
CS 5430

Block Cipher Modes and Asymmetric-key Encryption

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Spring 2017

Review: block ciphers

- Encryption schemes:
 - $\text{Enc}(m; k)$: encrypt message m under key k
 - $\text{Dec}(c; k)$: decrypt ciphertext c with key k
 - $\text{Gen}(\text{len})$: generate a key of length len
- Defined for a particular block length
 - DES: 64 bit blocks
 - AES: 128 bit blocks
 - Messages must have exactly that length
- Every pair of principals must share a key
 - $O(n^2)$ key distribution problem

BLOCK CIPHER MODES

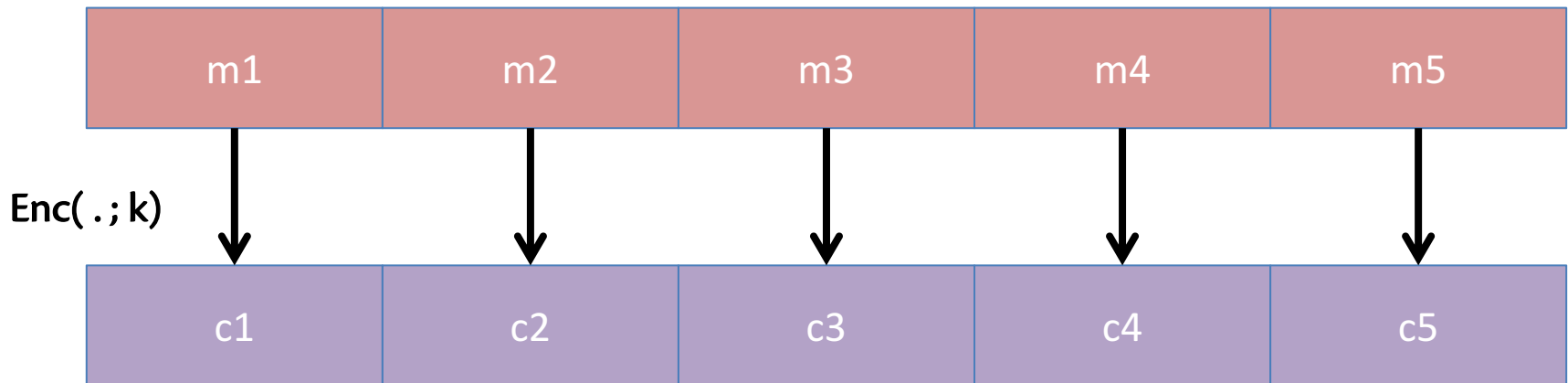
The obvious idea...

- Divide long message into short chunks, each the size of a block
- Encrypt each block with the block cipher

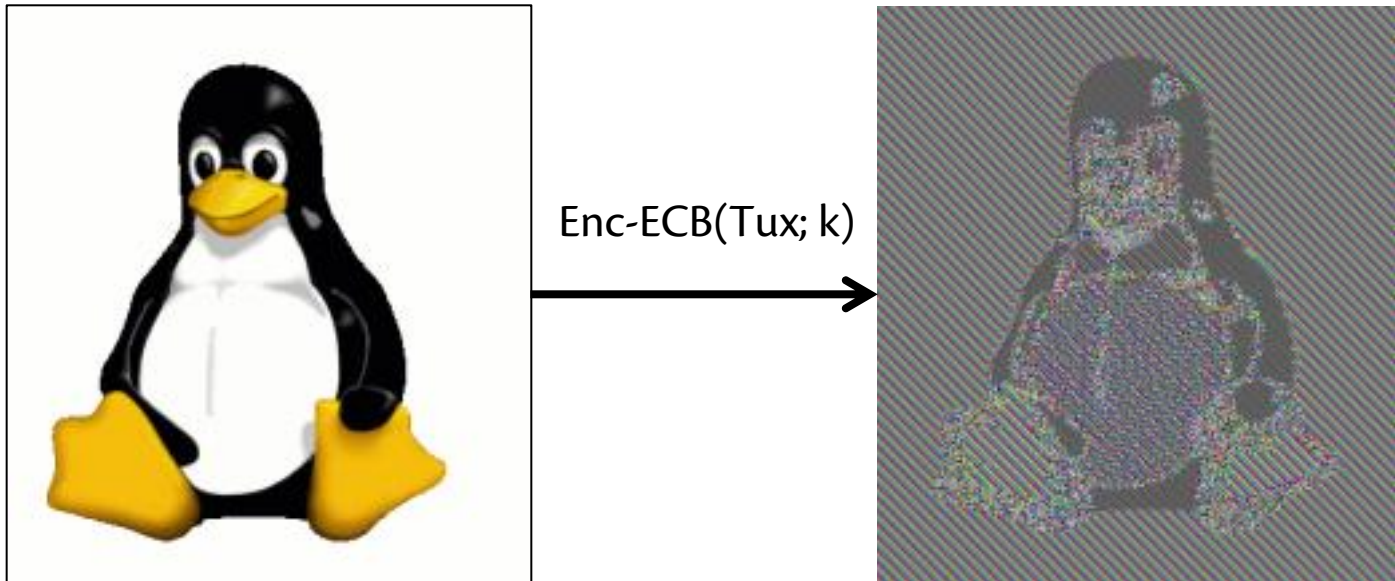


The obvious idea...

- Divide long message into short chunks, each the size of a block
- Encrypt each block with the block cipher



...is a bad idea

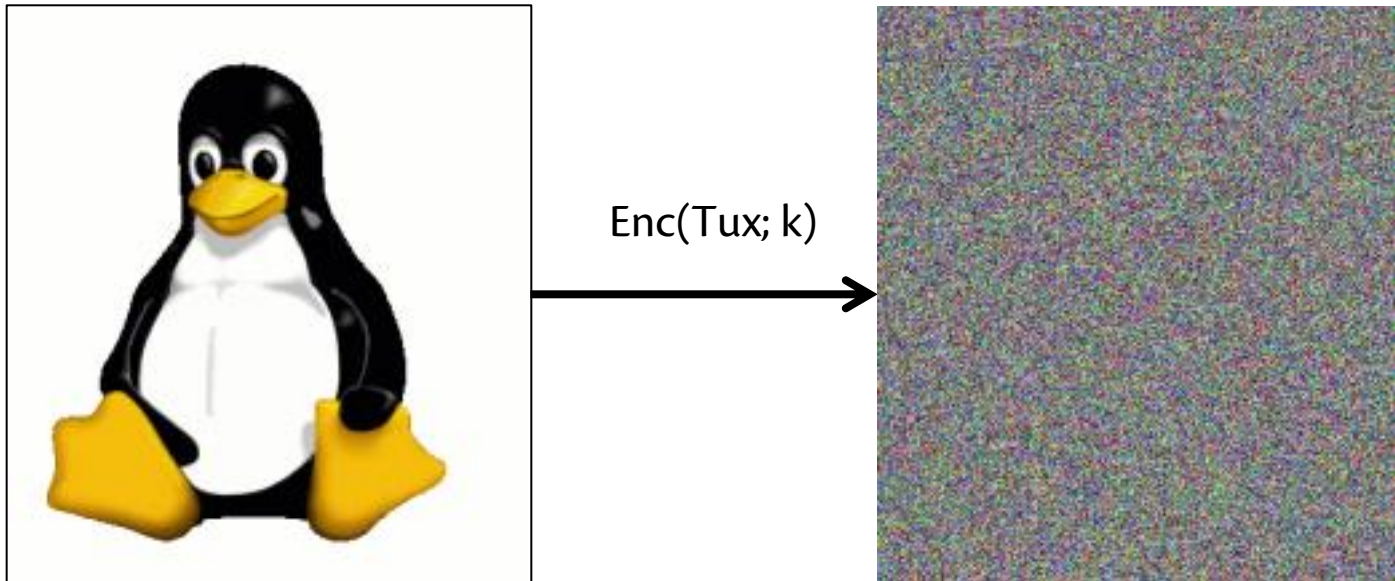


Called *electronic code book*
(ECB) mode

Good modes

- Cipher Block Chaining (CBC) mode
 - idea: XOR previous ciphertext block into current plaintext block
- Counter (CTR) mode
 - idea: derive one-time pad from increasing counter
- (and others)
- With both:
 - every ciphertext block depends in some way upon previous plaintext or ciphertext blocks
 - so even if plaintext blocks repeat, ciphertext blocks don't
 - so *intra-message* repetition doesn't disclose information

Good modes



but what if you encrypt Tux twice under the same key?

Good modes

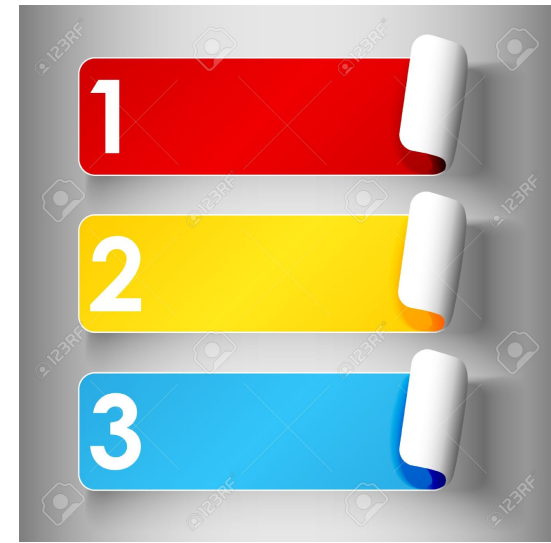
- Problem: block ciphers are *deterministic*. inter-message repetition is visible to attacker
- Both CBC and CTR modes require an additional parameter: a *nonce*
 - $\text{Enc}(m; \text{nonce}; k)$
 - $\text{Dec}(c; \text{nonce}; k)$
 - CBC calls the nonce an *initialization vector* (IV)
- Different nonces make each encryption different than others
 - Hence inter-message repetition doesn't disclose information

Nonces

A nonce is a number used once

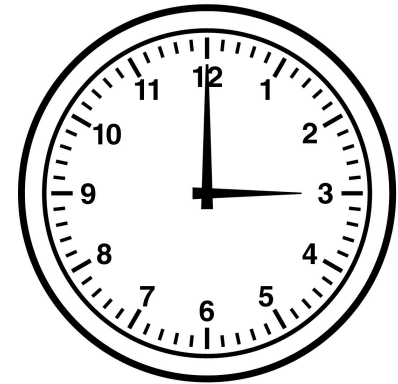
Must be

- **unique:** never used before in lifetime of system and/or (depending on intended usage)
- **unpredictable:** attacker can't guess next nonce given all previous nonces in lifetime of system



Nonce sources

- **counter**
 - requires state
 - easy to implement
 - can overflow
 - highly predictable
- **clock**: just a counter
- **random number generator**
 - might not be unique, unless drawn from large space
 - might or might not be unpredictable
 - generating randomness:
 - standard library generators often are not cryptographically strong, i.e., unpredictable by attackers
 - cryptographically strong randomness is a black art



Random comics

DILBERT By SCOTT ADAMS



```
int getRandomNumber()  
{  
    return 4; // chosen by fair dice roll.  
              // guaranteed to be random.  
}
```

Padding

What if the message length isn't *exactly* a multiple of block length? End up with final block that isn't full:



Non-solution: pad out final block with 0's (not reversible)

Solution: Let B be the number of bytes that need to be added to final plaintext block to reach block length. Pad with B copies of the byte representing B . Called PKCS #5 or #7 padding.

Block modes

Now we know how to encrypt messages of arbitrary length!

But we still have the quadratic key distribution problem...

ASYMMETRIC-KEY ENCRYPTION

Key pairs

- Instead of sharing a key between pairs of principals...
- ...every principal has a pair of keys
 - **public key:** published for the world to see
 - **private key:** kept secret and never shared



Key pairs

Terminology breakdown!

- private keys aren't necessarily personally-identifying
- symmetric-key crypto sometimes called "secret key" even though private keys also kept secret

Protocol to exchange encrypted message

1. A: $c = \text{Enc}(m; K_B)$
2. A \rightarrow B: c
3. B: $m = \text{Dec}(c; k_B)$

key pair: (K_B, k_B)

- public key written with uppercase letter
- private key written with lowercase letter

Public keys

0. B: $(K_B, k_B) = \text{Gen}(\text{len})$
1. ...

- All public keys published in "phonebook"
- So A can lookup B's key to send message
- Length of phonebook is $O(n)$
- So quadratic problem reduced to linear!

RSA

[Rivest, Shamir, Adleman 1977]

Shared Turing Award in 2002: *ingenious contribution to making public-key cryptography useful in practice*



RSA modulus

- Encryption and decryption are big integer operations modulo a large number called the *modulus*
 - Size of modulus bounds the size of keys and messages
 - Common modulus sizes: 1024, 2048, ... bits
- Modulus is itself a product of two large primes
 - One way to break RSA would be to efficiently factor such numbers
 - Largest challenge broken so far is 768-bit modulus [2010]
 - Shor's algorithm factors in polynomial time on a quantum computer
 - largest factorization so far is of the number 56153 (i.e., 16 bits)
 - motivates work on *post-quantum cryptography*

Textbook RSA is insecure

- *Deterministic*: given same plaintext and key, always produces the same ciphertext
- Several other attacks, too [Katz & Lindell 2008, section 10.4.2]
- **Solution:** incorporate a nonce in the message before encrypting
 - Called *padding* but *encoding* might be a better term
 - Don't implement yourself; use OAEP implementation in your crypto library (Optimal Asymmetric Encryption Padding)

Elgamal

Taher Elgamal [1985]



Elgamal

- Like RSA:
 - Big integer operations modulo a large number
 - Common modulus (*group*) sizes: 1024, 2048, ... bits
- Unlike RSA:
 - Key size can be much smaller than group size, which can speed up some operations
 - Elgamal encryption is *probabilistic*:
 - Given same plaintext and key, different calls to Enc produce different ciphertexts with high probability
 - Choice of a nonce is built-in to algorithm instead of part of padding
 - Factoring isn't relevant
 - One way to break Elgamal is by taking discrete logarithms

Key lengths

Again, various recommendations for strength summarized at <https://www.keylength.com/en/>

Problems of length

- Asymmetric encryption uses big integers, not byte arrays
 - all messages must be encoded as integers
 - modulus dictates maximum integer that can be encrypted
 - big integer operations are slow
 - say, 1 to 3 orders of magnitude slower than block ciphers
- So the problems we had before crop up again...
 - what if message length is too short?
 - actually that's okay: a small integer is still an integer
 - what if message length is too long?
 - in theory could use block modes like with symmetric encryption
 - in practice, that's too inefficient...



HYBRID ENCRYPTION

Hybrid encryption



- Assume:
 - Symmetric encryption scheme ($\text{Gen}_S, \text{Enc}_S, \text{Dec}_S$)
 - Asymmetric encryption scheme ($\text{Gen}_A, \text{Enc}_A, \text{Dec}_A$)
- Use asymmetric encryption to establish a shared session key
 - Avoids quadratic problem, assuming existence of phonebook
 - Session key will be short, so avoids inefficiency
- Use symmetric encryption to exchange long plaintext encrypted under session key
 - Gain efficiency of block cipher and mode

Protocol to exchange encrypted message

0. B: $(K_B, k_B) = \text{Gen}_A(\text{len}_A)$
1. A: $k_s = \text{Gen}_S(\text{len}_S)$
 $c1 = \text{Enc}_A(k_s; K_B)$
 $c2 = \text{Enc}_S(m; k_s) \text{ //mode}$
2. A \rightarrow B: $c1, c2$
3. B: $k_s = \text{Dec}_A(c1; k_B)$
 $m = \text{Dec}_S(c2; k_s)$

Session keys

- If key compromised, only those messages encrypted under it are disclosed
- Used for a brief period then discarded
 - **cryptoperiod**: length of time for which key is valid
 - in this case, for a single (long) message
 - not intended for reuse in future messages
 - only intended for unidirectional usage:
 - $A \rightarrow B$, not $B \rightarrow A$
 - why? A chose the key, not B

Encryption

- We can now protect confidentiality of messages against Dolev-Yao attacker
 - efficiently, thanks to hybrid of symmetric and asymmetric encryption
 - assuming existence of phonebook of public keys
- But what about integrity...?

Upcoming events

- [today] A1 due, A2 out
- [Mon] Feb Break

Few false ideas have more firmly gripped the minds of so many intelligent men than the one that, if they just tried, they could invent a cipher that no one could break. – David Kahn