Name:	First Name:	Cornell NetID:
(CS 4620 Midterm, October 21, 2	2014
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1. [20 points] Ray Intersection.

Consider a scene with a sphere and a triangle. The sphere's center is at (0,0,0) and its radius is 1. UV coordinates of the sphere are the same as in assignment 1.

The triangle has vertices (2,0,0), (0,2,0), and (0,0,2). The camera (ray origin) is at $(\sqrt{3},\sqrt{3},\sqrt{3})$ and the ray direction is $(-\frac{1}{\sqrt{3}},-\frac{1}{\sqrt{3}},-\frac{1}{\sqrt{3}})$.

Please answer the following questions. The answers can be unreduced—they can be in terms of square roots, fractions, and (inverse) trigonometric functions.

(a) Does the ray intersect the sphere? If yes, what data (position, normal, and t) would be put in the intersection record? If not, why?

(b) Does the ray intersect the triangle? If yes, what data would be put in the intersection record? If not, why?

(c) Which intersection record, if any, would be used in a subsequent shading computation? Why?

The North pole of the earth is at (0,1,0). The South pole is at (0,-1,0). And points on the Greenwich meridian have coordinates (0,y,z) with z>0. The texture coordinate u depends only on longitude, with u=0 at longitude 180° West and u=1 at 180° East. v depends only on latitude, with v=0 at the South pole and v=1 at the North pole.

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2. [16 points] **Transformation Matrices**. Consider the following matrices representing transformations on 3D points in homogeneous coordinates.

$$A = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0.5 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} B = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 2 \end{bmatrix} C = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} D = \begin{bmatrix} \frac{\sqrt{3}}{2} & 0 & \frac{1}{2} & 0 \\ 0 & 1 & 0 & 0 \\ -\frac{1}{2} & 0 & \frac{\sqrt{3}}{2} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- (a) Describe the transformation of each one of the matrices above (e.g. X represents a rotation by Y degrees, etc.), using the categories: scale, translation, rotation, projection.
- (b) What matrix would you use to rotate 30° clockwise around the y-axis.
- (c) Suppose you wanted to undo the effect of BA. Write a single matrix that can achieve such a result.
- (d) Is it possible to write a matrix to $undo\ C$? (explain, in your own words, why that is the case)

Question:	1	2	3	4	5	Total
Points:	20	16	24	20	20	100
Score:						

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3. [24 points] Meshes

Suppose we are given the geometry (an octahedron) shown in Figure 1, and the following position buffer containing floating point data:

Here are three possible index buffers (containing integer data) that correspond to the octahedron. For each, please state whether the specification will give the correct output. If not, please explain what went wrong and fix it by crossing out and rewriting some of the numbers.

1.
$$\{0, 1, 2, 0, 2, 3, 0, 3, 4, 0, 4, 1, 2, 0, 1, 3, 0, 2, 4, 0, 3, 1, 0, 4\}$$

$$2. \{2, 0, 1, 2, 3, 0, 2, 5, 3, 2, 1, 5, 4, 0, 1, 4, 1, 5, 4, 5, 3, 4, 3, 0\}$$

$$3. \{1, 2, 0, 1, 0, 4, 1, 4, 5, 1, 5, 2, 3, 4, 0, 3, 0, 2, 3, 2, 5, 3, 5, 4\}$$

Now suppose we take this same mesh and duplicate a few of the vertices. Our position buffer now becomes:

$$\{0.0,\ 1.0,\ 0.0,\ 0.0,\ 1.0,\ 0.0,\ 0.0,\ 1.0,\ 0.0,\ 0.0,\ 1.0,\ 0.$$

And our index buffer is:

$$\{0, 4, 6, 1, 6, 7, 2, 7, 8, 3, 8, 5, 9, 6, 4, 10, 7, 6, 11, 8, 7, 12, 5, 8\}$$

Let's add texture coordinates to our new mesh. Below are two different texture coordinate buffers. For each, please match it with the corresponding mesh layout in UV-space (Figure 2), as well as the corresponding final renderings (Figure 3).

The answer for each part on this page consists of a number (to describe which UV layout corresponds) and a letter (to describe which pair of renderings corresponds). For instance, "UV Layout 1 and Rendering A" could be an answer.

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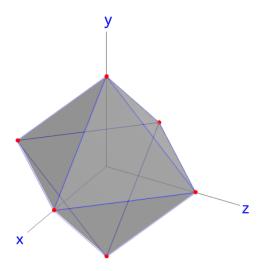


Figure 1: The target mesh configuration.

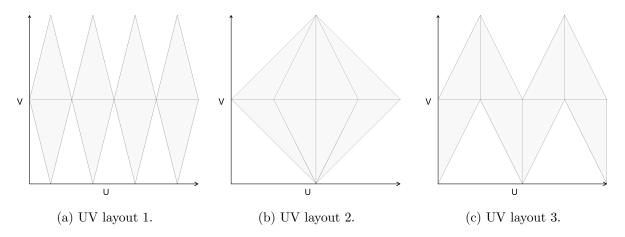
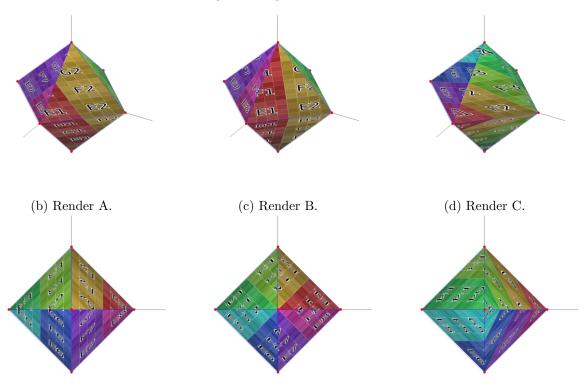


Figure 2: Layouts of the mesh in UV-space.



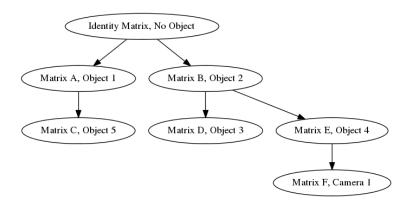
(a) The texture used in the following renderings.



- (e) Render A, top-down view.
- (f) Render B, top-down view.
- (g) Render C, top-down view.

Figure 3: Views of the rendered mesh. Pictures in the same column have the same UV layout but a different camera location; the bottom row is a top-down view of the mesh.

4. [20 points] **Scene hirearchy** Consider the following simple scene graph. Each node is given with its corresponding local transformation matrix and object pair.



- (a) Fill in the blank: In the standard scene graph model, the matrix *D* takes coordinates in _______'s frame to coordinates in ________'s frame.
- (b) What is the associated M_{model} matrix, that brings object-space coordinates to world-space coordinates, for...
 - (a) Object 1:
- (b) Object 3:
- (c) Camera 1:
- (c) Suppose we are currently using Camera 1, which is a perspective camera that uses the perspective projection matrix M_{per1} and the viewport transformation M_{vp} . Unfortunately, all of our geometry is currently described in Object 5's frame. Say we wanted to view our geometry on a screen. How should we transform \vec{p} (given in Object 5's frame) such that \vec{p} ends up on our screen? Your solution should be of the form $X\vec{p}$ where X is a composition of several matrices. Additionally, include a sentence or two explaining how $X\vec{p}$ gets us screen coordinates.

- (d) Suppose during the coordinate change described in the previous question, we'd like to translate point p by 5 units in the +y direction. This is somewhat ambiguious, because we don't know which frame this transformation takes place in. How should we transform \vec{p} (again as an expression $X\vec{p}$) if we want this to occur in...
 - i. In world space?
 - ii. In Object 2's space?

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5. [20 points] Ray tracer bugs		
Look at each of the five images i	in Figure 5 that were pr	roduced by a Ray I ray tracer with

various bugs. For each one choose one of the three possible explanations for the bug:

- i. The error is caused by a problem with ray generation.
- ii. The error is caused by a problem with ray intersection.
- iii. The error is caused by a problem with shading computations.

For each choice, back it up with an example of an error that would cause the observed symptoms. There is no right or wrong explanation; only plausible and implausible ones. But when there is a clearly plausible cause, very far-fetched explanations will not make full credit. Shadow computations and texture operations count as part of shading. Computing surface normals counts as part of ray intersection. The first one is done as an example.

(a) iii. The problem is that the texture is flipped along the v axis, which could be caused by the texture mapping code failing to reverse the y coordinate when indexing into the texture image.

(b)

(c)

(d)

(e)

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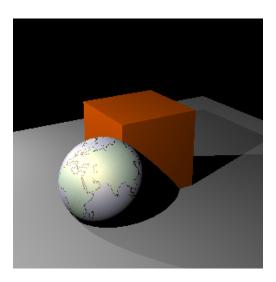


Figure 4: The correct rendering

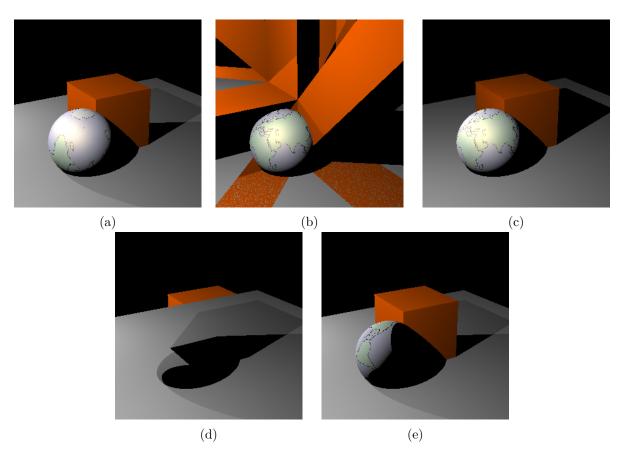


Figure 5: Images produced by introducing single-statement bugs into the program.