Antialiasing

CS5625 Lecture 12

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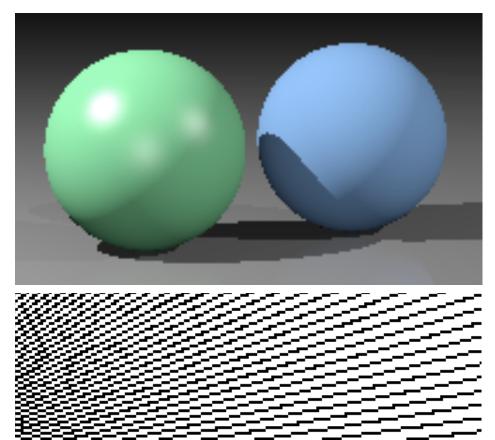
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Aliasing

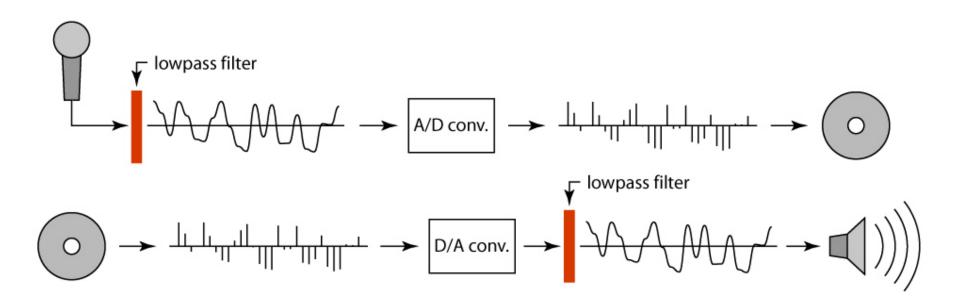
point sampling a continuous image:

continuous image defined by ray tracing procedure

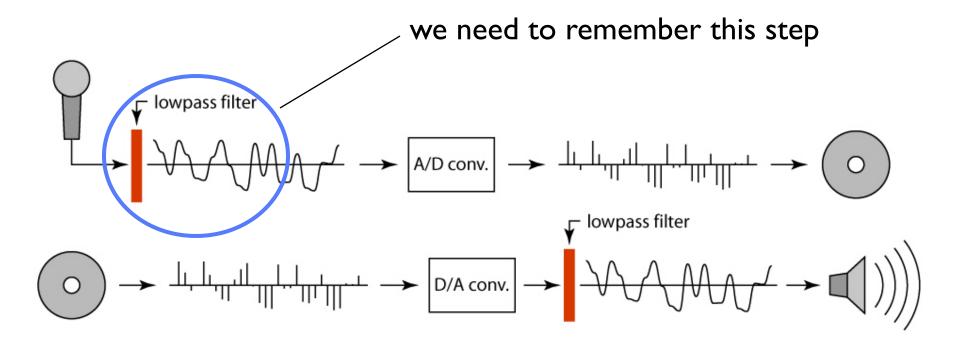
continuous image defined by a bunch of black rectangles



Signal processing view



Signal processing view



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Antialiasing

- A name for techniques to prevent aliasing
- In image generation, we need to filter
 - Convolve continuous image with a sampling filter
 - Simple: average the image over an area (box filtering)
 - Better: weight by a smoother filter
- Methods depend on source of image
 - Rasterization (lines and polygons)
 - Point sampling (e.g. raytracing)
 - Texture mapping

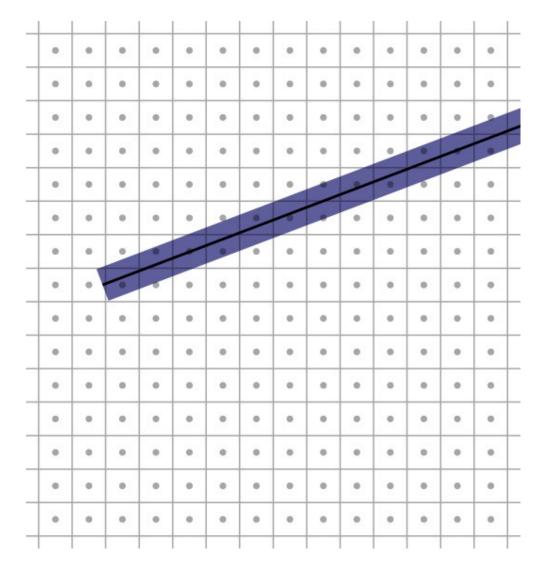
Rasterizing lines

- Define line as a rectangle
- Specify by two endpoints
- Ideal image: black inside, white outside

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Rasterizing lines

- Define line as a rectangle
- Specify by two endpoints
- Ideal image: black inside, white outside



Point sampling

- Approximate rectangle by drawing all pixels whose centers fall within the line
- Problem: all-ornothing leads to jaggies
 - this is sampling with no filter (aka. point sampling)

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Point sampling

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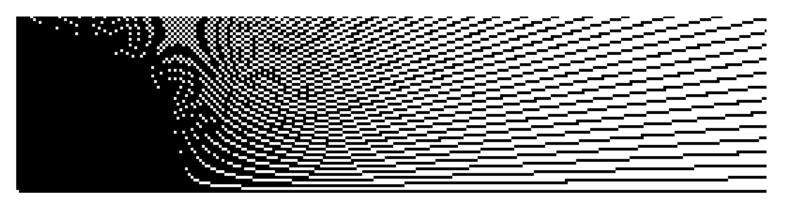
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Point sampling in action

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Aliasing

- Point sampling is fast and simple
- But the lines have stair steps and variations in width
- This is an aliasing phenomenon
 - Sharp edges of line contain high frequencies
- Introduces features to image that are not supposed to be there!



Antialiasing

- Point sampling makes an all-or-nothing choice in each pixel
 - therefore steps are inevitable when the choice changes
 - yet another example where discontinuities are bad
- On bitmap devices this is necessary
 - hence high resolutions required
 - 600+ dpi in laser printers to make aliasing invisible
- On continuous-tone devices we can do better

Antialiasing

- Basic idea: replace "is the image black at the pixel center?" with "how much is pixel covered by black?"
- Replace yes/no question with quantitative question.

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Box filtering

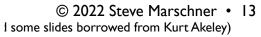
- Pixel intensity is proportional to area of overlap with square pixel area
- Also called "unweighted area averaging"

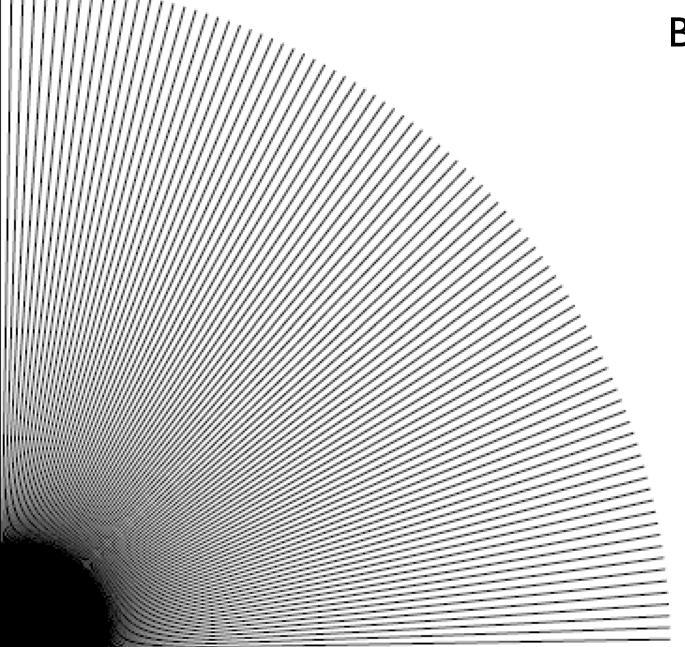
Box filtering by supersampling

- Compute coverage fraction by counting subpixels
- Simple, accurate
- But slow

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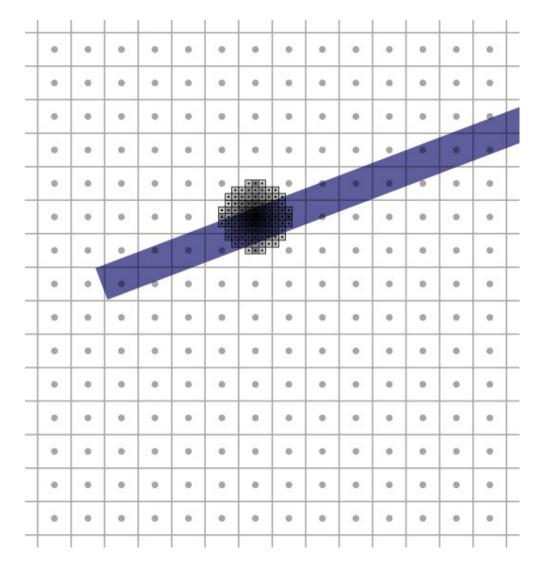


Weighted filtering

- Box filtering problem: treats area near edge same as area near center
 - results in pixel turning on "too abruptly"
- Alternative: weight area by a smooth function
 - unweighted averaging corresponds to using a box function
 - a gaussian is a popular choice of smooth filter
 - important property: normalization (unit integral)

Weighted filtering by supersampling

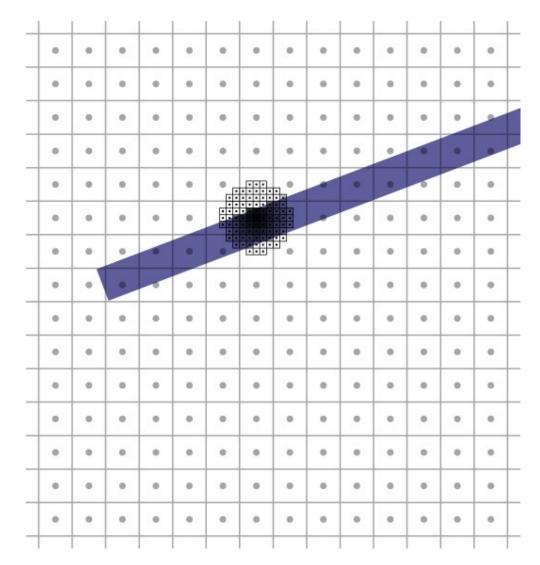
- Compute filtering integral by summing filter values for covered subpixels
- Simple, accurate
- But really slow



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Weighted filtering by supersampling

- Compute filtering integral by summing filter values for covered subpixels
- Simple, accurate
- But really slow

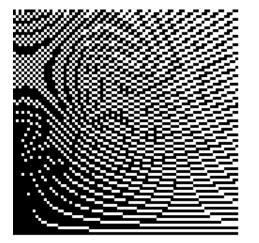


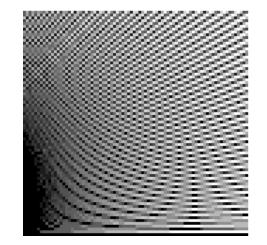
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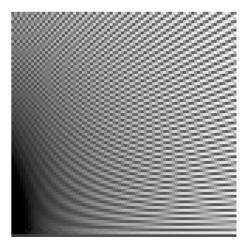
Gaussian filtering in action

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Filter comparison







Point sampling

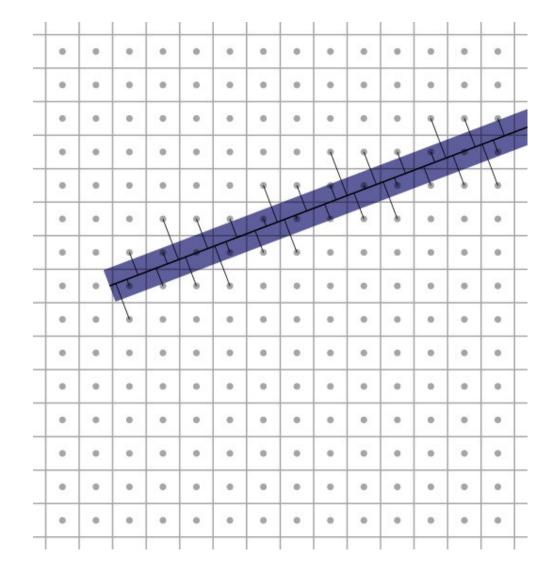
Box filtering

Gaussian filtering

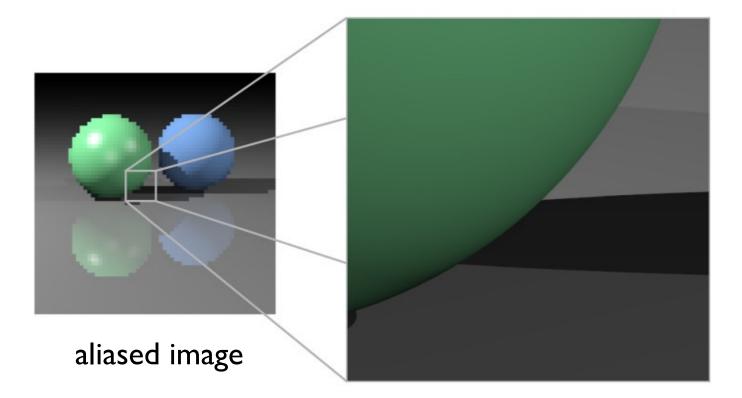
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More efficient antialiased lines

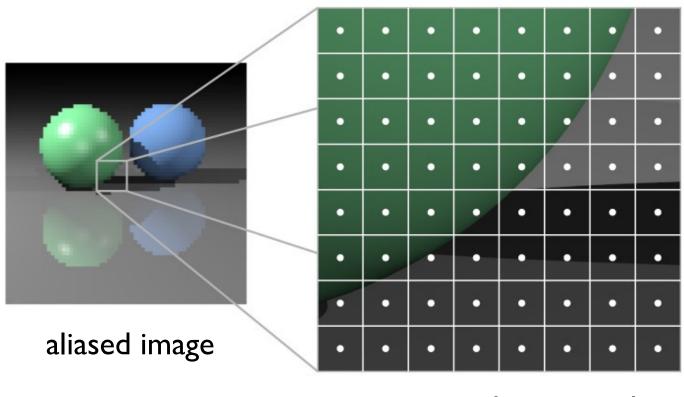
- Filter integral is the same for pixels the same distance from the center line
- Just look up in precomputed table based on distance
 - Gupta-Sproull
- Some additional details at ends...



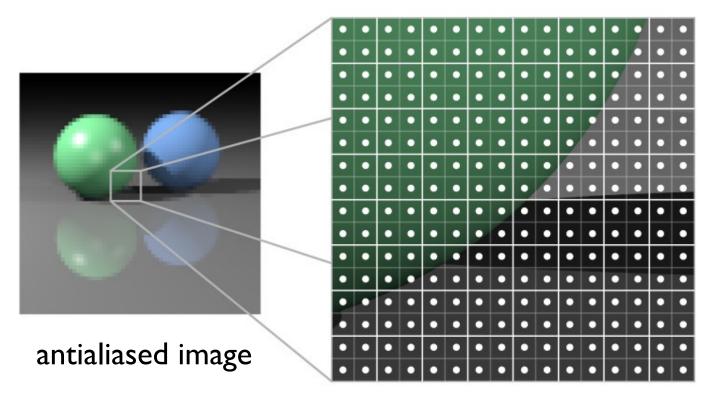
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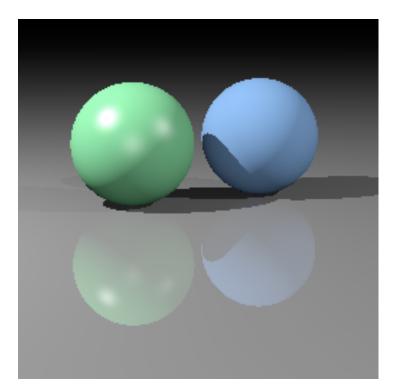
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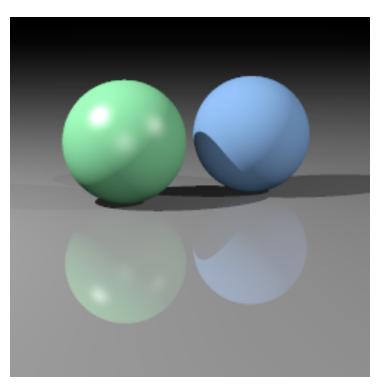


one sample per pixel



four samples per pixel





9 samples/pixel

one sample/pixel

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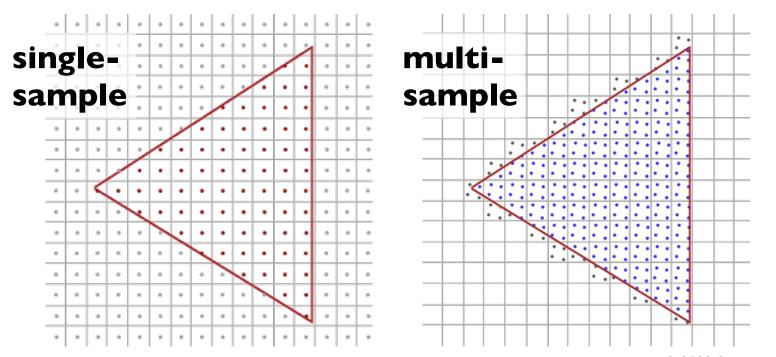
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Supersampling vs. multisampling

- Supersampling is terribly expensive
- GPUs use an approximation called *multisampling*
 - Compute one shading value per pixel
 - Store it at many subpixel samples, each with its own depth

Multisample rasterization

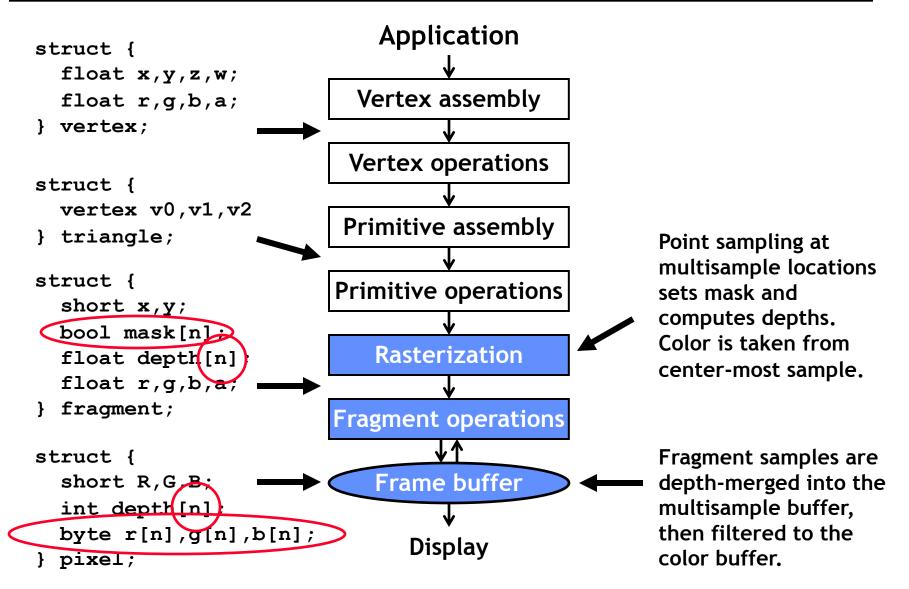
- Each fragment carries several (color,depth) samples
 - shading is computed per-fragment
 - depth test is resolved per-sample
 - final color is average of sample colors



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Multisample implementation (*n* samples)



CS248 Lecture 6

Kurt Akeley, Fall 2007

Multisample rasterization operations

Fragment selection

- Identify pixels for which fragments are to be generated
- New: generate fragment if any sample is within the primitive
 - Requires tiled sampling, rather than point sampling
 - Generates more fragments

Attribute assignment

- Assign attribute values to each fragment
- Sample color at the center of the pixel (as before)
- New: compute the Boolean per-sample coverage mask
 - True if-and-only-if the sample is within the primitive
- New: compute depth values for each sample location

Point-sampled fragment selection

Generate fragment if pixel center is inside triangle Implements point-sampled aliased rasterization

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9 fragments generated

Kurt Akeley, Fall 2007

Generate fragment if unit square intersects triangle Implements multisample rasterizations

■ 4x4 sample pattern with unit-square filter extent

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