# CS 5430 Expressive Information Flow Labels

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Spring 2019

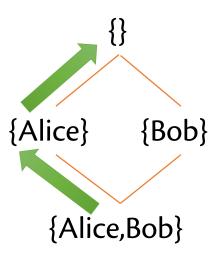
## A lattice for integrity

- Information is allowed to flow from data of high integrity (H) to data of low integrity (L).
- Low integrity (e.g., corrupted) data is not allowed to flow to high integrity data.



## Lattices for confidentiality





Defining allowed flows based only on a lattice might be too conservative or too permissive!

## Examples for confidentiality



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
res:=maj(vote, vote',)			

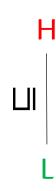
vote is high, but result of maj can be low.



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
res:=maj(vote, vote',)	YES		

vote is high, but result of maj can be low.

Declassification: A desirable flow from H to L.



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
res:=maj(vote, vote',)	YES	NO	is too conservative

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Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
c:=Enc(msg,key)			

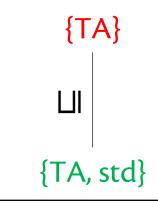
msg and key are high, but result of Enc can be low.



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
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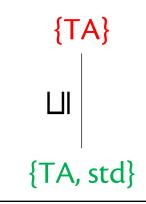
## Allowing a flow may depend on state



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
<pre>if end_of_semester() then   out:=release(grade)</pre>			

grade can flow only to TA, but at the end of the semester it can also flow to std.

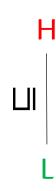
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## Allowing a flow may depend on ownership



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
<pre>if pgm_executed_by_FBI()   out:=release(xfile)</pre>			

xfile is high and owned by FBI. Only the FBI can make it low.

## Allowing a flow may depend on ownership



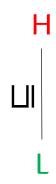
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a:=asgn(papers, reviewers)			

reviewers is low, but result of asgn should be high.



Example for confidentiality	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
a:=asgn(papers, reviewers)	NO	YES	is too permissive

reviewers is low, but result of asgn should be high.

Classification: A mandatory flow from L to H.

## Examples for integrity



Example for integrity	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
entry:=sanitize(userIN)			

userIN is low, but
result of sanitize
can be high.



Example for integrity	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
entry:=sanitize(userIN)	YES	NO	is too conservative

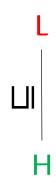
userIN is low, but result of sanitize can be high.

Endorsement: A desirable flow from L to H.



Example for integrity	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
doc':=excerpt(doc)			

doc is high, but result of excerpt should be low.



Example for integrity	Is flow desirable?	Is flow allowed by lattice?	Defining allowed flows based on lattice
doc':=excerpt(doc)	NO	YES	is too permissive

doc is high, but result of excerpt should be low.

Deprecation: A mandatory flow from H to L.

## Reclassifiers cause restrictions to change

Reclassifier	Restriction	Change
Operations	Confidentiality	Declassification Classification
State Ownership	Integrity	Endorsement Deprecation

Reclassifiers cause reclassifications!

We need information flow labels that specify reclassifications.

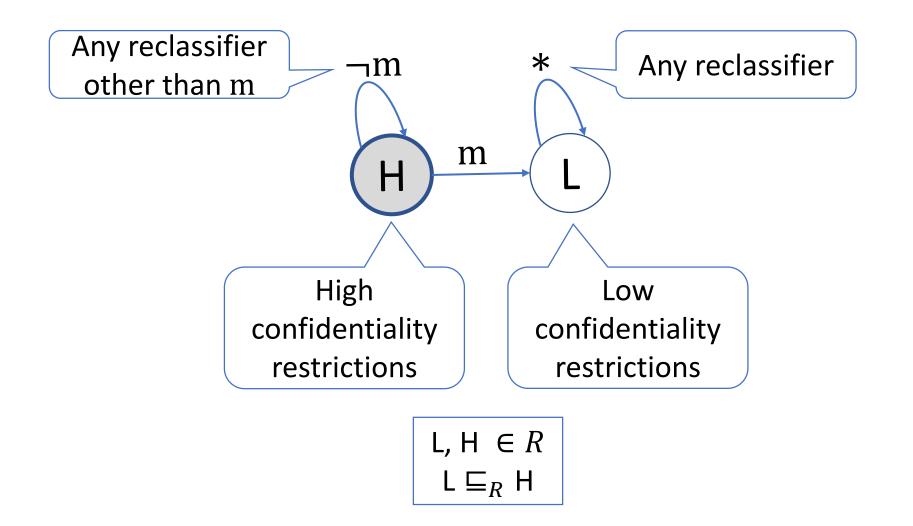
### Reactive Information Flow (RIF) labels

- A RIF label maps sequences of operations to restrictions.
  - Restrictions are taken from a partially ordered set  $\langle R, \sqsubseteq_R \rangle$ .
  - For confidentiality, restrictions can be sets of principals allowed to read.
- Reclassifiers abstract operations applied on inputs:
  - $[op(e_1, ..., e_n)]_{f_1,..,f_n}$

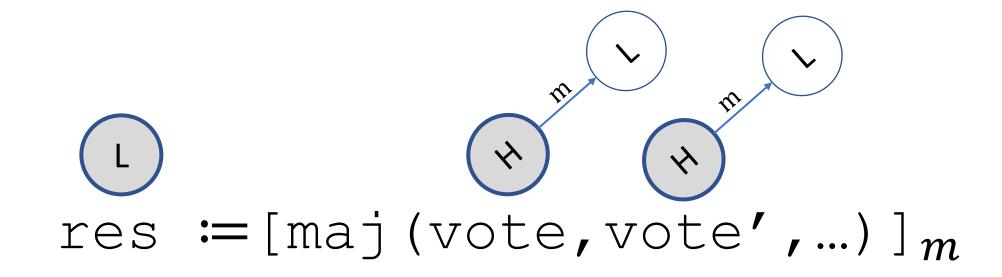
## Confidentiality example

```
res := [maj(vote, vote', ...)]_m
Reclassifier
```

#### RIF automaton for a vote



### RIF automata: Confidentiality example



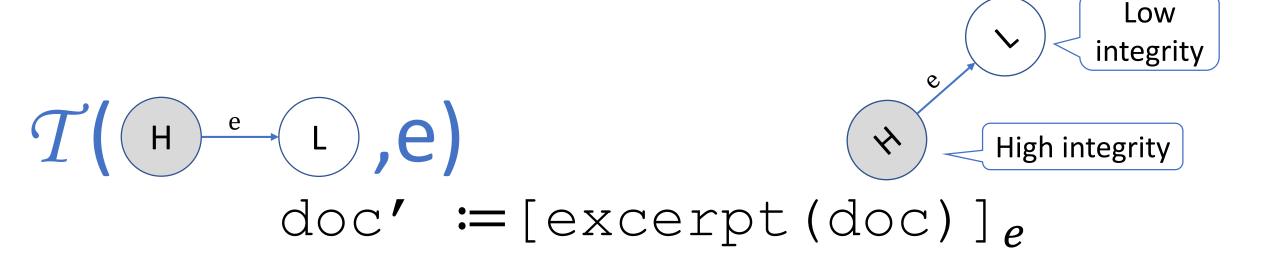
Reclassifier m triggers a declassification.

#### RIF automata

- An instantiation of RIF labels.
- A *RIF automaton* is a finite state automaton whose states correspond to restrictions and transitions correspond to reclassifiers.
- Formally, a RIF automaton  $\lambda_a$  is  $\langle Q, F, \delta, q_0, r \rangle$ :
  - Q is a finite set of automaton states,
  - F is the finite set of reclassifiers,
  - $\delta: Q \times F \to Q$  is a (deterministic) next-state transition function,
  - $q_0 \in Q$  is the current state of the RIF automaton,
  - $r: Q \to R$  gives the restrictions associated with each automaton state.

#### Function $\mathcal{T}$ for transition

 $L, H \in R$  $H \sqsubseteq_R L$ 



#### Function $\mathcal{T}$ for transition



### Function $\mathcal{R}$ , for current restrictions

$$\frac{1}{\operatorname{doc'}} := [\operatorname{excerpt}(\operatorname{doc})]_e$$

$$\mathcal{R}(L) = L$$

$$\mathcal{R}(H - L) = H$$

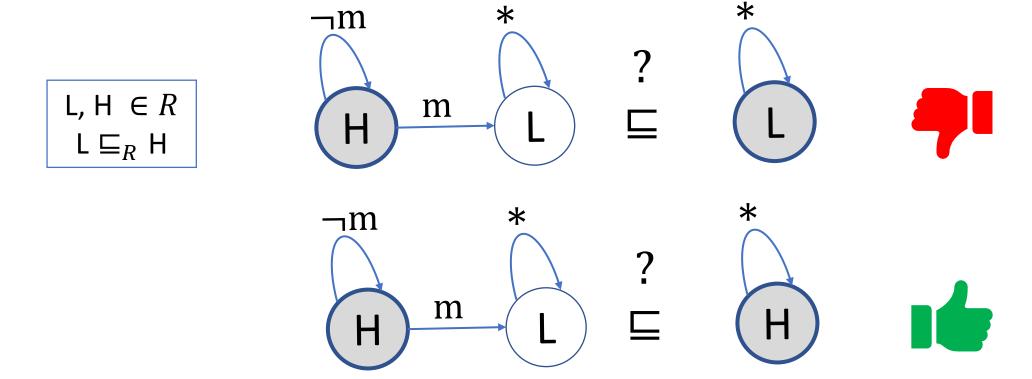
Reclassifier e triggers a deprecation.

### Functions $\mathcal{R}$ and $\mathcal{T}$

- $\mathcal{R}$  maps  $\lambda_a = \langle Q, F, \delta, q_0, r \rangle$  to the restrictions  $r \in R$  that  $\lambda_a$  currently imposes:
  - $\mathcal{R}(\lambda_a) \triangleq r(q_0)$
- $\mathcal{T}$  maps  $\lambda_a = \langle Q, F, \delta, q_0, r \rangle$  and reclassifier  $f \in \mathcal{F}$  to a RIF automaton that should be associated with the value produced by an operation abstracted by f:
  - $\mathcal{T}(\lambda_a) \triangleq \langle Q, F, \delta, \delta(q_0, f), r \rangle$
  - For sequence F of reclassifiers,  $\mathcal{T}(\lambda_a, Ff) \triangleq \mathcal{T}(\mathcal{T}(\lambda_a, F), f)$ .

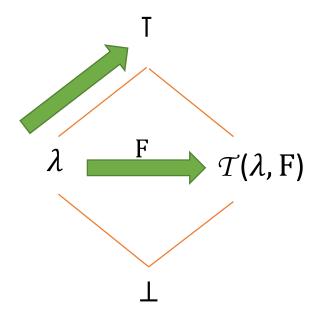
#### RIF automata form a lattice

$$\lambda \sqsubseteq \lambda' \triangleq \forall F \in \mathcal{F}^* : \mathcal{R}(\mathcal{T}(\lambda, F)) \sqsubseteq_R \mathcal{R}(\mathcal{T}(\lambda', F))$$



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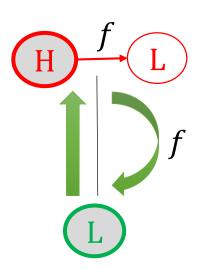


#### When is a flow allowed?

Assume variable  $\underline{y}$  is tagged with  $\underline{L}$  and variable  $\underline{x}$  is tagged with  $\underline{L}$ 



- $x := y \mod 2$





$$m: H \xrightarrow{Enc(k)} L$$

$$c := [Enc(m, k)]_{Enc(k)}$$

$$m: H \longrightarrow L$$

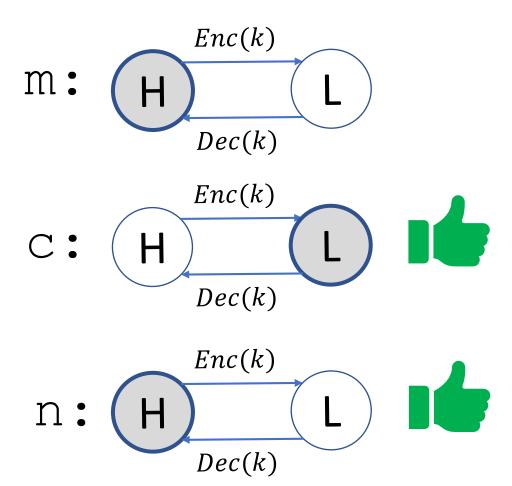
$$C := [Enc(m, k)]_{Enc(k)}$$

$$n := [Dec(c, k)]_{Dec(k)}$$



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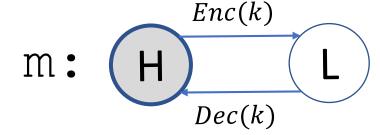
## Can RIF automata handle the encryption

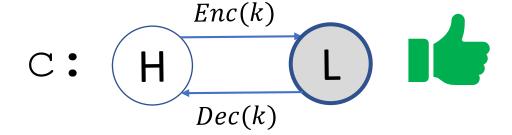
example?

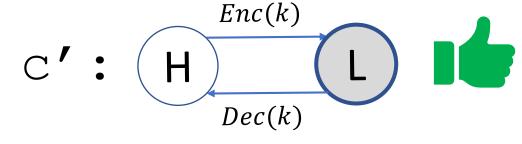
$$c := [Enc(m, k)]_{Enc(k)}$$

$$c' \coloneqq [Enc(c,k)]_{Enc(k)}$$

$$n := [Dec(c', k)]_{Dec(k)}$$







$$n: \underbrace{H}_{Dec(k)}^{Enc(k)}$$

- Examples:
  - m is H
  - Enc(Enc(m, k), k) is L
  - Dec(Enc(Enc(m, k), k), k) is L
  - Dec(Dec(Enc(Enc(m, k), k), k), k) is H
- If the number of consecutive Dec equals the number of consecutive Enc, then the restriction is H; otherwise the restriction is L.
- RIF automata cannot be used to count an unbounded number of applied cryptographic operations.

#### к-labels

```
declassification
x = Enc(m, k)
H

Enc(k)
H
```

$$y = Enc(x, k'):$$
Enc(k')

H

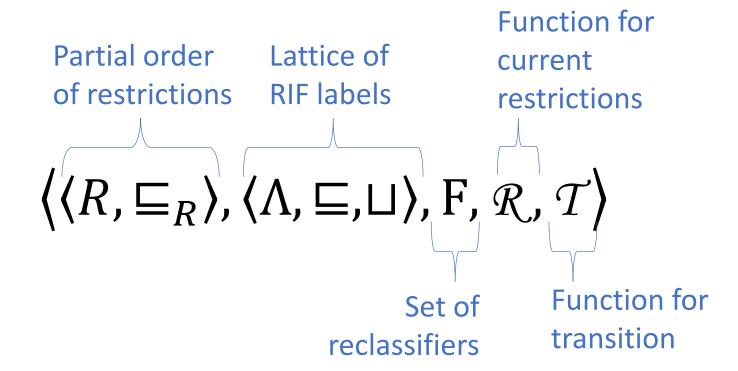
$$^{\mathsf{H}}$$
m =  $Dec(z,k)$ :

$$z = Dec(y, k'):$$
Enc(k)
H

#### к-labels

- A  $\kappa$ -label  $\lambda_{\kappa}$  is a stack (i.e., a simplifies push-down automaton).
- Assume restrictions  $\langle \{H, L\}, \sqsubseteq_R \rangle$ .
- $\mathcal{R}(\lambda_{\kappa}) \triangleq$ 
  - H, if  $\lambda_{\kappa}$  is empty (stores no reclassifier)
  - L, otherwise.
- $\mathcal{T}(\lambda_{\kappa}, f) \triangleq$ 
  - $pop(\lambda_{\kappa})$ , if f is the inverse of the top element in  $\lambda_{\kappa}$
  - push( $\lambda_{\kappa}$ , f), otherwise.

#### A class of RIF labels



#### RIF labels

