## CS 5430:

## Formal Analysis of a

 Hierarchical Certification AuthorityFred B. Schneider<br>Samuel B Eckert Professor of Computer Science<br>Department of Computer Science<br>Cornell University<br>Ithaca, New York 14853<br>U.S.A.

Cornell CIS

## CAL

## Language:

C ::= F (F a formula of First-order Predicate Logic)
| P says C
| $\mathrm{P}^{\prime}$ speaksfor P
| $P^{\prime}$ speaks $x: C$ for $P$
| C^C'
| CvC'
$\mathrm{C} \Rightarrow \mathrm{C}^{\prime}$
N.b. $\neg \mathrm{C}: ~(\mathrm{C} \Rightarrow$ false)

## Models for CAL

$\omega(P)$ is the set of beliefs principal $P$ has.

- P says $C$ iff $C \in \omega(P)$
- $\mathrm{P}^{\prime}$ speaksfor P iff $\quad \omega\left(\mathrm{P}^{\prime}\right) \subseteq \omega(\mathrm{P})$
$\omega(\mathrm{P})$ called the worldview of P


## CAL Inference Rules: says

$$
\frac{C}{P \text { says } C} \quad \frac{P \text { says } C}{P \text { says }(P \text { says } C)} \quad \frac{P \text { says }(P \text { says } C)}{P \text { says } C}
$$

$$
\frac{P \text { says }\left(C \Rightarrow C^{\prime}\right)}{(P \text { says } C) \Rightarrow\left(P \text { says } C^{\prime}\right)}
$$

## Example CAL Proof (1)

P says $C$,

$$
P \text { says }\left(C \Rightarrow C^{\prime}\right)
$$

## Example CAL Proof (2)

$P$ says $C, \frac{P \text { says }\left(C \Rightarrow C^{\prime}\right)}{(P \text { says } C) \Rightarrow\left(P \text { says } C^{\prime}\right)}$

## Example CAL Proof (3)

$\frac{P \text { says } C, \frac{P \text { says }\left(C \Rightarrow C^{\prime}\right)}{(P \text { says } C) \Rightarrow\left(P \text { says } C^{\prime}\right)}}{P \text { says } C^{\prime}}$

## CAL Inference Rules: speaksfor

$P$ says $\left(P^{\prime}\right.$ speaksfor $P$ ) $P^{\prime}$ speaksfor $P$
$P^{\prime}$ speaksfor $P$
$\left(P^{\prime}\right.$ says $\left.C\right) \Rightarrow(P$ says $C)$
$\underline{P \text { speaksfor } P^{\prime}, P^{\prime} \text { speaksfor } P^{\prime \prime}}$

$$
P \text { speaksfor } P^{\prime \prime}
$$

## Credentials Can Convey Beliefs

$\mathrm{k}_{\mathrm{S}}$ is a signing key; $\mathrm{K}_{\mathrm{S}}$ is a verification key
$\mathrm{k}_{\mathrm{s}}$-sign(C): $\mathrm{K}_{\mathrm{S}}$ says C

- Public keys are principals.
- $K_{S}$ speaksfor $S$ if principal $S$ is the only agent with access to private key $\mathrm{k}_{\mathrm{s}}$.

A principal $S$ can be a hash of the running code and data that was read.

## Application

## Public Key Infrastructure (PKI)

$\mathrm{k}_{\mathrm{s}}$-sign(C):

- Certificate: $\mathrm{K}_{\mathrm{S}}-\langle\mathrm{C}\rangle$
- CAL formalization: $\mathrm{K}_{\mathrm{S}}$ says C

CAL formalization of delegation certificate:

- Certificate: $\mathrm{K}_{\mathrm{I}}-\left\langle\epsilon / \mathrm{com}: \mathrm{K}_{\text {com }}\right\rangle$
- CAL formalization: $\mathrm{K}_{\mathrm{I}}$ says ( $\mathrm{K}_{\text {com }}$ speaksfor $\epsilon / \mathrm{com}$ )


## Public Key Infrastructure (PKI)



## PKI Excerpt


$\mathrm{K}_{\text {edu }}-\left\langle\epsilon / \mathrm{edu} / \mathrm{cu}: \mathrm{K}_{\text {cu }}\right\rangle$
$\mathrm{K}_{\text {edu }}-\left\langle\epsilon / \mathrm{edu} / \mathrm{mit}: \mathrm{K}_{\text {mit }}\right\rangle$ /edu

```
K_cu-\langle\epsilon/edu/cu/cs: K K cs 
/edu/cu
```

$$
\begin{array}{l|l}
\mathrm{K}_{\mathrm{cs}}\left\langle\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}: \mathrm{K}_{\mathrm{fb}}\right\rangle & \text { /edu/cu/cs } \\
\mathrm{K}_{\mathrm{cs}}\left\langle\left\langle\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{la}: \mathrm{K}_{\mathrm{la}}\right\rangle\right.
\end{array}
$$

## CAL Model for PKI Excerpt


$\mathrm{K}_{\text {edu }}{ }^{-}\left\langle\epsilon / \mathrm{edu} /\right.$ mit : $\left.\mathrm{K}_{\text {mit }}\right\rangle \rightarrow \mathrm{K}_{\text {edu }}$ says ( $\mathrm{K}_{\text {mit }}$ speaksfor $\epsilon /$ edu/mit)

$\mathrm{K}_{\mathrm{cs}}-\left\langle\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}: \mathrm{K}_{\mathrm{fbs}} \rightarrow \mathrm{K}_{\mathrm{cs}}\right.$ says $\left(\mathrm{K}_{\mathrm{fbs}}\right.$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ ) $\mathrm{K}_{\mathrm{cs}}-\left\langle\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{la}: \mathrm{K}_{\mathrm{la}}\right\rangle \rightarrow \mathrm{K}_{\mathrm{cs}}$ says ( $\mathrm{K}_{\mathrm{la}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{la}$ )

## Sample Derivation

$\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

## CAL Model for PKI Except

$\mathrm{K}_{\mathrm{I}}-\left\langle\epsilon / \mathrm{com}: \mathrm{K}_{\text {com }}\right\rangle$
$\mathrm{K}_{\mathrm{I}}-\left\langle\epsilon /\right.$ edu : $\left.\mathrm{K}_{\text {edu }}\right\rangle \longrightarrow \mathrm{K}_{\mathrm{I}}$ says ( $\mathrm{K}_{\text {edu }}$ speaksfor $\epsilon /$ edu)
$\dddot{\mathrm{K}}_{\text {edu }}-\left\langle\epsilon / \mathrm{edu} / \mathrm{cu}: \mathrm{K}_{\mathrm{cu}}\right\rangle \longrightarrow \mathrm{K}_{\mathrm{edu}}$ says $\left(\mathrm{K}_{\mathrm{cu}}\right.$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu}$ )
$\mathrm{K}_{\text {edu }}-\left\langle\epsilon / \mathrm{edu} / \mathrm{mit}\right.$ : $\left.\mathrm{K}_{\text {mit }}\right\rangle$


## Sample Derivation (1)

$\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

## Sample Derivation (2)

$\mathrm{K}_{\mathrm{cs}}$ says $\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\mathrm{K}_{\mathrm{CS}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

## Sample Derivation (3)

$\mathrm{K}_{\mathrm{CS}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\mathrm{K}_{\mathrm{cs}}$ says $\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

- $\mathrm{K}_{\mathrm{CS}}$ speatesfor c/eder
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$


## Sample Derivation (4)

$\mathrm{K}_{\mathrm{cu}}$ says $\mathrm{K}_{\mathrm{cs}}$ speaksfor $\epsilon /$ edu/cu/cs
$\mathrm{K}_{\mathrm{cu}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu}$
$\epsilon / \mathrm{edu} / \mathrm{cu}$ says $\mathrm{K}_{\mathrm{cs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\epsilon / \mathrm{edu} / \mathrm{cu}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ says $\mathrm{K}_{\mathrm{cs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\mathrm{K}_{\mathrm{CS}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\mathrm{K}_{\mathrm{cs}}$ says $\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ says $\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

## Sample Derivation (5)

$\mathrm{K}_{\mathrm{I}}$ speaksfor $\epsilon$...
$\mathrm{K}_{\mathrm{cu}}$ says $\mathrm{K}_{\mathrm{cs}}$ speaksfor $\epsilon /$ edu/cu/cs
K cu chanlicfor f/odulot
$\epsilon / \mathrm{edu} / \mathrm{cu}$ says $\mathrm{K}_{\mathrm{cs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\epsilon / \mathrm{edu} / \mathrm{cu}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ says $\mathrm{K}_{\mathrm{cs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\mathrm{K}_{\mathrm{CS}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$
$\mathrm{K}_{\mathrm{cs}}$ says $\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$
$\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ says $\mathrm{K}_{\text {fbs }}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$ $\mathrm{K}_{\mathrm{fbs}}$ speaksfor $\epsilon / \mathrm{edu} / \mathrm{cu} / \mathrm{cs} / \mathrm{fbs}$

