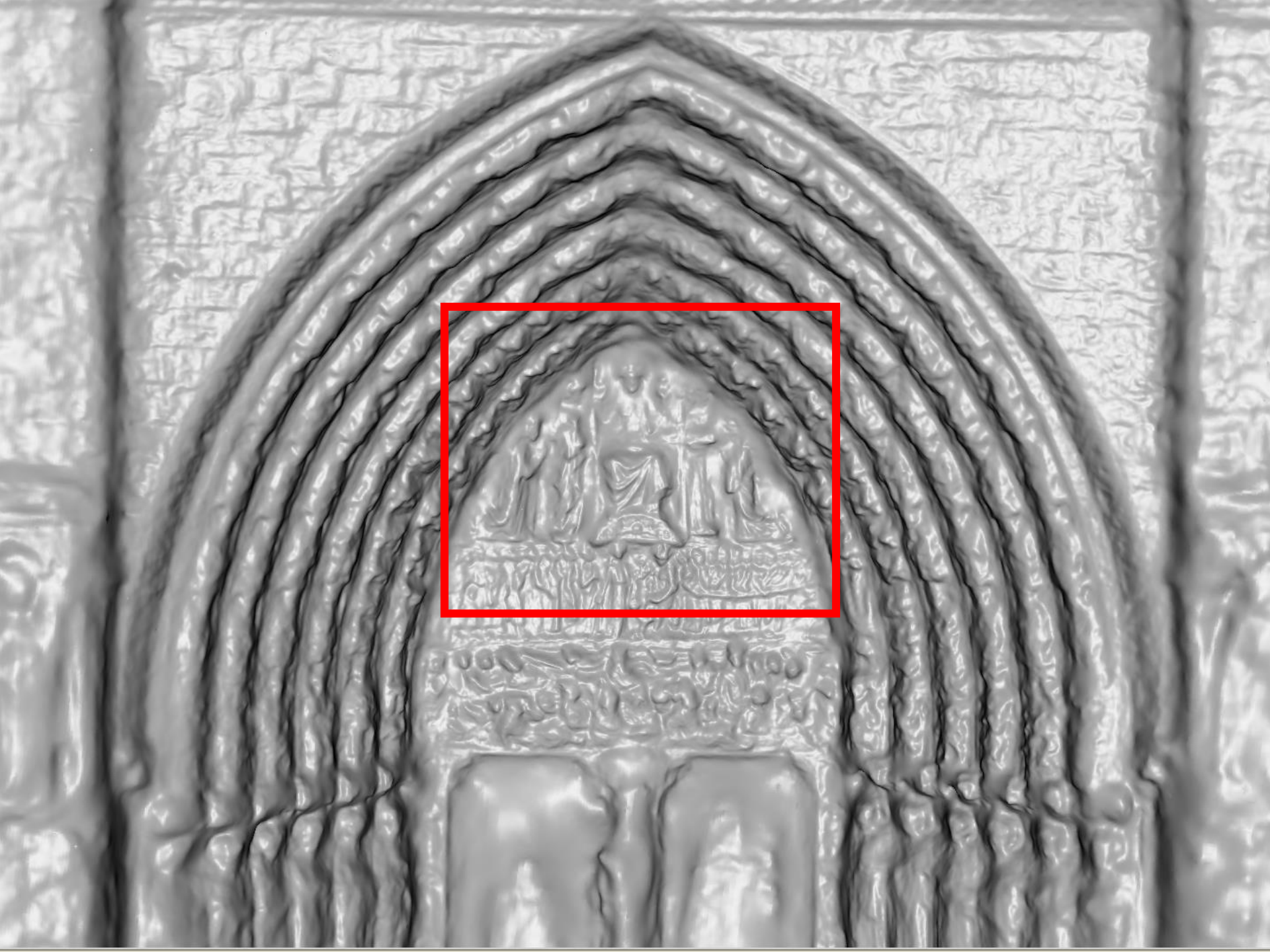


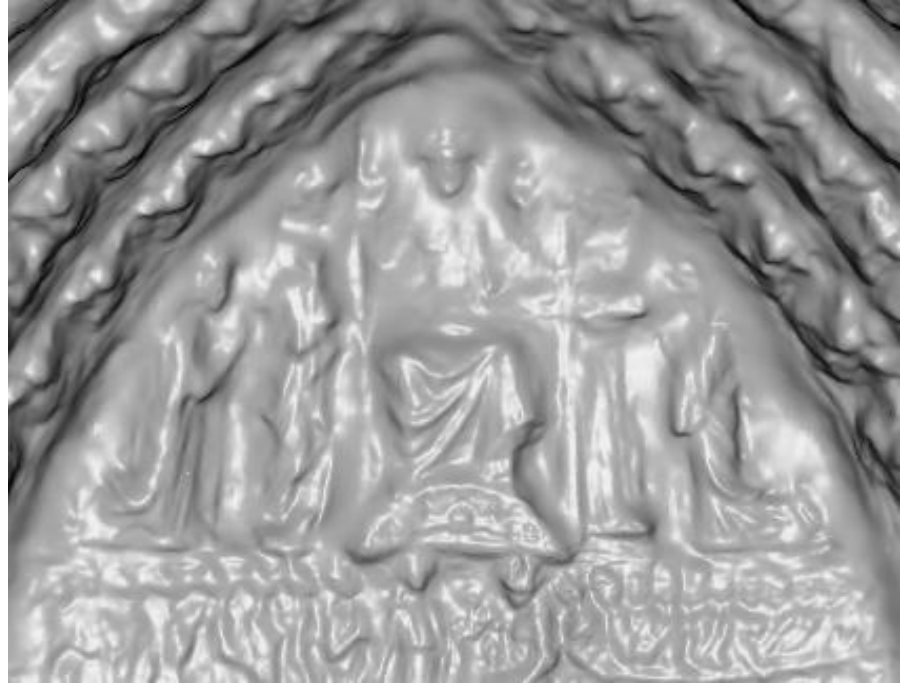
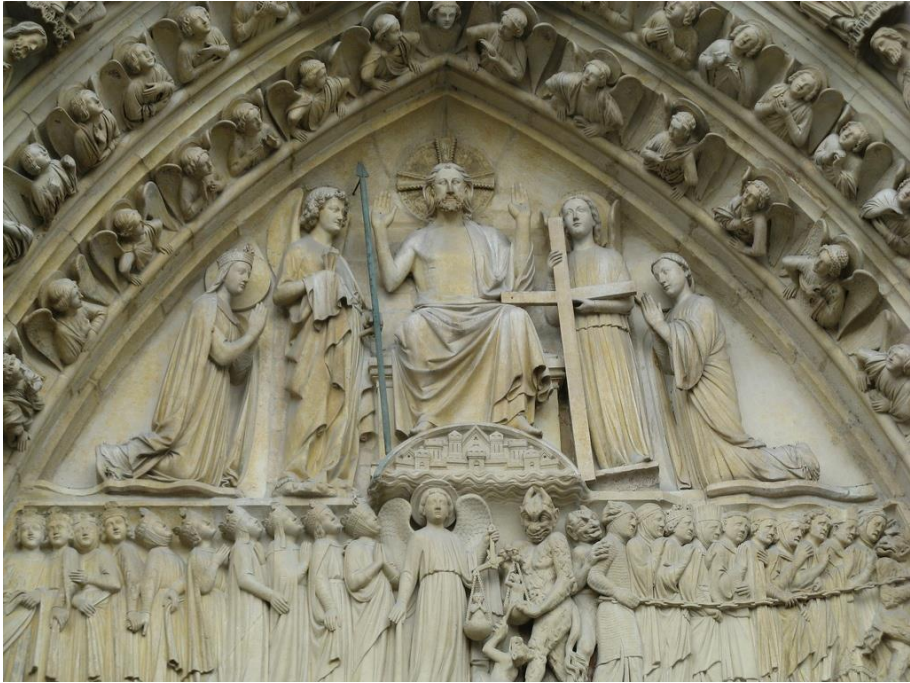
Notre Dame de Paris

653 images

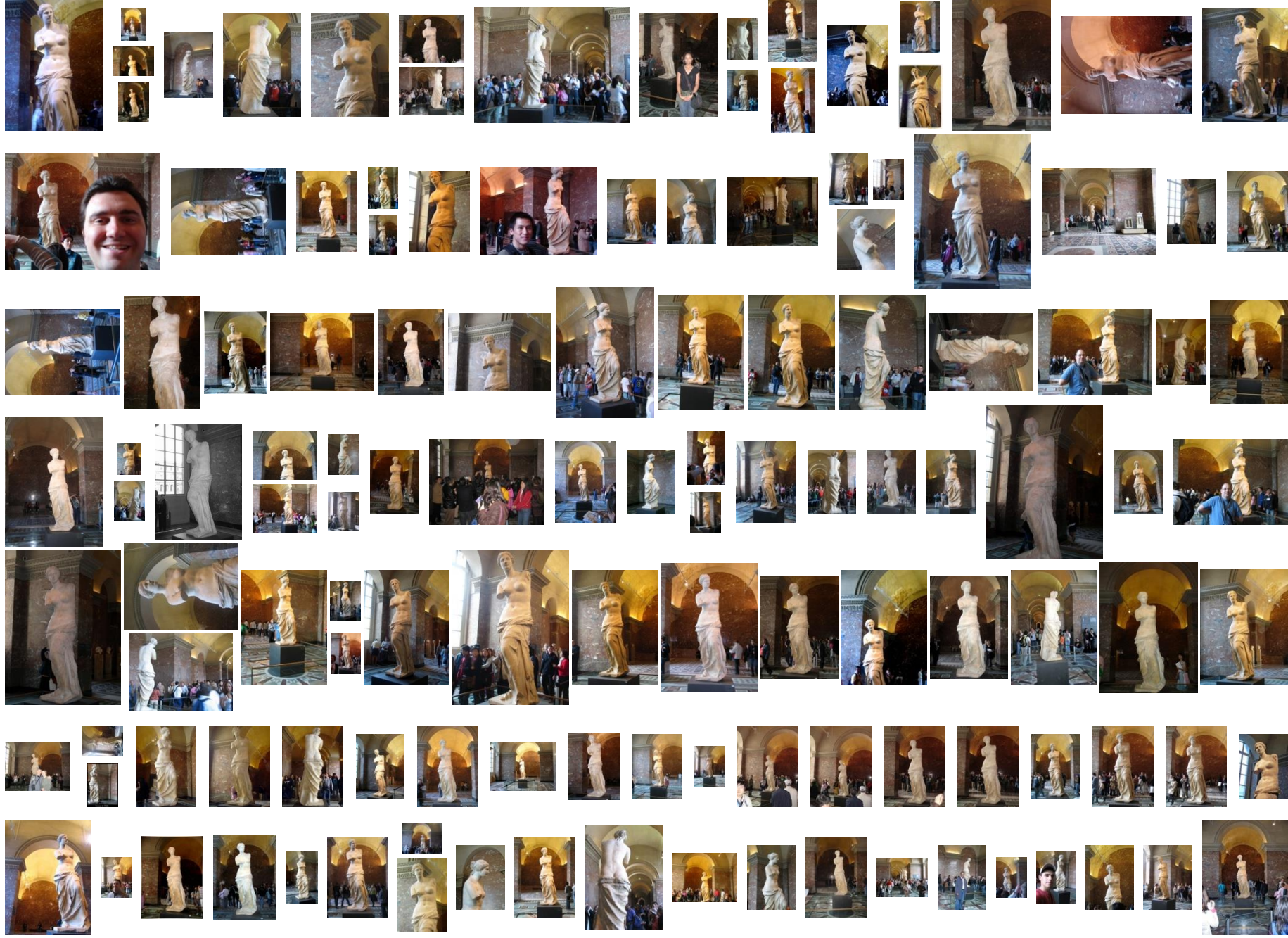
313 photographers





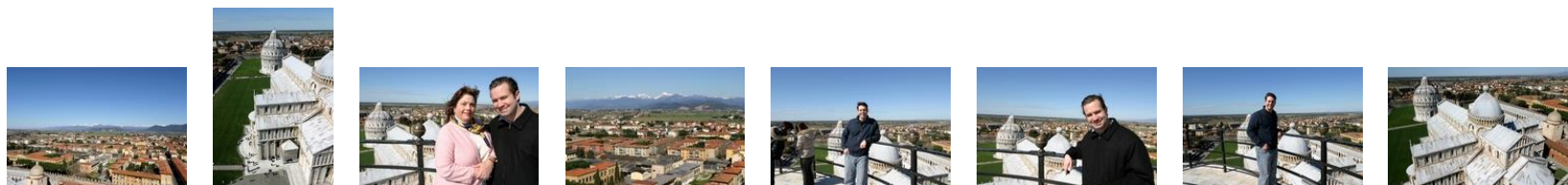
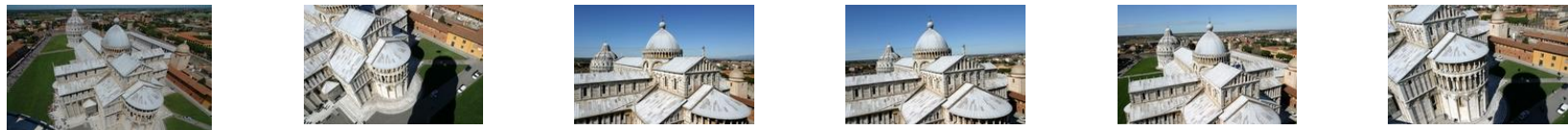


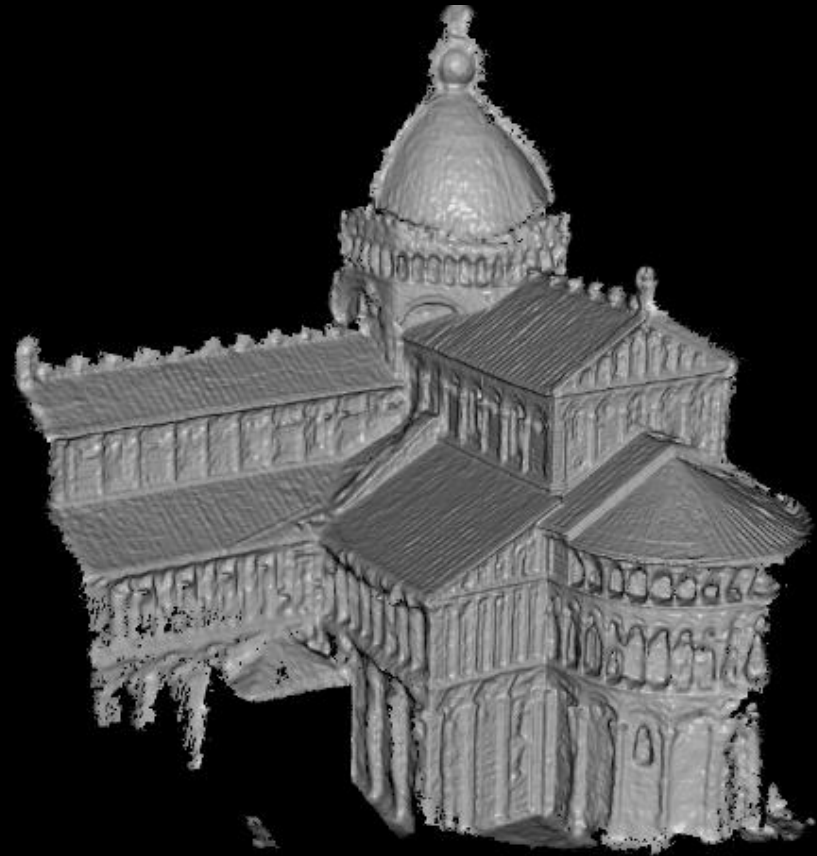




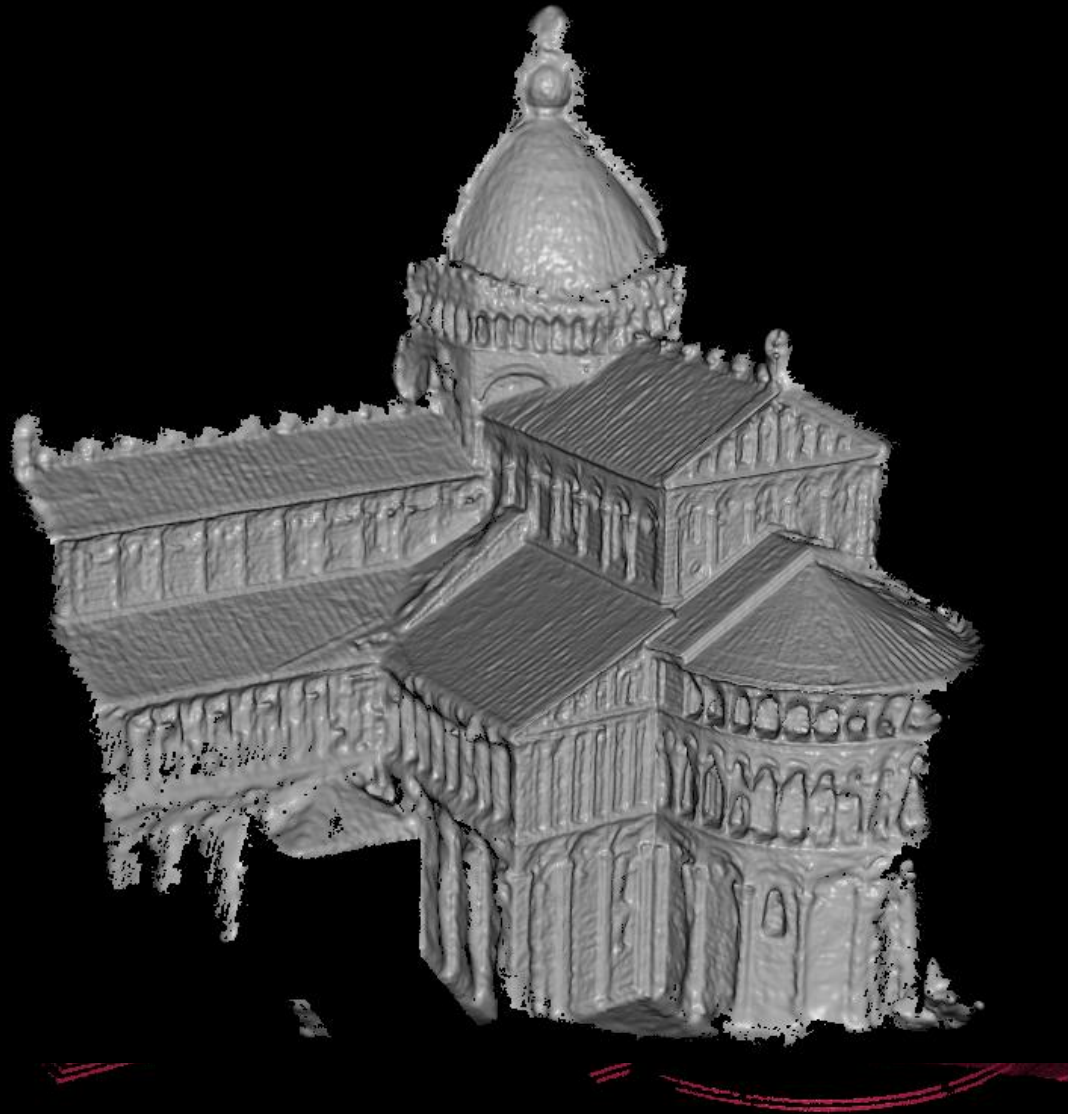


merged model of Venus de Milo





merged model of Pisa Cathedral



Accuracy compared to laser scanned model:  
90% of points within 0.25% of ground truth