

CS4670 / 5670: Computer Vision

Kavita Bala

Lecture 21: Panoramas



Announcements

- **Prelim on Thu**
 - Everything till Lecture 17
 - Closed book
 - Bring your calculator
 - **7:30 pm, Location**
 - **Kennedy Hall, 116**

Mosaics

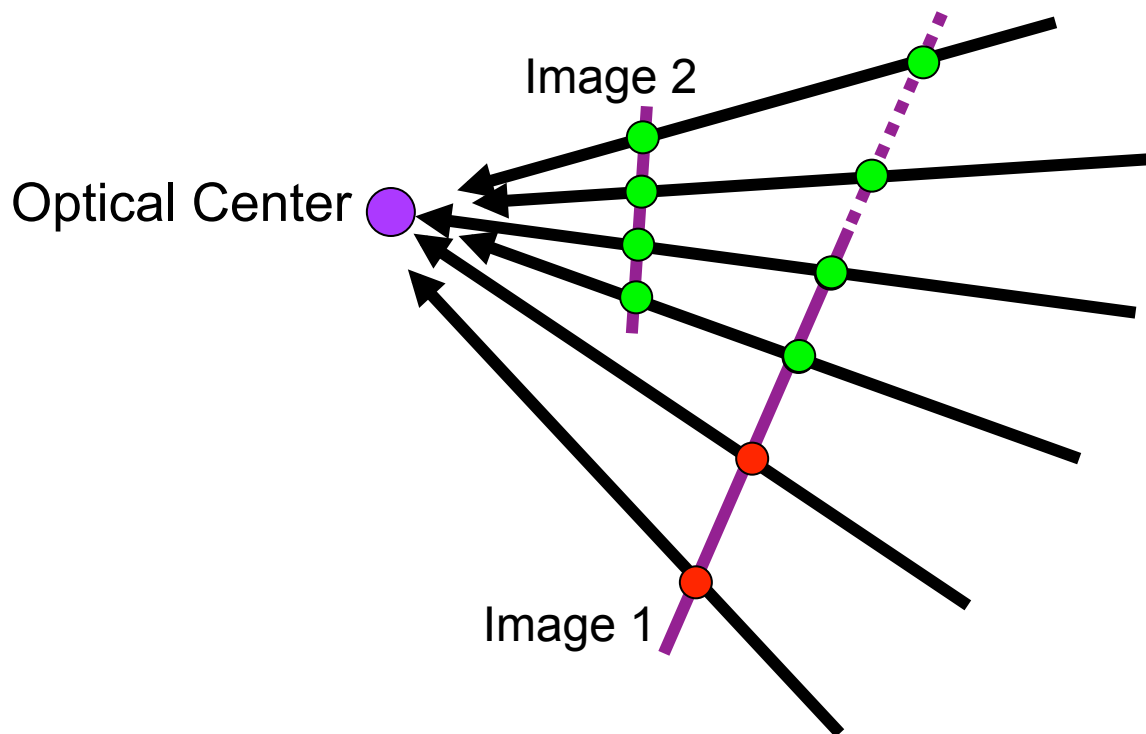


- How do we align the images?

Creating a panorama

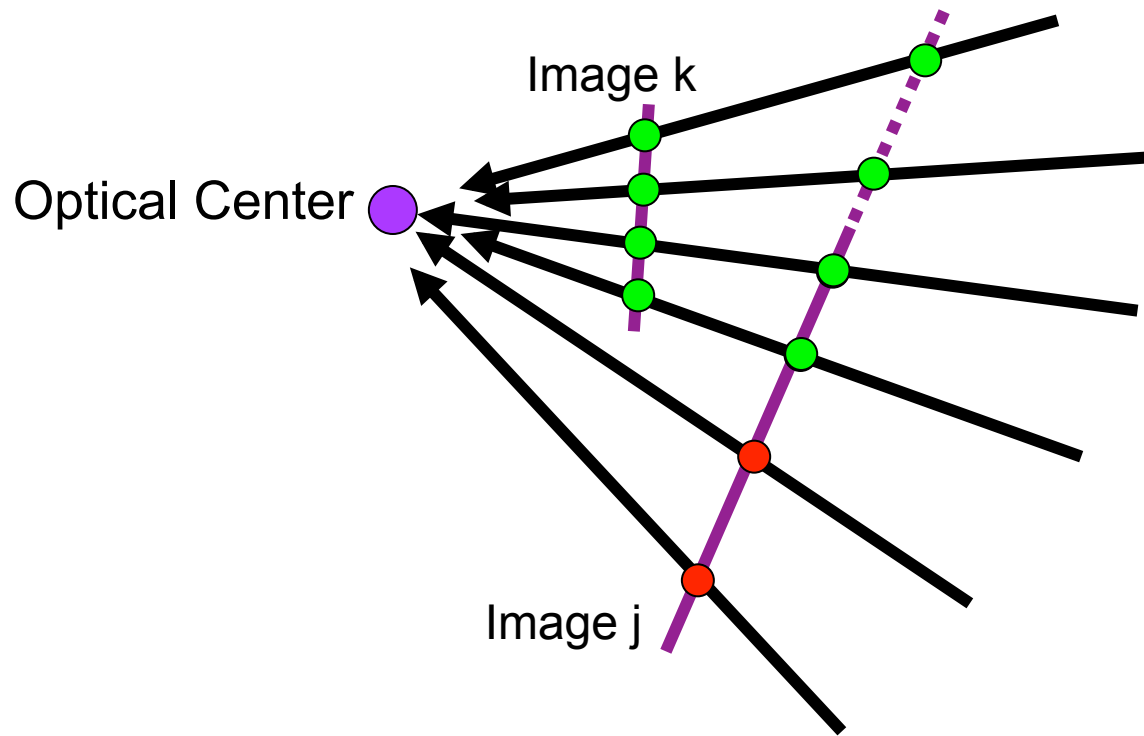
- Basic Procedure
 - Take a sequence of images from the same position
 - Rotate the camera about its optical center
 - Compute transformation between second image and first
 - Transform the second image to overlap with the first
 - Blend the two together to create a mosaic
 - If there are more images, repeat

Geometric Interpretation of Mosaics



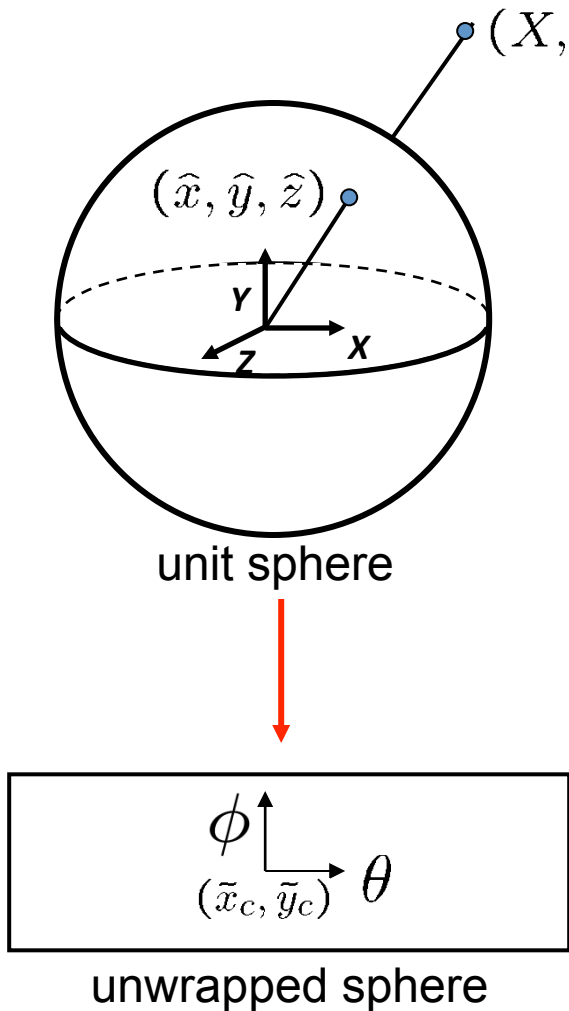
- If we capture all 360° of rays, we can create a 360° panorama
- The basic operation is *projecting* an image from one plane to another
- The projective transformation is scene-INDEPENDENT
 - This depends on all the images having the same optical center

What is the transformation?



$$\tilde{\mathbf{x}}_{ik} \sim \tilde{\mathbf{H}}_{kj} \tilde{\mathbf{x}}_{ij} = \mathbf{K}_k \mathbf{R}_k \mathbf{R}_j^{-1} \mathbf{K}_j^{-1} \tilde{\mathbf{x}}_{ij}.$$

Spherical projection



- Map 3D point (X, Y, Z) onto sphere

$$(\hat{x}, \hat{y}, \hat{z}) = \frac{1}{\sqrt{X^2 + Y^2 + Z^2}}(X, Y, Z)$$

- Convert to spherical coordinates

$$(\sin\theta\cos\phi, \sin\phi, \cos\theta\cos\phi) = (\hat{x}, \hat{y}, \hat{z})$$

- Convert to spherical image coordinates

$$(\tilde{x}, \tilde{y}) = (s\theta, s\phi) + (\tilde{x}_c, \tilde{y}_c)$$

- s defines size of the final image

» often convenient to set s = camera focal length in pixels

Spherical reprojection



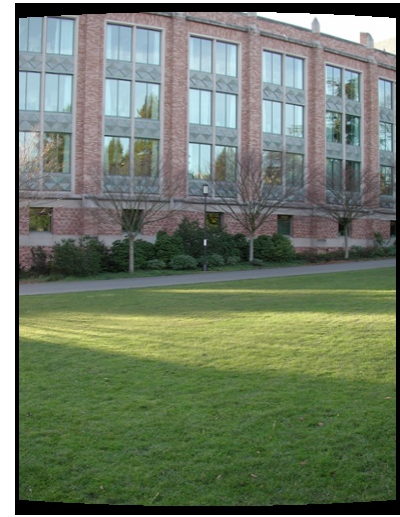
input



$f = 200$ (pixels)



$f = 400$



$f = 800$

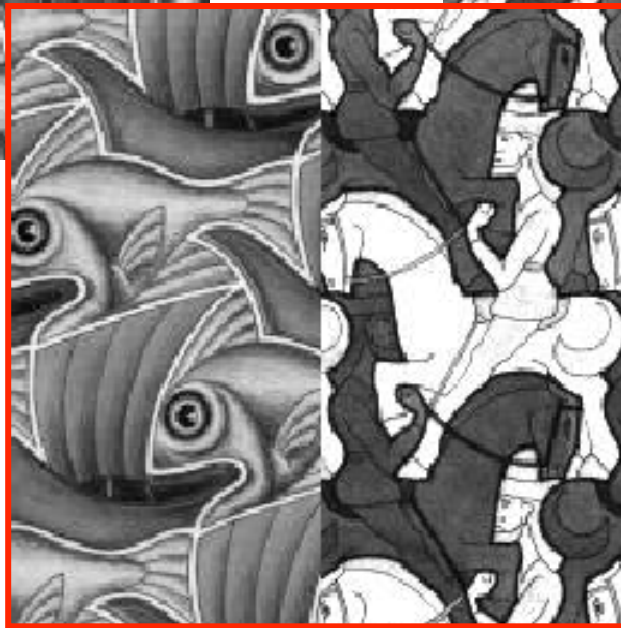
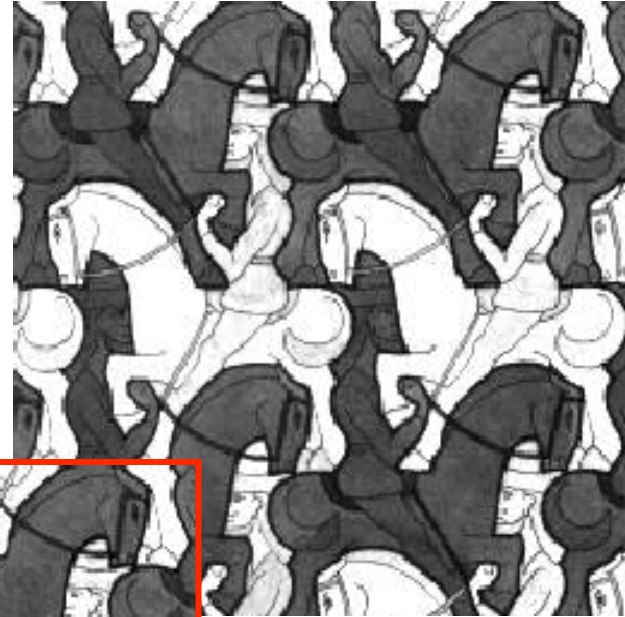
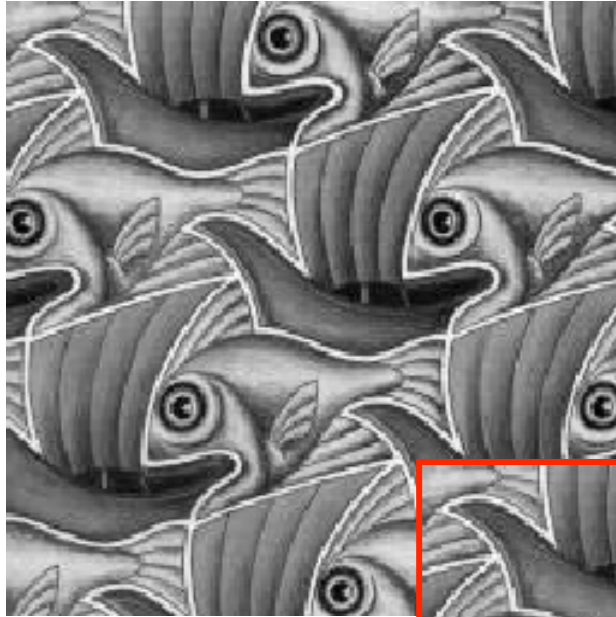
- Map image to spherical coordinates
 - need to know the focal length

Aligning spherical images

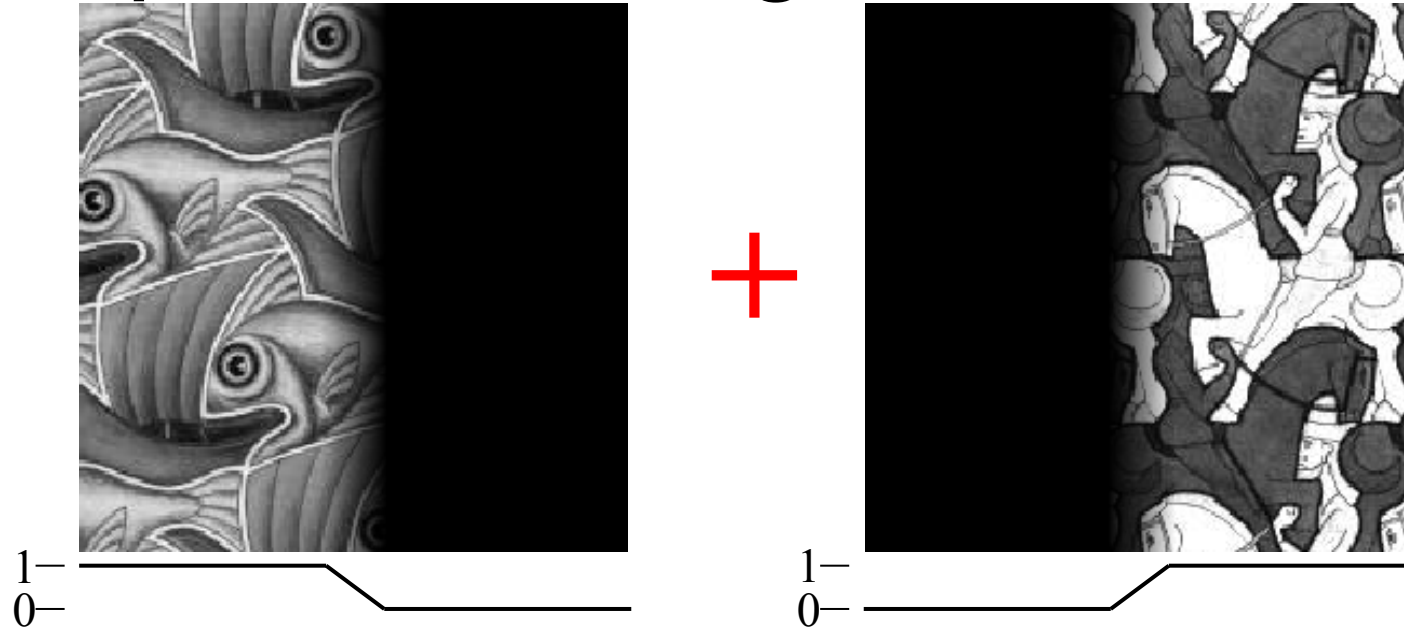


- Suppose we rotate the camera by θ about the vertical axis
 - How does this change the spherical image?
 - Translation by θ
 - This means that we can align spherical images by translation

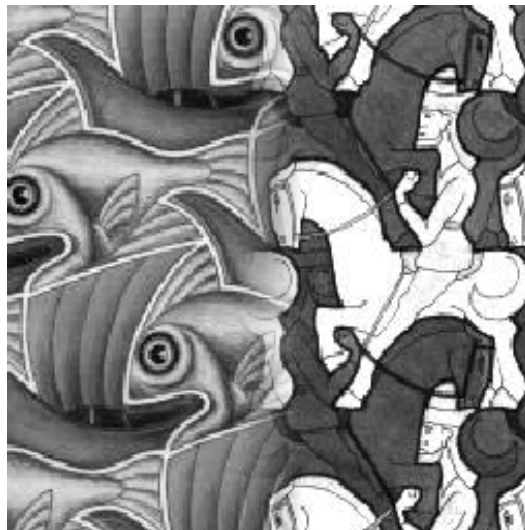
Need blending



Alpha Blending / Feathering

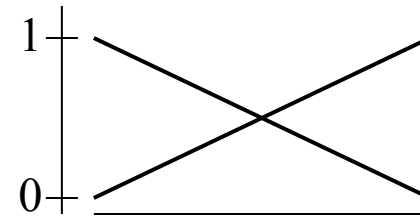
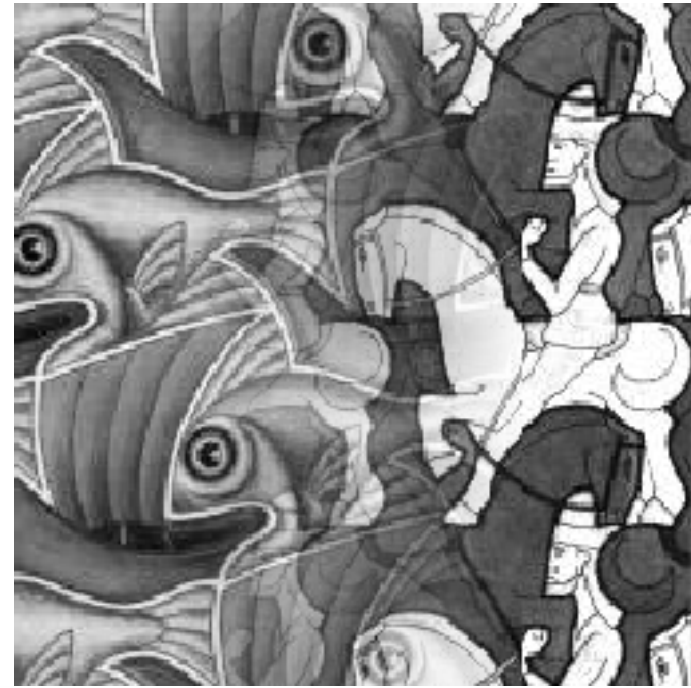
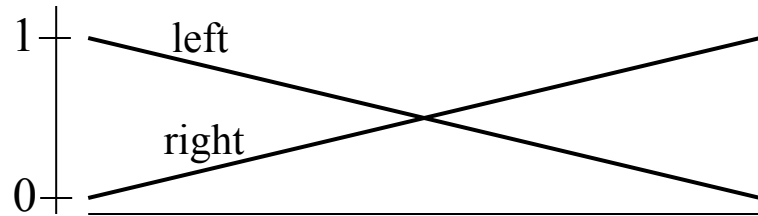
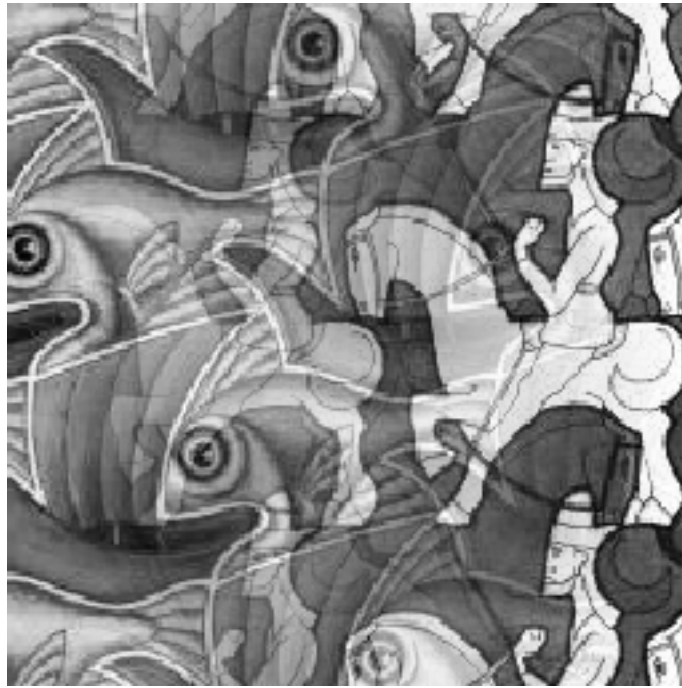


=

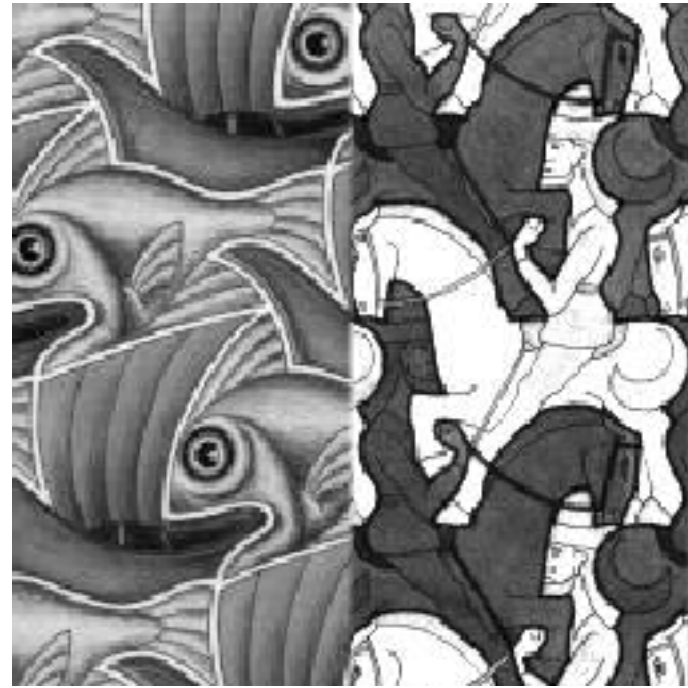
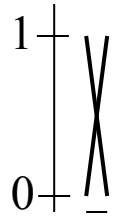
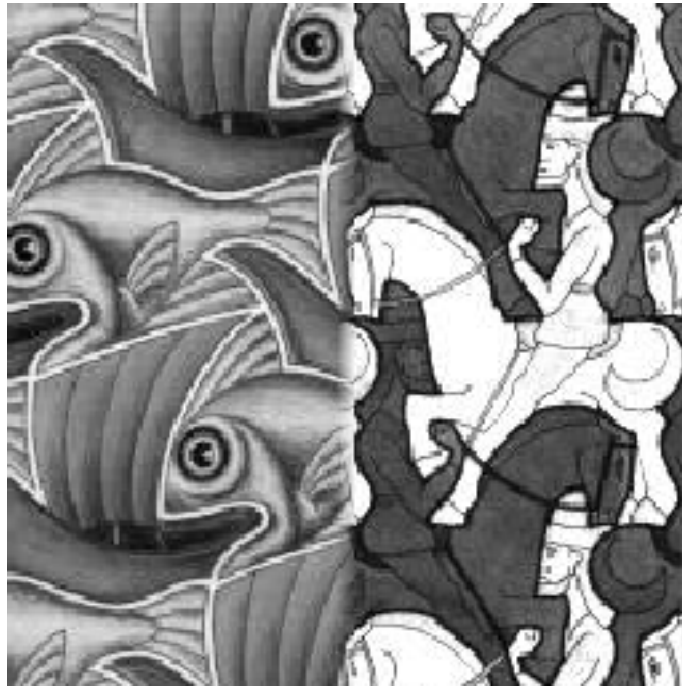


$$I_{\text{blend}} = \alpha I_{\text{left}} + (1-\alpha) I_{\text{right}}$$

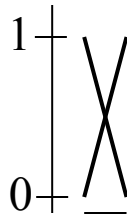
Effect of Window Size



Effect of Window Size



Good Window Size

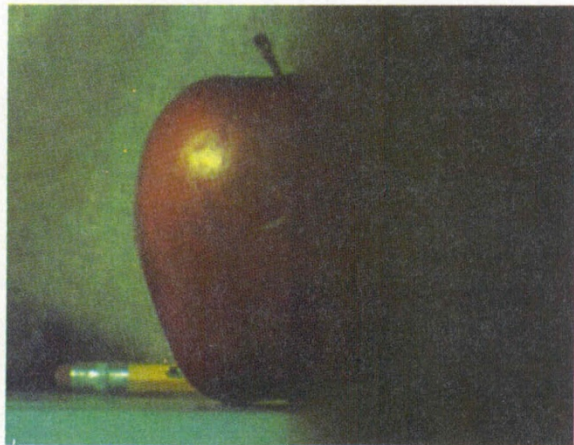
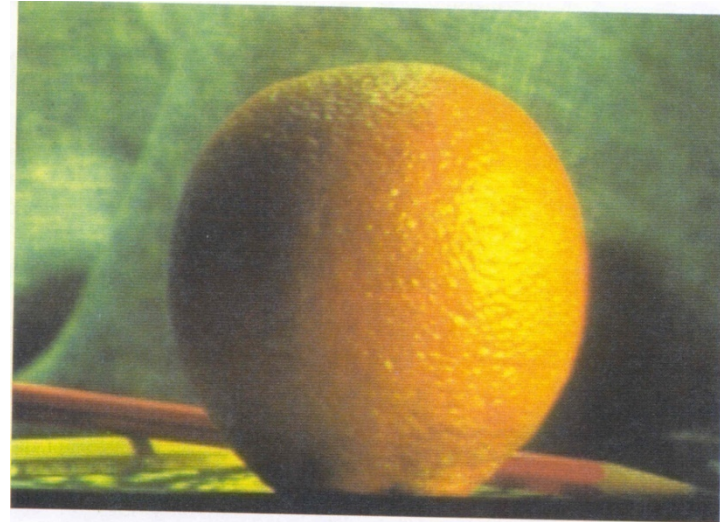
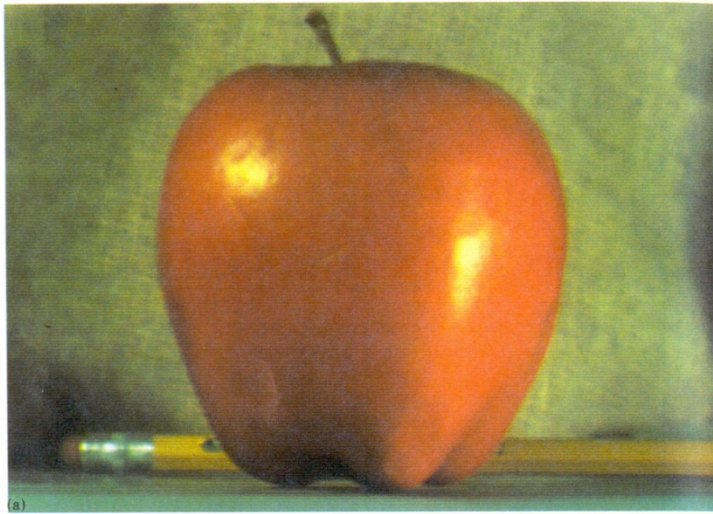


“Optimal” Window: smooth but not ghosted

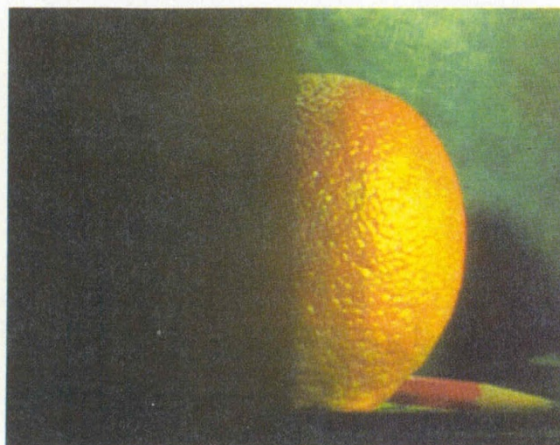
What is the optimal size?

- To avoid seams
 - Window \geq size of largest prominent feature
- To avoid ghosting
 - Window/2 \leq size of smallest prominent feature

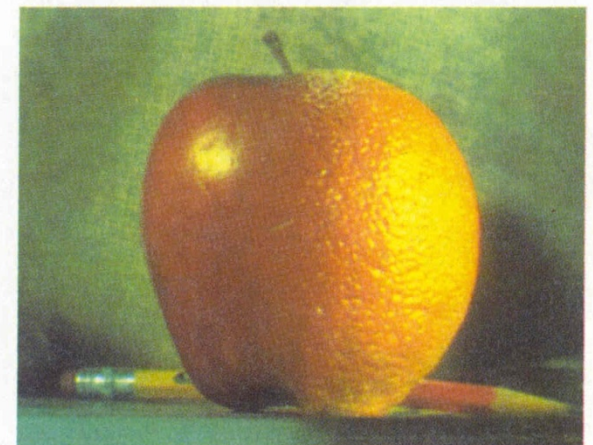
Pyramid blending



(d)



(h)

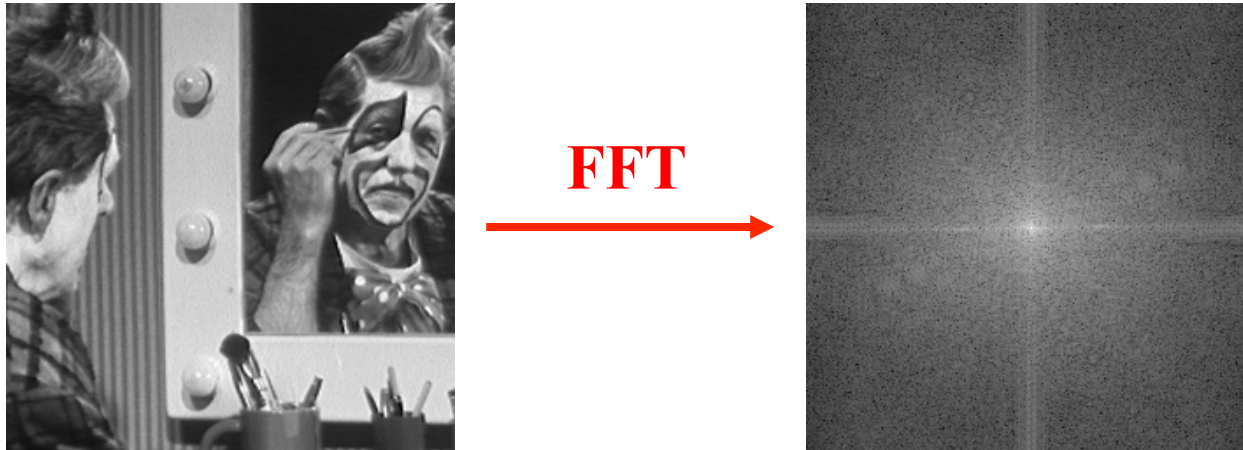


(l)

Create a Laplacian pyramid, blend each level (octave)

- Burt, P. J. and Adelson, E. H., [A multiresolution spline with applications to image mosaics](#), ACM Transactions on Graphics, 42(4), October 1983, 217-236.

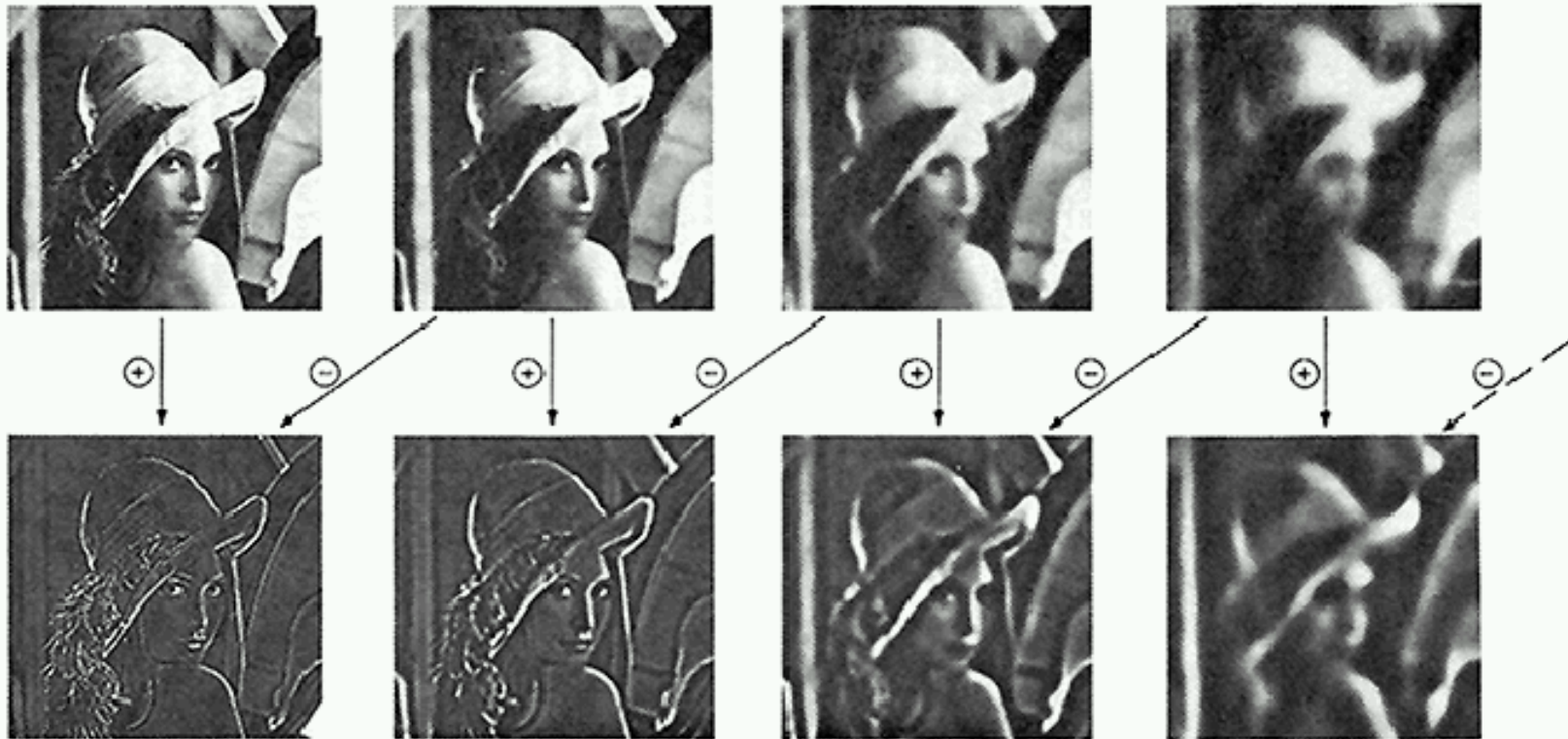
What if the Frequency Spread is Wide



- Idea (Burt and Adelson)
 - Compute $F_{\text{left}} = \text{FFT}(I_{\text{left}})$, $F_{\text{right}} = \text{FFT}(I_{\text{right}})$
 - Decompose Fourier image into octaves (bands)
 - $F_{\text{left}} = F_{\text{left}}^1 + F_{\text{left}}^2 + \dots$
 - Feather corresponding octaves F_{left}^i with F_{right}^i
 - Can compute inverse FFT and feather in spatial domain
 - Sum feathered octave images in frequency domain
- Better implemented in *spatial domain*

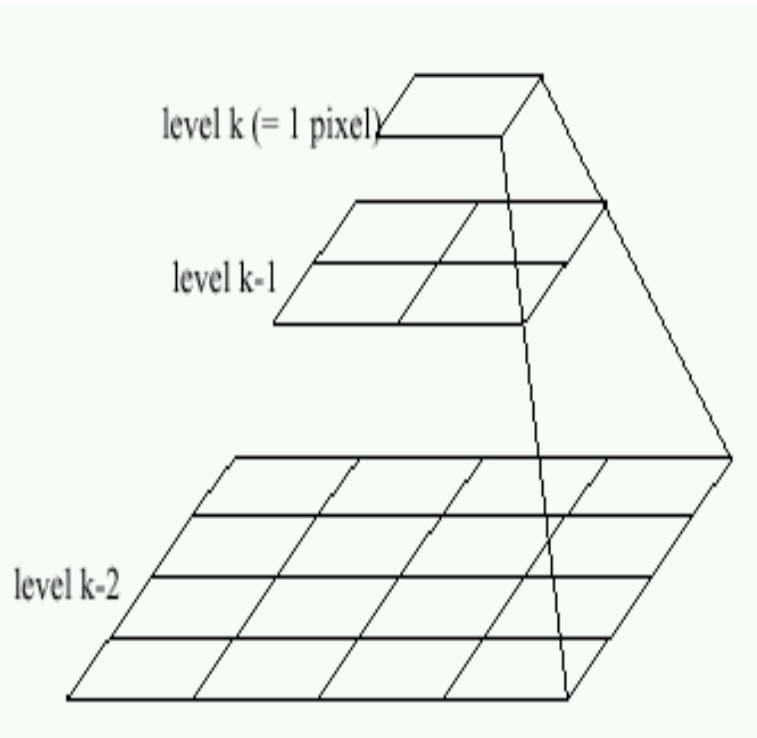
Octaves in the Spatial Domain

Lowpass Images

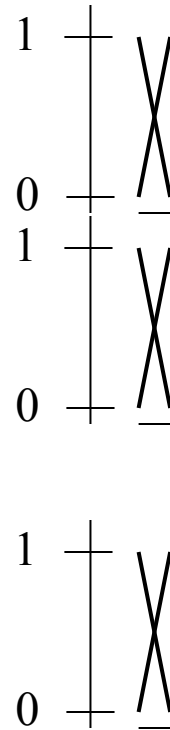


- Bandpass Images

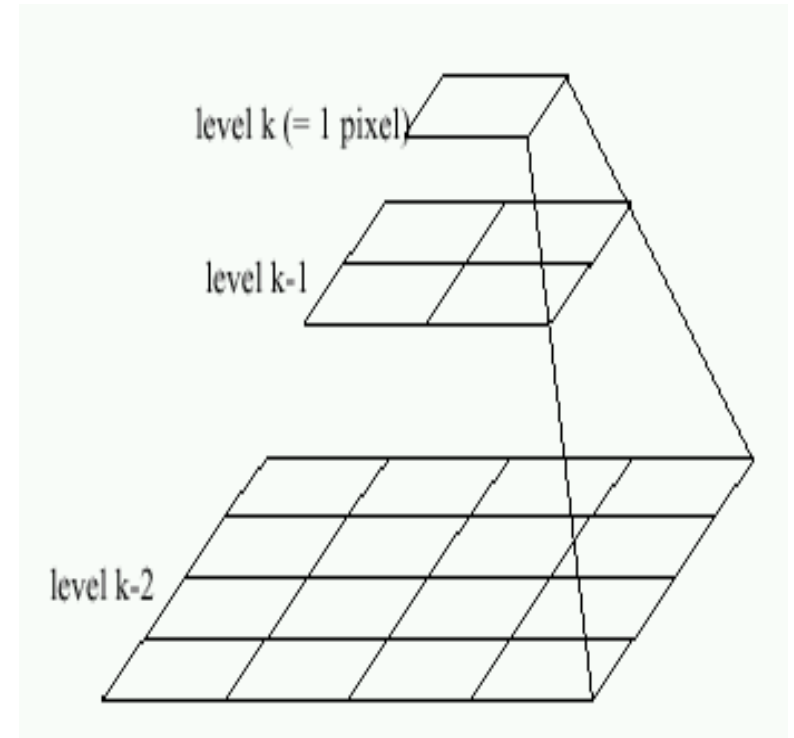
Pyramid Blending



Left pyramid

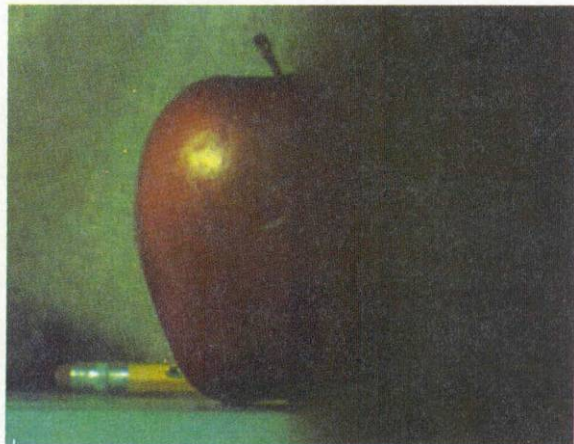
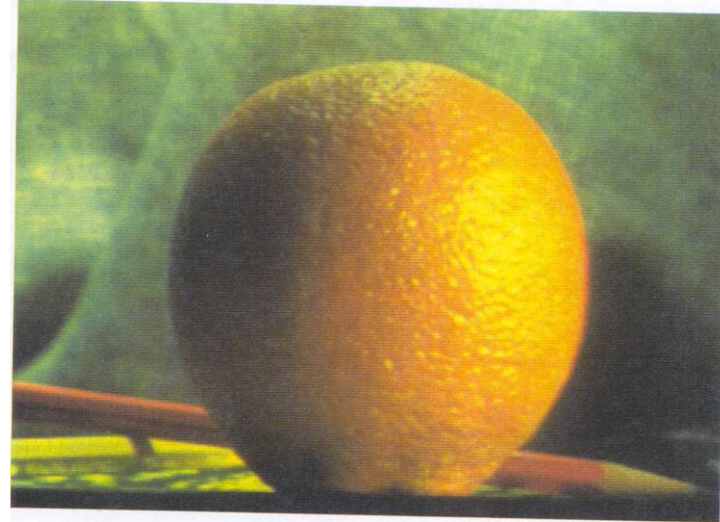
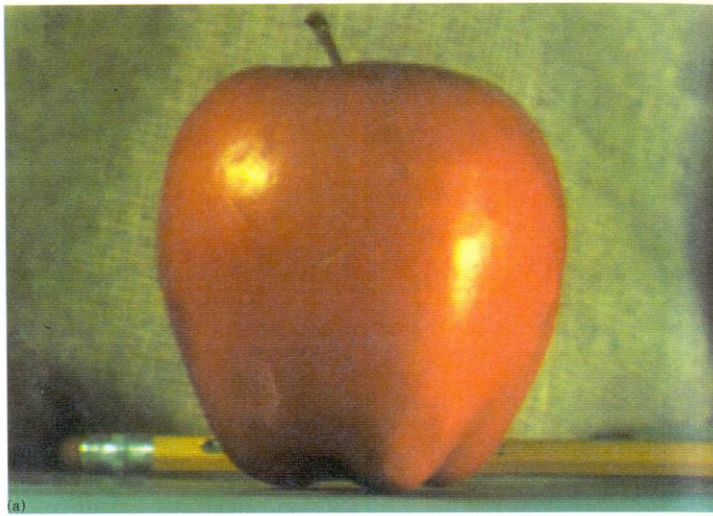


blend

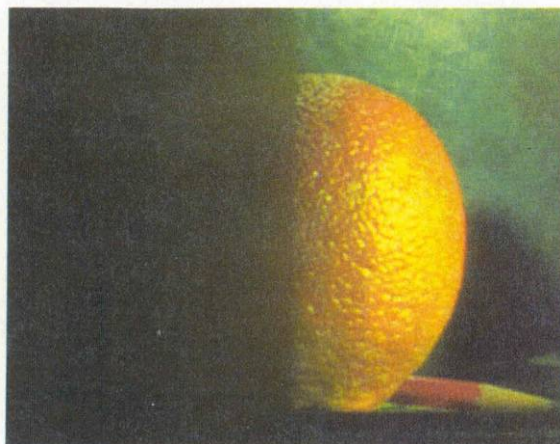


Right pyramid

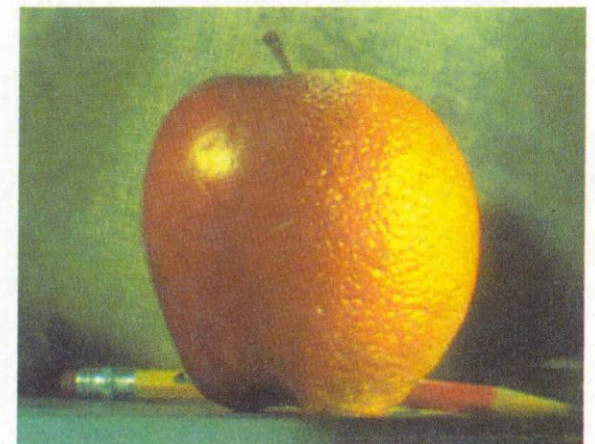
Pyramid Blending



(d)

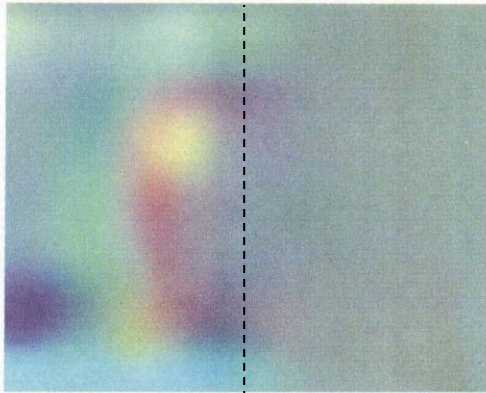


(h)

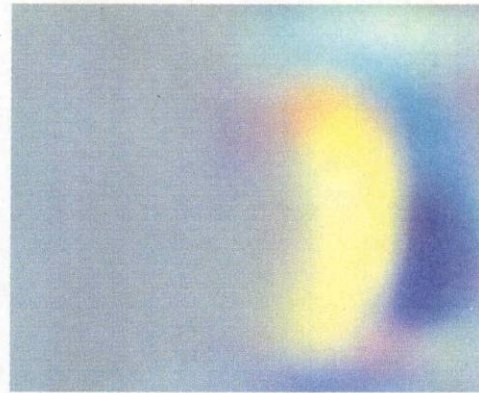


(l)

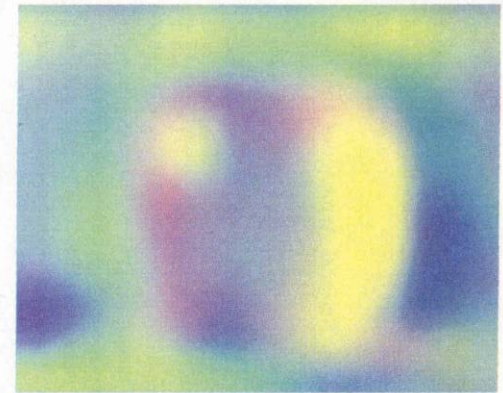
laplacian
level
4



(c)

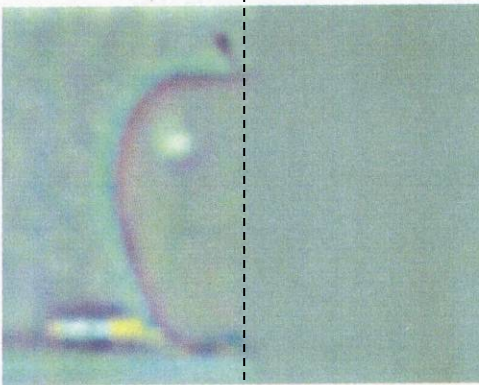


(g)

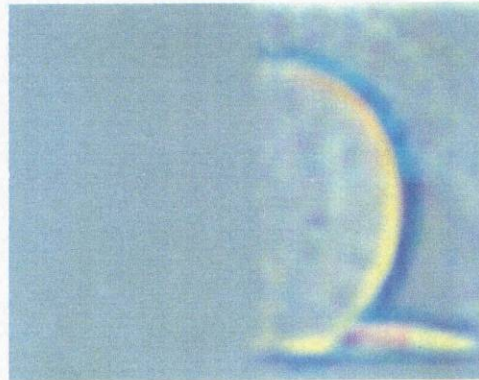


(k)

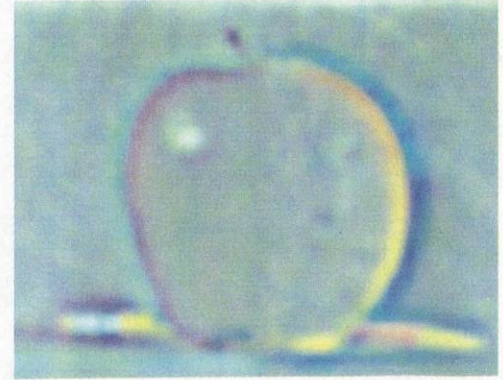
laplacian
level
2



(b)

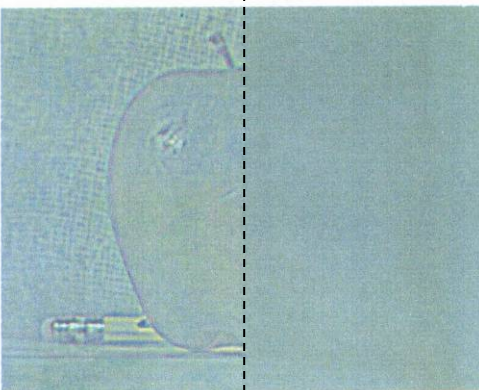


(f)

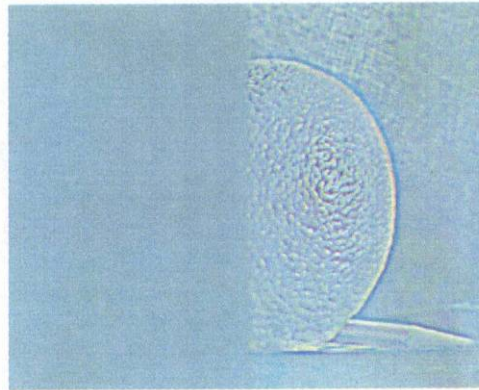


(j)

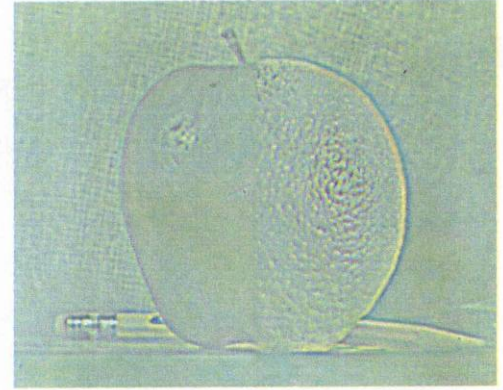
laplacian
level
0



(a)



(e)



(i)

left pyramid

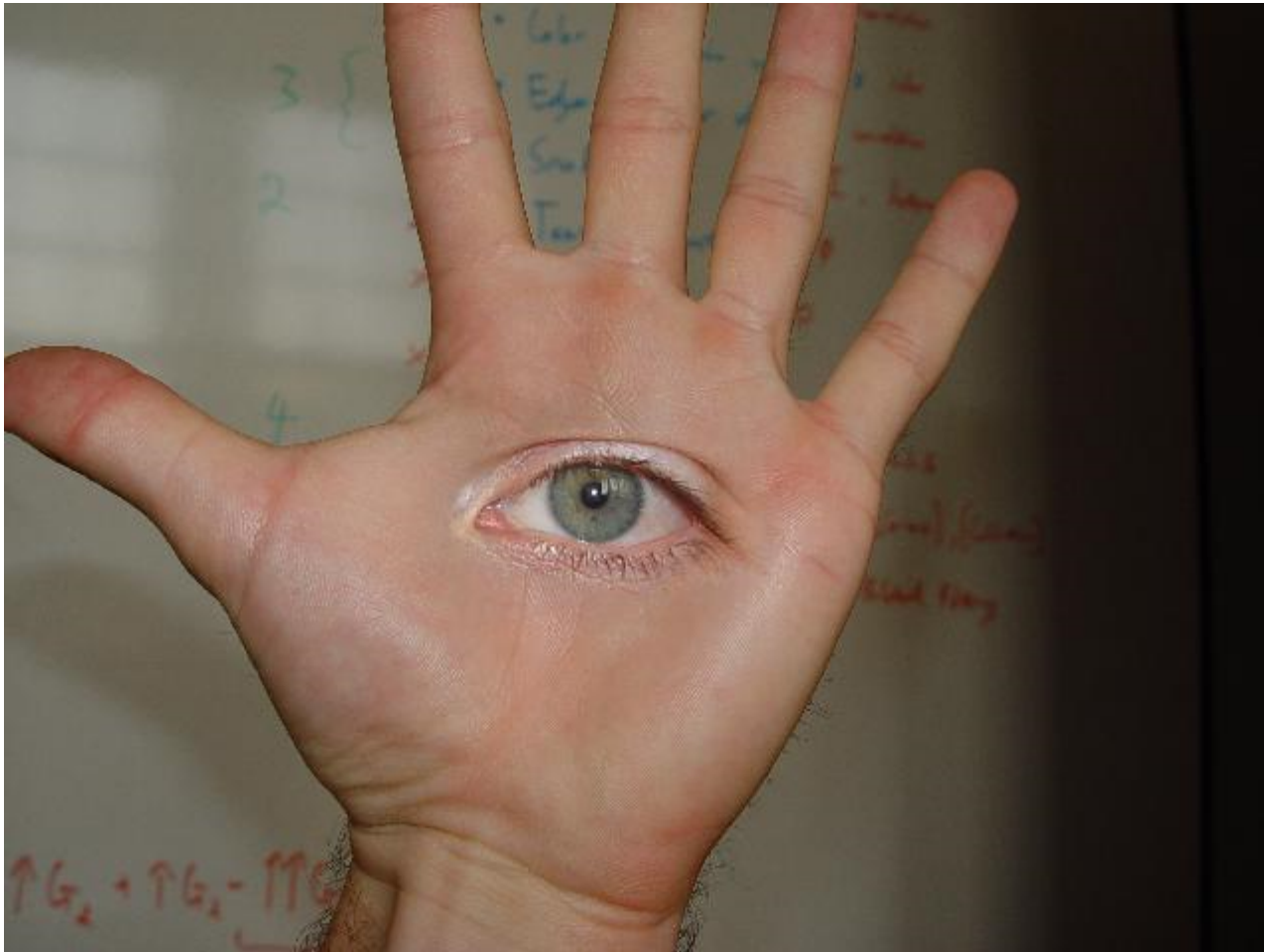
right pyramid

blended pyramid

Blending Regions



Horror Photo



© david dmartin (Boston College)

Simplification: Two-band Blending

- Brown & Lowe, 2003
 - Only use two bands: high freq. and low freq.



2-band Blending



Low frequency ($\lambda > 2$ pixels)



High frequency ($\lambda < 2$ pixels)

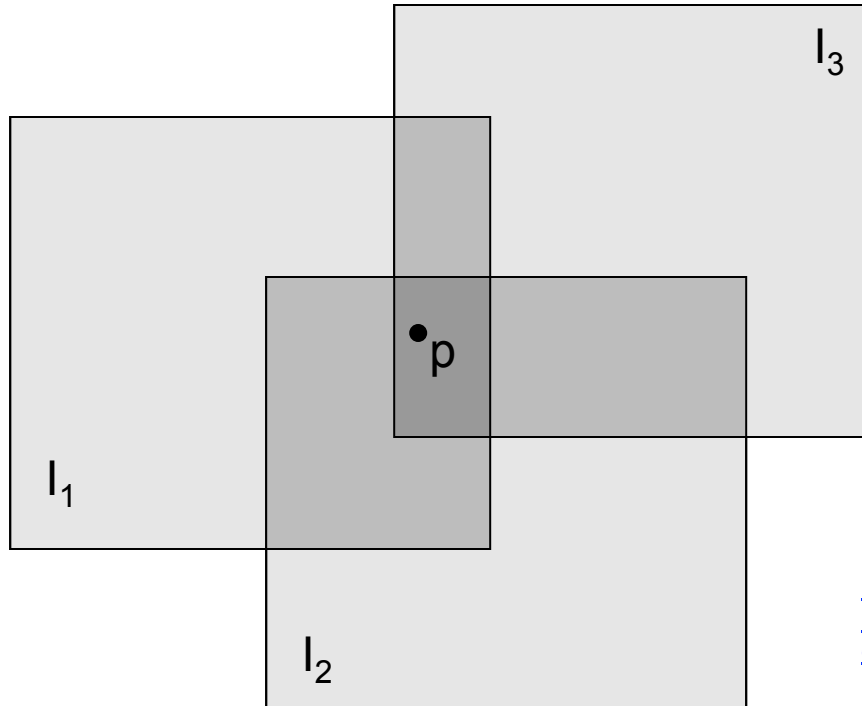
Linear Blending



2-band Blending



Alpha Blending



Optional: see Blinn (CGA, 1994) for details:

<http://ieeexplore.ieee.org/iel1/38/7531/00310740.pdf?isNumber=7531&prod=JNL&arnumber=310740&arSt=83&ared=87&arAuthor=Blinn%2C+J.F.>

Encoding blend weights: $I(x,y) = (\alpha R, \alpha G, \alpha B, \alpha)$

color at $p = \frac{(\alpha_1 R_1, \alpha_1 G_1, \alpha_1 B_1) + (\alpha_2 R_2, \alpha_2 G_2, \alpha_2 B_2) + (\alpha_3 R_3, \alpha_3 G_3, \alpha_3 B_3)}{\alpha_1 + \alpha_2 + \alpha_3}$

Implement this in two steps:

1. accumulate: add up the (α premultiplied) RGB α values at each pixel
2. normalize: divide each pixel's accumulated RGB by its α value

Q: what if $\alpha = 0$?

Project 3

- Take pictures on a tripod (or handheld)
- Warp to spherical coordinates (optional if using homographies to align images)
- Extract features
- Align neighboring pairs using RANSAC
- Write out list of neighboring translations
- Blend the images
- Correct for drift
- Now enjoy your masterpiece!

Some panorama examples

- Every image on Google Streetview



Other types of mosaics



- Can mosaic onto *any* surface if you know the geometry
 - See NASA's [Visible Earth project](http://earthobservatory.nasa.gov/Newsroom/BlueMarble/) for some stunning earth mosaics
 - <http://earthobservatory.nasa.gov/Newsroom/BlueMarble/>
 - Click for [images...](#)

- <https://t.co/qean7Alb7p>

Don't blend, CUT!



Moving objects become ghosts

- So far we only tried to blend between two images. What about finding an optimal seam?

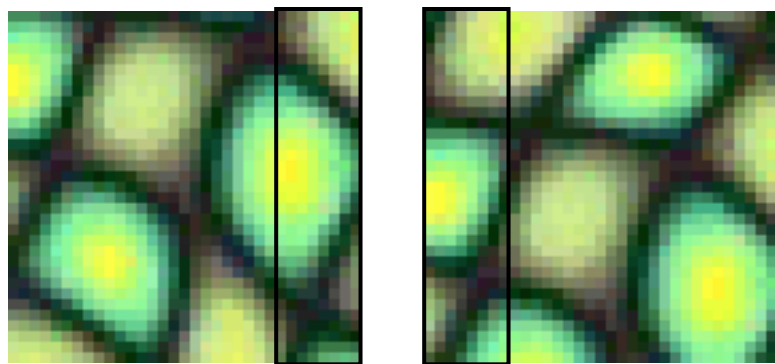
Davis, 1998

- Segment the mosaic
 - Single source image per segment
 - Avoid artifacts along boundaries
 - Dijkstra's algorithm

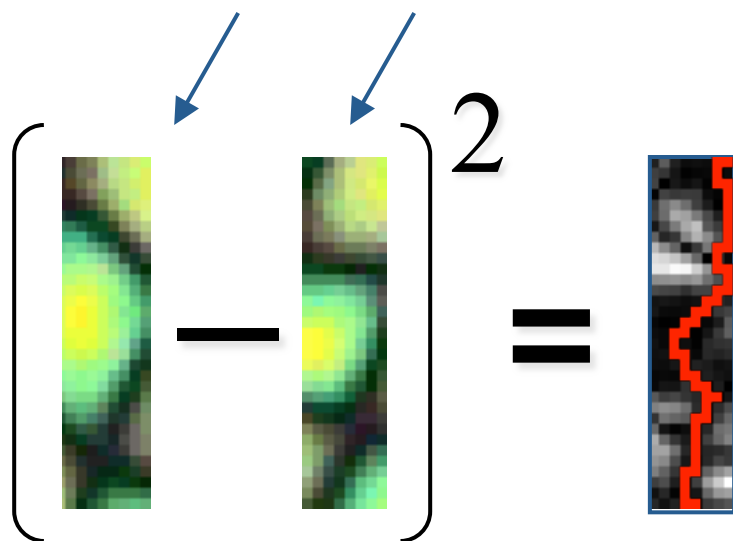
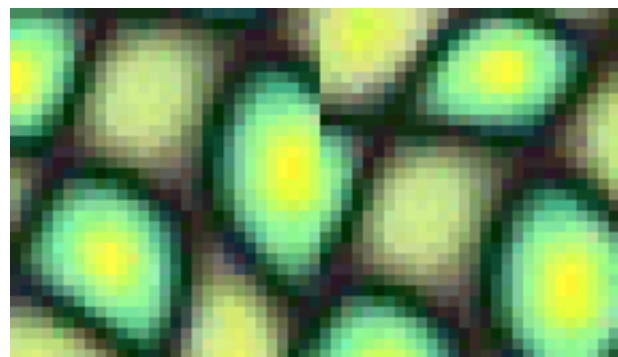


Minimal error boundary

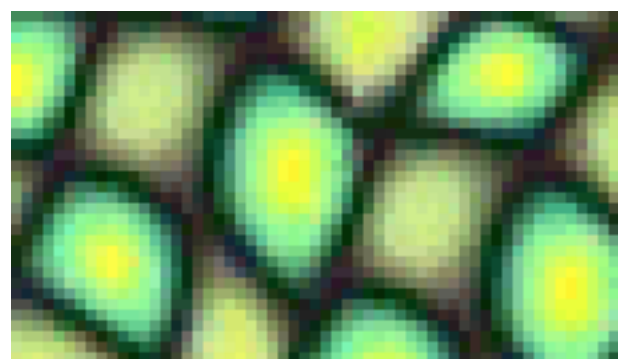
overlapping blocks



vertical boundary



overlap error



min. error boundary

Seam Carving

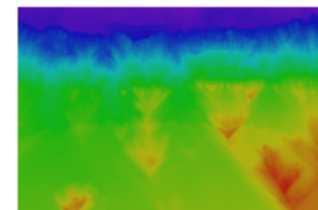
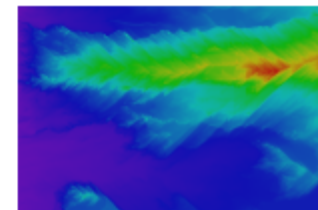
Seam Carving for Content-Aware Image Resizing

Shai Avidan

Mitsubishi Electric Research Labs

Ariel Shamir

The Interdisciplinary Center & MERL

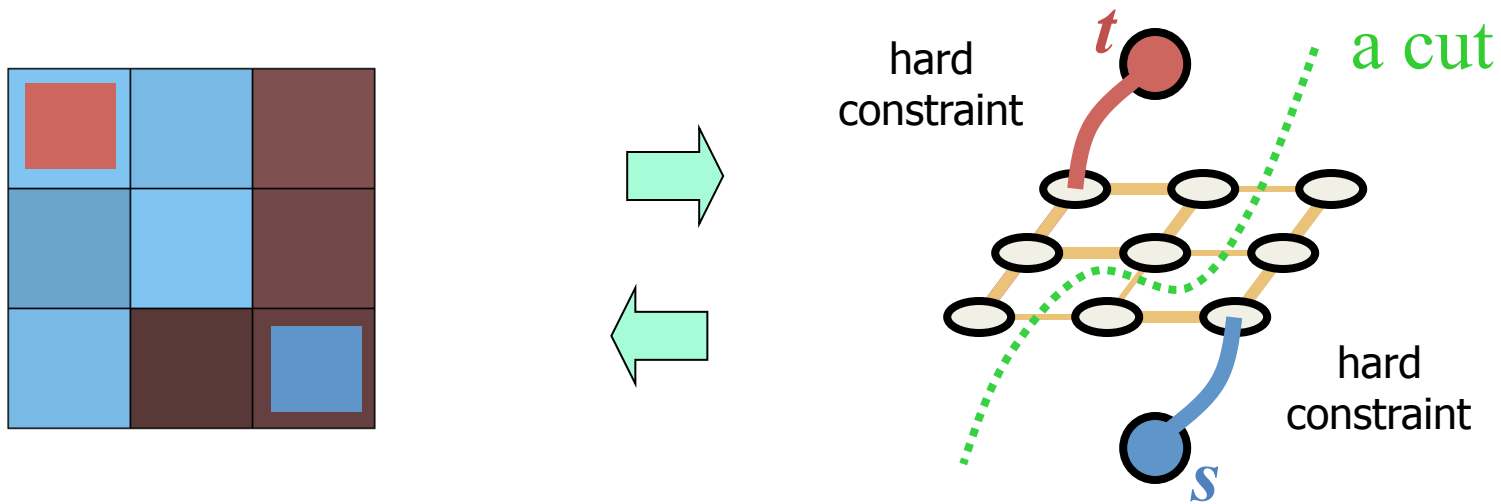


Graphcuts

- What if we want similar “cut-where-things-agree” idea, but for closed regions?
 - Dynamic programming can't handle loops

Graph cuts

(simple example à la Boykov&Jolly, ICCV' 01)



Minimum cost cut can be computed in polynomial time
(max-flow/min-cut algorithms)

Kwatra et al, 2003



Actually, for this example, DP will work just as well...

Lazy Snapping



(a) Girl (4/2/12)

(b) Ballet (4/7/14)

(c) Boy (6/2/13)



(c) Grandpa (4/2/11)

(d) Twins (4/4/12)

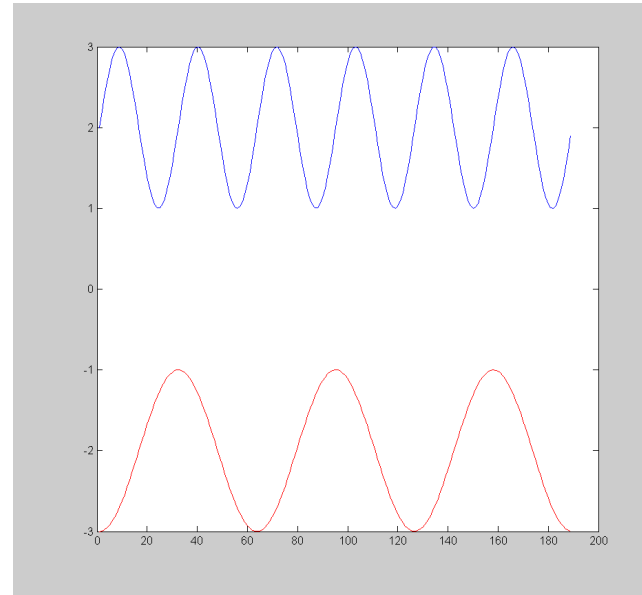
Interactive segmentation using graphcuts

Gradient Domain

- In Pyramid Blending, we decomposed our image into 2nd derivatives (Laplacian) and a low-res image
- Let us now look at 1st derivatives (gradients):
 - No need for low-res image
 - captures everything (up to a constant)
 - Idea:
 - Differentiate
 - Blend
 - Reintegrate

Gradient Domain blending (1D)

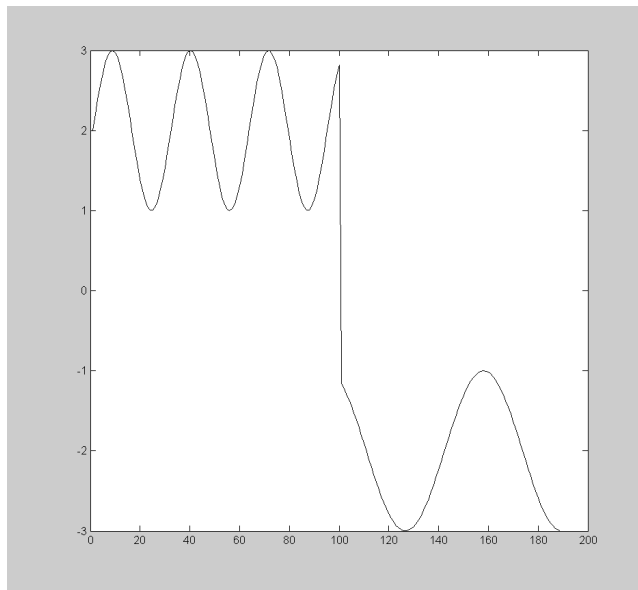
Two signals



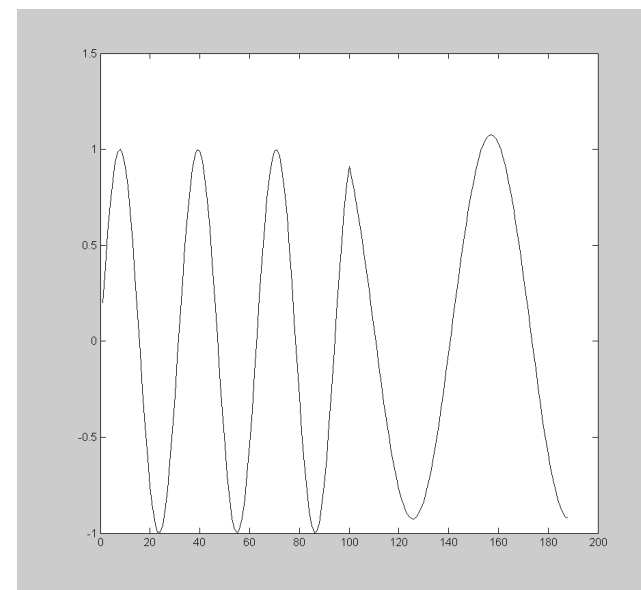
bright

dark

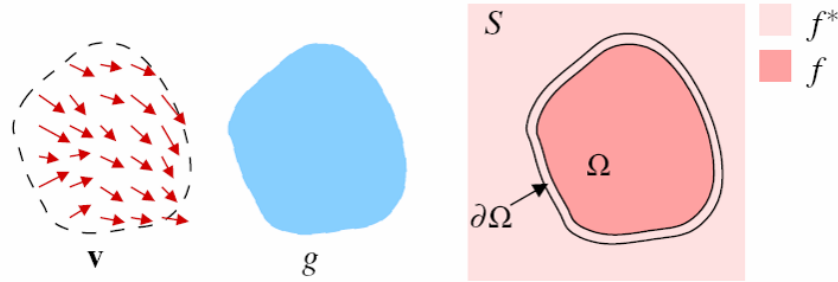
Regular blending



Blending derivatives



Gradient Domain Blending (2D)



- Trickier in 2D:
 - Take partial derivatives dx and dy (the gradient field)
 - Edit (smooth, blend, feather, etc)
 - Reintegrate
 - Find the most agreeable solution
 - Equivalent to solving Poisson equation
 - Can use FFT, deconvolution, multigrid solvers, etc.

Perez et al., 2003

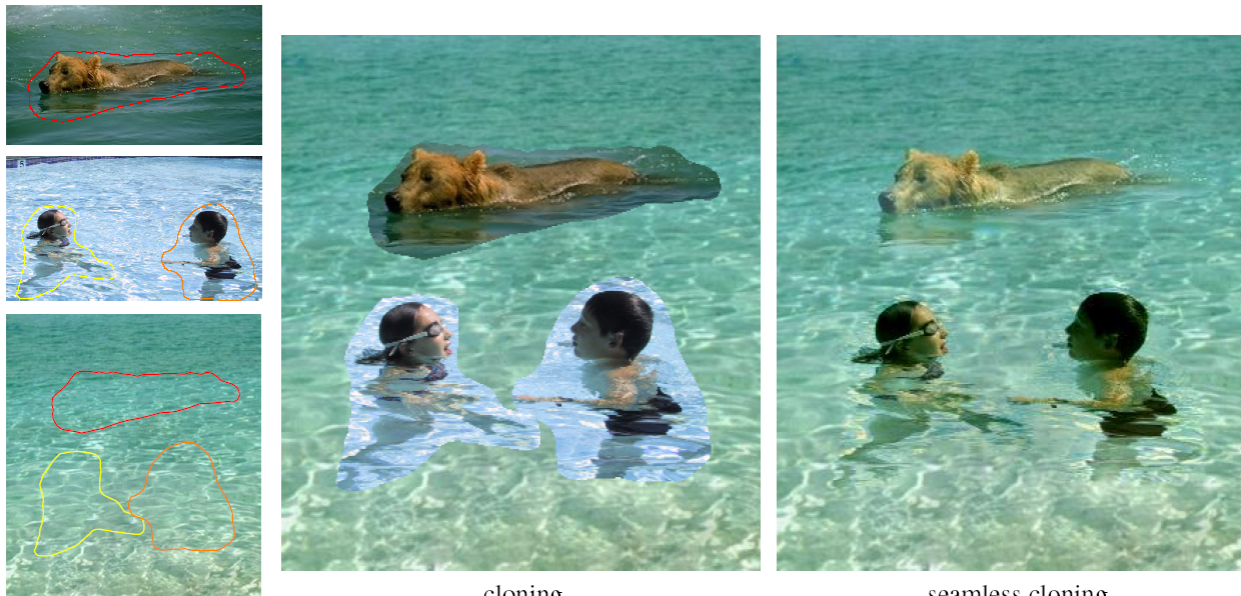


sources

destinations

cloning

seamless cloning

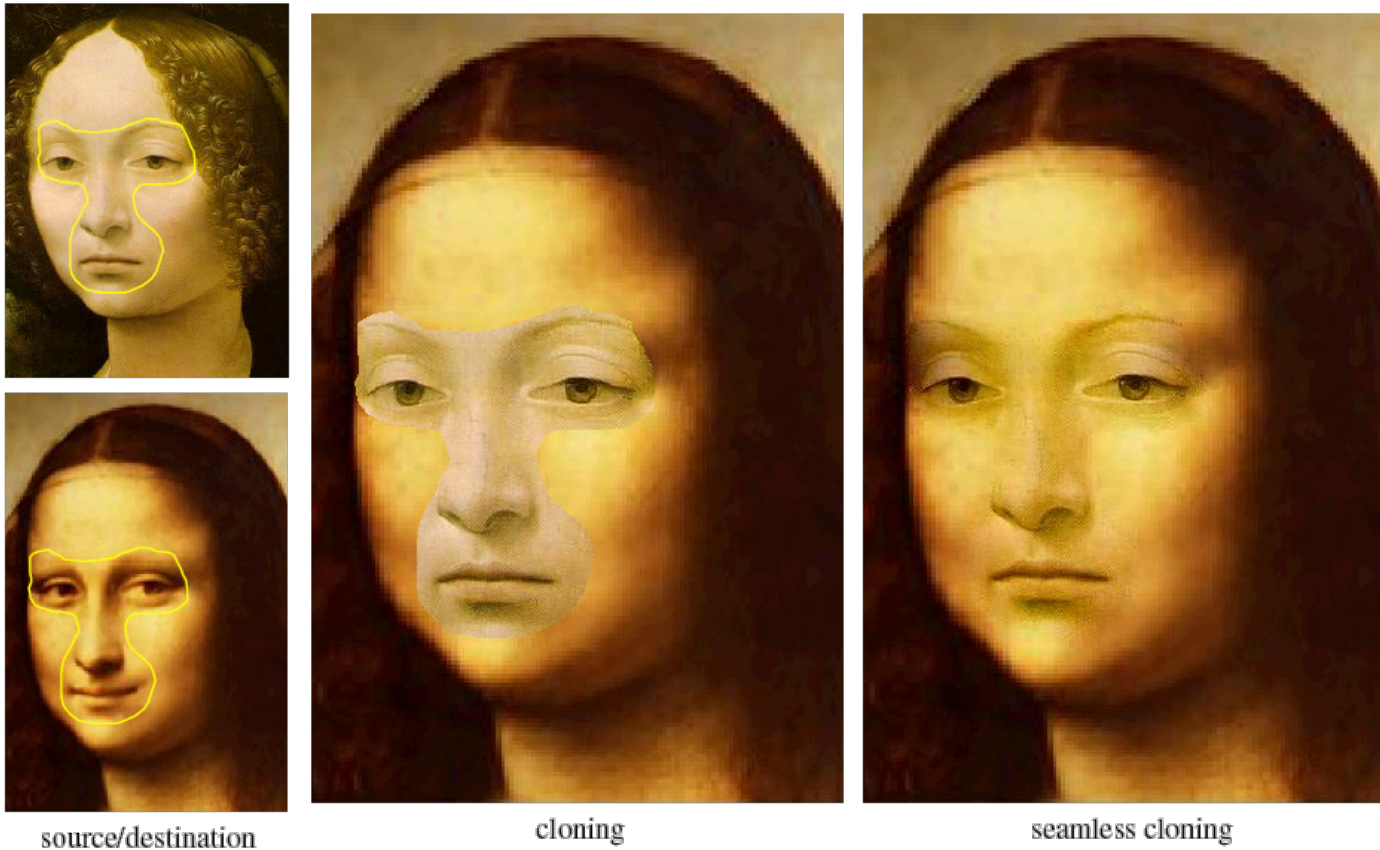


sources/destinations

cloning

seamless cloning

Perez et al, 2003



- Limitations:
 - Images need to be very well aligned

Putting it all together

- Compositing images
 - Have a clever blending function
 - Feathering
 - Blend different frequencies differently
 - Gradient based blending
 - Choose the right pixels from each image
 - Dynamic programming – optimal seams
 - Graph-cuts
- Now, let's put it all together:
 - Interactive Digital Photomontage, 2004 (video)

Interactive Digital Photomontage



Aseem Agarwala, Mira Dontcheva
Maneesh Agrawala, Steven Drucker, Alex Colburn
Brian Curless, David Salesin, Michael Cohen

