CS 4810 Homework Assignment 3 due Monday in class Sept 17

1. Write a regular expression for the set of strings of 0 's and 1 's where every substring 00 appears before any substring 11 .
2. Write a regular expression for the set accepted by the finite automaton

|  | 0 | 1 |
| :---: | :---: | :---: |
| $A$ | $B$ | $C$ |
| $B$ | $C$ | $D$ |
| $C$ | $D$ | $A$ |
| $D$ | $A$ | $B$ |

The start state is $A$ and the set of final states is $\{D\}$.
3. Let $L$ be the set of all strings of 0 's and 1 's with an odd number of 0 's and a number of 1 's divisible by three.
(a) Try to write a regular expression denoting the set $L$. You do not need to hand this work in. Just see how hard it is.
(b) Construct a deterministic finite automaton $M$ that accepts $L$.
(c) Convert the deterministic finite automaton $M$ to a regular expression.
4. Consider the set $L$ of all strings of 0 's and 1 's with an equal number of substrings 01 and 10. The substrings 01 and 10 may overlap. Thus 010 is in $L$ as well as 0110 . Is $L$ a regular set or not a regular set? Give a compelling argument for your answer.
5. Let $L$ be the regular set $0^{*} 10^{*} 10^{*}$. Let $J$ be the set of all middle thirds of strings in $L$ whose lengths are divisible by 3 . List a few strings of $J$. Is $J$ a regular set? Give a compelling argument for your answer.

