## Antialiasing

## CS5625 Lecture I2

## Aliasing

point sampling a continuous image:
continuous image defined by ray tracing procedure

continuous image defined by a bunch of black rectangles


## Signal processing view



## Signal processing view



## Antialiasing

- A name for techniques to prevent aliasing
- In image generation, we need to filter
- Convolve continuous image with a sampling filter
- Simple: average the image over an area (box filtering)
- Better: weight by a smoother filter
- Methods depend on source of image
- Rasterization (lines and polygons)
- Point sampling (e.g. raytracing)
- Texture mapping


## Rasterizing lines

- Define line as a rectangle
- Specify by two endpoints
- Ideal image: black inside, white outside

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## Point sampling

- Approximate rectangle by drawing all pixels whose centers fall within the line
- Problem: all-ornothing leads to jaggies
- this is sampling with no filter (aka. point sampling)

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I some slides borrowed from Kurt Akeley)


## Aliasing

- Point sampling is fast and simple
- But the lines have stair steps and variations in width
- This is an aliasing phenomenon
- Sharp edges of line contain high frequencies
- Introduces features to image that are not supposed to be there!



## Antialiasing

- Point sampling makes an all-or-nothing choice in each pixel
- therefore steps are inevitable when the choice changes
- yet another example where discontinuities are bad
- On bitmap devices this is necessary
- hence high resolutions required
- 600+ dpi in laser printers to make aliasing invisible
- On continuous-tone devices we can do better


## Antialiasing

- Basic idea: replace "is the image black at the pixel center?" with "how much is pixel covered by black?"
- Replace yes/no question with quantitative question.

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## Box filtering

- Pixel intensity is proportional to area of overlap with square pixel area
- Also called "unweighted area averaging"


## Box filtering by supersampling

- Compute coverage fraction by counting subpixels
- Simple, accurate
- But slow

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## Box filtering in action

## Weighted filtering

- Box filtering problem: treats area near edge same as area near center
- results in pixel turning on "too abruptly"
- Alternative: weight area by a smooth function
- unweighted averaging corresponds to using a box function
- a gaussian is a popular choice of smooth filter
- important property: normalization (unit integral)


## Weighted filtering by supersampling

- Compute filtering integral by summing filter values for covered subpixels
- Simple, accurate
- But really slow


## Weighted filtering by supersampling

- Compute filtering integral by summing filter values for covered subpixels
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## Gaussian filtering in action

## Filter comparison



Point sampling


Box filtering


Gaussian filtering

## More efficient antialiased lines

- Filter integral is the same for pixels the same distance from the center line
- Just look up in precomputed table based on distance
- Gupta-Sproull
- Some additional details at ends...


## Antialiasing in ray tracing



## Antialiasing in ray tracing



## Antialiasing in ray tracing


four samples per pixel

## Antialiasing in ray tracing


one sample/pixel


9 samples/pixel

## Supersampling vs. multisampling

- Supersampling is terribly expensive
- GPUs use an approximation called multisampling
- Compute one shading value per pixel
- Store it at many subpixel samples, each with its own depth


## Multisample rasterization

- Each fragment carries several (color,depth) samples
- shading is computed per-fragment
- depth test is resolved per-sample
- final color is average of sample colors



## Multisample implementation ( $n$ samples)



## Multisample rasterization operations

## Fragment selection

■ Identify pixels for which fragments are to be generated

- New: generate fragment if any sample is within the primitive
■ Requires tiled sampling, rather than point sampling
- Generates more fragments

Attribute assignment
■ Assign attribute values to each fragment

- Sample color at the center of the pixel (as before)
- New: compute the Boolean per-sample coverage mask
- True if-and-only-if the sample is within the primitive
- New: compute depth values for each sample location


## Point-sampled fragment selection

Generate fragment if pixel center is inside triangle Implements point-sampled aliased rasterization


9 fragments generated

## Tiled fragment selection

Generate fragment if unit square intersects triangle Implements multisample rasterizations

- $4 \times 4$ sample pattern with unit-square filter extent


