CS 4810 Homework Assignment 4 due Monday class Sept 18

1. Create a finite automaton that accepts all strings of 0's and 1's in which some substring of length five has occurred twice.
2. Give a machine construction for shuffle $\left(L_{1}, L_{2}\right)$.
3. Minimize the finite automaton below. Its start state is A and the set of final states is $\{D\}$.

|  | 0 | 1 |
| ---: | :---: | :---: |
| $A$ | $B$ | $A$ |
| $B$ | $A$ | $C$ |
| $C$ | $D$ | $B$ |
| $* D$ | $D$ | $A$ |
| $E$ | $D$ | $F$ |
| $F$ | $G$ | $E$ |
| $G$ | $F$ | $G$ |
| $H$ | $G$ | $D$ |

4. Use the pumping lemma to prove that $\left\{a^{n} b^{n} c^{n} \mid n \geq 1\right\}$ is not a regular set.
5. Use the pumping lemma to prove that
$\{x y \mid$ number of a's in $x$ equals the number of a's in $y$ and the number of b's in $x$ equals the number of b's in $y$.
is not a regular set.
