

## CS5434 – Homework 5

Due Tuesday December 3<sup>rd</sup>, 2013.

### Problem 1

Suppose  $X$  is one of eight messages, A through H, where

$$P(A) = P(B) = P(C) = P(D) = 1/16$$

$$P(E) = P(F) = P(G) = 1/8$$

$$P(H) = 3/8.$$

What is the entropy of the distribution?

### Problem 2

Decrypt the following word, which was encrypted with a Caesar cipher of shift 3.

Dqwhgloxyldq

### Problem 3

Suppose we have a strong cryptographic hash, which produces values of fixed size of  $n$  bits. You may assume that the output has perfect entropy.

- a) Suppose we have two completely different plaintexts. What is the probability that they will have the same hash, as a function of  $n$ ?
- b) Suppose that we have  $m$  completely different plaintexts. What is the probability that any two of them will have the same hash, as a function of  $n$  and  $m$ ?

### Problem 4

Look up the top 10 global websites using the Alexa 500 list. Determine who each of them use as their Certificate Authority.

### Problem 5

The following cipher-text was encrypted with a single-character substitution cipher of some kind. Decrypt it to determine the English plain-text.

Hint 1) Line breaks were not encrypted, but spaces and punctuation were.

Hint 2) The plain-text is famous.

.xebwcmxb,wfvnwc,z,vwi,fbcwfpwxxebw.fdq,bcwgbxepqdw.xbdqwxvwdqrcwmxvdrv,vdk  
fvw, wvfdrxvkwmxvm,rz,nwrwvurg,bdikwfvnwn,nrmfd,nwdxwdq,wybxyxcrdxvwdqfd  
fuuwo,vwfb,wmb,fd,nw,aeful

vx w ,wfb,w,vpfp,nwrwvfwpb,fdwmrzruw fbkwd,cdrvpw q,dq,bwdqfdwvdrxvkxb  
fviwvdrxvwcxwmxvm,rz,nwfvnwcxwn,nrmfd,nkwmfvwuxvpw,vneb,lw ,wfb,wo,d  
xvwfwpb,fdwgfddu,t,r,unwx.wdqfdw fblww ,wqfz,wmxo,wdxwn,nrmfd,wfvyxbrxvwx.  
dqfdw.r,unkwfcfw.rvfuw,b,cdrvpwyufm,w.xbwqxc,w qxwq,b,wpfz,wdq,rbwurz,cwdqfdw  
dqfdwvdrxvworpqdwurz,lwrdrwcfudxp,dq,bw.rddrvpwwvwybxy,bwdqfdw ,wcqxeunwnxw  
dqrl

gedkwrwfwufbp,bwc,vc,kw ,wmfvvxdwn,nrmfd,wttw ,wmfvvxdwmxvc,mbfd,wttw ,  
mfvvdwqfuux wttwdqrcwpxevnlwdq,wgbfz,wo,vkwurzrvpwwfvnwn,fknw qx  
cdebpu,nwq,b,kwqfz,wmxvc,mbfd,nwrdkw.fbwfgxz,wxebwyxxbwyx ,bwdxvfnwxb  
n,dbfmdlwdq,w xbunw ruuwurddu,wvxd,kwvxbwuxvpwb,o,og,bw qfdw ,wcfiwq,b,kw  
gedwrdwfmfvw,z,bw.xbp,dw qfdwdq,iwnrnwq,b,lwrdrwcv.xbwecwdq,wurzrvpkwbfq,bkwdx  
g,wn,nrmfd,nwq,b,wdxwdq,wev.rvrcq,nw xb-w qrmqwdq,iw qxw.xepqdwq,b,  
qfz,wdqecw.fbwcxwvxguiwfnzfm,nlwrdrwrcwbfq,bw.xbwecwdxwg,wq,b,wn,nrmfd,nw  
dxwdq,wpb,fdwdfc-wb,ofrvrvpwg,.xb,wecwttwdqfdw.bxowdq,c,wqxvxb,nwn,fn  
,wdf-,wrvmb,fc,nwn,zdxrvwdxwdqfdwfmec,w.xbw qrmqwdq,iwqfz,wdq,wufcd  
.uuwo,fceb,wx.wn,zdxrvwttwdqfdw ,wq,b,wqrpqiwb,cxuz,wdqfdwdq,c,wn,fn  
cqfuuvxdwqfz,wnr,nwrwvzfrvttwdqfdwdqrcwvdrxvkwevn,bwpxnkwcqfuuwqfz,wf  
v, wgrbdqwx.w.b,,nxowttwfvnwdqfdwpxz,bvo,vdwx.wdq,wy,xyu,kwgiwdq,wy,xyu,kw  
.xbwdq,wy,xyu,kwcqfuuvxdwy,brcqw.bxowdq,w,fbdq