

# Solution Direction to HW1

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**Abstract**

## 1 TA Game

Graded on "all or nothing" scale, 1 point for each part

Constrained by the `if-else` clause in for loop, the card A can only followed by card T, and vice versa. So the answer will be in the form of "ATAT..." or "TATA..."

Besides, strings of all different length (from 2 to  $2 \cdot (1 + k)$ ) are possible because the execution of two players can interleave in any way.

So the final answer will be all strings expressed in  $k = n$  case.

### 1.1 $k = 1$

All possible strings:

AT	TA
ATA	TAT
ATAT	TATA

### 1.2 $k = 2$

All possible strings:

AT	TA
ATA	TAT
ATAT	TATA
ATATA	TATAT
ATATAT	TATATA

### 1.3 k = n

Possible strings:

- $(AT)^i$  for  $i \in \{1..n + 1\}$ ,  $n + 1$  states;
- $(AT)^i A$  for  $i \in \{1..n\}$ ,  $n$  states;
- $(TA)^i$  for  $i \in \{1..n + 1\}$ ,  $n + 1$  states;
- $(TA)^i T$  for  $i \in \{1..n\}$ ,  $n$  states;

So total number:  $4n + 2$

## 2 Aurora's Addition

Question 2 will be graded as follows:

- Points will be split evenly 5 - 9 per part
- In part 1, -1 per missing number
- In part 2, -2 per missing number
- Minimum score for both (ie they turned something in that made it look like they attempted it) is 1
- It is possible that they may have the same 2 numbers - if they match, quickly check netIds to see they did it right, count as right
- In other cases investigate further. If they have 3 numbers, it is likely but not guaranteed they are missing one

### 2.1 Call Add Once

There may be other schedules leading to outputs below. Only one possible schedule listed here.

Possible output	Possible schedule
6	$\text{if } \delta < 0(\text{MainLoop}) \rightarrow y = x - \delta(\text{MainLoop}) \rightarrow x = a(\text{Add})$
Int1 + 6	$\text{if } \delta < 0(\text{MainLoop}) \rightarrow x = a(\text{Add}) \rightarrow y = x - \delta(\text{MainLoop}) \text{ to } \delta = d(\text{Add})$
Int1 + Int2	$x = a(\text{Add}) \rightarrow \delta = d(\text{Add}) \rightarrow \text{if } \delta < 0(\text{MainLoop})$
Int1 - Int2	$\text{if } \delta < 0(\text{MainLoop}) \rightarrow x = a(\text{Add}) \rightarrow \delta = d(\text{Add}) \rightarrow y = x - \delta(\text{MainLoop})$

## 2.2 Call Add Twice

Possible Output	Case
6, Int1 + 6, Int1 + Int2, Int1 - Int2,	( second notify before waiting)
(6, Int1 - Int2)	
(Int1 + 6, Int1 - Int2)	
(Int1 + Int2, Int1 - Int2)	$\delta = -\text{Int2}$ after second if and before $y = x + \delta$
(Int1 - Int2, Int1 - Int2)	
(6, Int1 + Int2)	
(Int1 + 6, Int1 + Int2)	$\delta = -\text{Int2}$ after second if and after $y = x + \delta$
(Int1 + Int2, Int1 + Int2)	
(Int1 - Int2, Int1 + Int2)	or $\delta = -\text{Int2}$ before second if

## 3 To Be or Not To Be There

Question 3 will be graded on a all or nothing scale:

- The answers go like this: Same, Different, Different, Same, Stuck, Stuck
- Each is worth half a point

*CLARIFICATION:*

- *Sequential is 1 a) and 2 a)*
- *Interleaved\_v1 is 1 b)c)*
- *interleaved\_v2 is 2 b)c)*

We denote:

$p_A \leftarrow \text{select\_party}(A)$

$p_B \leftarrow \text{select\_party}(B)$

### 3.1 Sequential Case

$(p_A, p_A)$

When B gets to the if clause, A has already written  $p_A$  on the whiteboard. So B jumps to else case and set  $p[B] := \text{whiteboard} = p_A$

### 3.2 Interleaved Case 1

$(p_A, p_B)$

Because they execute lines in turn, both of them find  $\text{whiteboard} = \emptyset$  when they reach if clause. So in the next line A sets  $p[A] := p_A$  and B sets  $p[B] := p_B$ .

### 3.3 Interleaved Case 2

$(p_A, p_B)$

A have set its own choice  $p[A] := p_A$  but have not written to `whiteboard` yet. So B also enters the case `whiteboard=∅` and sets its own choice  $p[B] := p_B$ .

### 3.4 For More Complex Case

(1) $(p_A, p_A)$

Same case as explained above.

(2)Getting stuck

A sets `alice_busy=true`, and then B sets `bob_busy=true` immediately. Then A begins to wait for B and B begins to wait for A. Both of them get stuck.

(3)Getting stuck

A is still busy (`alice_busy=true`) till `select_party(i)` of A. Then B begins to execute and wait for A at the while loop. Now A is waiting for B to execute the entire function and B can never finish execution before A set `alice_busy=false`. Both of them get stuck.