Binocular stereo

Binocular stereo

• General case: cameras can be arbitrary locations and orientations



Binocular stereo

• Special case: cameras are parallel to each other and translated along X axis



Stereo with *rectified cameras*

• Special case: cameras are parallel to each other and translated along X axis



Stereo head



Kinect / depth cameras



Stereo with "rectified cameras"



 Without loss of generality, assume origin is at pinhole of 1st camera

$$\vec{\mathbf{x}}_{img}^{(1)} \equiv \begin{bmatrix} I & \mathbf{0} \end{bmatrix} \vec{\mathbf{x}}_{u}$$
$$\vec{\mathbf{x}}_{img}^{(2)} \equiv \begin{bmatrix} I & \mathbf{t} \end{bmatrix} \vec{\mathbf{x}}_{w}$$
$$\mathbf{t} = \begin{bmatrix} t_{x} \\ 0 \\ 0 \end{bmatrix}$$

 Without loss of generality, assume origin is at pinhole of 1st camera



• Without loss of generality, assume origin is at pinhole of 1st camera $\vec{\mathbf{x}}_{img}^{(1)} \equiv \begin{bmatrix} I & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{x}_w \\ 1 \end{bmatrix} = \mathbf{x}_w = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$ $\vec{\mathbf{x}}_{img}^{(2)} \equiv \begin{bmatrix} I & \mathbf{t} \end{bmatrix} \begin{bmatrix} \mathbf{x}_w \\ 1 \end{bmatrix} = \mathbf{x}_w + \mathbf{t} = \begin{bmatrix} X + t_x \\ Y \\ Z \end{bmatrix}$

 Without loss of generality, assume origin is at pinhole of 1st camera



 Without loss of generality, assume origin is at pinhole of 1st camera_____



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 Without loss of generality, assume origin is at pinhole of 1st camera



- X coordinate differs by t_x/Z
- That is, difference in X coordinate is *inversely proportional to depth*
- Difference in X coordinate is called *disparity*
- Translation between cameras (tx) is called *baseline*
- disparity = baseline / depth

The disparity image

- For pixel (x,y) in one image, only need to know disparity to get correspondence
- Create an image with color at (x,y) = disparity



right image



left image



disparity



- For rectified cameras, correspondence problem is easier
- Only requires searching along a particular row.

NCC - Normalized Cross Correlation

- Lighting and color change pixel intensities
- Example: increase brightness / contrast
- $I' = \alpha I + \beta$
- Subtract patch mean: invariance to β
- Divide by norm of vector: invariance to $\boldsymbol{\alpha}$

•
$$x' = x - \langle x \rangle$$

• $x'' = \frac{x'}{||x'||}$

• similarity = $x'' \cdot y''$



Cross-correlation of neighborhood





regions A, B, write as vectors a, b

translate so that mean is zero

$$\mathbf{a} \rightarrow \mathbf{a} - \langle \mathbf{a} \rangle, \ \mathbf{b} \rightarrow \mathbf{b} - \langle \mathbf{b} \rangle$$

cross correlation = $\frac{\mathbf{a}.\mathbf{b}}{|\mathbf{a}||\mathbf{b}|}$

Invariant to $I \rightarrow \alpha I + \beta$





The NCC cost volume

- Consider M x N image
- Suppose there are D possible disparities.
- For every pixel, D possible scores
- Can be written as an M x N x D array
- To get disparity, take max along 3rd axis

Computing the NCC volume

- 1. For every pixel (x, y)
 - 1. For every disparity d
 - 1. Get normalized patch from image 1 at (x, y)
 - 2. Get normalized patch from image 2 at (x + d, y)
 - 3. Compute NCC

Computing the NCC volume

1. For every disparity d

- 1. For every pixel (x, y)
 - 1. Get normalized patch from image 1 at (x, y)
 - 2. Get normalized patch from image 2 at (x + d, y)
 - 3. Compute NCC

Assume all pixels lie at same disparity d (i.e., lie on same plane) and compute cost for each

Plane sweep stereo







NCC volume

Disparity

 Without loss of generality, assume origin is at pinhole of 1st camera



- disparity = t_x/Z
- If t_x is known, disparity gives Z
- Otherwise, disparity gives Z in units of t_x
 - Small-baseline, near depth = large-baseline, far depth



- For rectified cameras, correspondence problem is easier
- Only requires searching along a particular row.

- Given two images from two cameras with known P, can we rectify them?
 - Can we create new images corresponding to a rectified setup?



• Can we rotate / translate cameras?



Rotating cameras

$$\vec{\mathbf{x}}_{img} \equiv K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \vec{\mathbf{x}}_w$$

- Assume K is identity
- Assume coordinate system at camera pinhole

$$\vec{\mathbf{x}}_{img} \equiv \begin{bmatrix} I & \mathbf{0} \end{bmatrix} \vec{\mathbf{x}}_w \\ \equiv \begin{bmatrix} I & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{x}_w \\ 1 \end{bmatrix}$$

 $\equiv \mathbf{x}_w$

Rotating cameras

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Rotating cameras $\vec{\mathbf{x}}_{img} \equiv \begin{bmatrix} I & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{x}_w \\ 1 \end{bmatrix}$ $\vec{\mathbf{x}}_{img} \equiv \mathbf{x}_w$

• What happens if the camera is rotated? $\vec{\mathbf{x}}'_{img} \equiv \begin{bmatrix} R & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{x}_w \\ 1 \end{bmatrix}$ $\equiv R\mathbf{x}_w$ $\equiv R\vec{\mathbf{x}}_{img}$

Rotating cameras

• What happens if the camera is rotated?



• No need to know the 3D structure

Rotating cameras













