

$$\text{pair} \cong \lambda a. \lambda b. (\lambda f. f a b)$$

$$\text{int} \times \text{bool} = \forall \delta. (\text{int} \rightarrow \text{bool} \rightarrow \delta) \rightarrow \delta$$

$$\text{pair} \cong \Lambda \alpha. \Lambda \beta. \lambda a: \alpha. \lambda b: \beta.$$

$$\underbrace{\lambda \delta. \lambda f: \alpha \rightarrow \beta \rightarrow \delta. f a b}$$

: "PAIR OF  $\alpha$  AND  $\beta$ "

$$\text{pair} [\text{int}] [\text{bool}] \text{ true}$$

$$: \text{Pair int bool}$$

$$\text{Pair} \cong \lambda \alpha: \text{type}. \lambda \beta: \text{type}.$$

$$\forall \delta. (\alpha \rightarrow \beta \rightarrow \delta) \rightarrow \delta$$

$\lambda \omega$

$$\tau ::= b \mid \tau_1 \rightarrow \tau_2 \mid \alpha \mid$$

$$\lambda \alpha: \kappa. \tau \mid \tau_1 \tau_2$$

$b ::= \text{int} \mid \text{bool}$   
 $\kappa ::= \text{type} \mid \kappa_1 \Rightarrow \kappa_2$

$: \text{type} \Rightarrow$   
 $\text{type} \Rightarrow$   
 $\text{type}$

$\Delta; \Gamma \vdash e : \tau$   
 $\uparrow$  TVar  $\rightarrow$  Kind

$\frac{\Delta \vdash \tau : \text{type}}{\Delta; \Gamma, x : \tau \vdash x : \tau}$

~~$\Delta \vdash \tau : \text{ok}$~~   
 $\Delta \vdash \tau : \kappa$

$\frac{\Delta \vdash \tau_1 : \text{type} \quad \Delta; \Gamma, x : \tau_1 \vdash e : \tau_2}{\Delta; \Gamma \vdash \lambda x : \tau_1. e : \tau_1 \rightarrow \tau_2}$

$\frac{\Delta; \Gamma \vdash e_1 : \tau_1 \rightarrow \tau_2 \quad \Delta; \Gamma \vdash e_2 : \tau_1}{\Delta; \Gamma \vdash e_1 e_2 : \tau_2}$

$\text{Pair int bool} \equiv \forall \delta. (\text{int} \rightarrow \text{bool} \rightarrow \delta) \rightarrow \delta$

$$\Delta; \Gamma \vdash e : \tau \quad \tau \equiv \tau' \quad \Delta \vdash \tau' : \text{type}$$


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$$\begin{array}{c} \text{TYPES} \uparrow \quad \text{KINDS} \downarrow \\ \Delta; \Gamma \vdash e : \tau' \\ \hline \Delta, \alpha : \kappa \vdash \alpha : \kappa \end{array} \quad \begin{array}{c} \Delta, \alpha : \kappa_1 \vdash \tau : \kappa_2 \\ \hline \Delta \vdash \lambda \alpha : \kappa. \tau : \\ \kappa_1 \Rightarrow \kappa_2 \\ \Delta \vdash \tau_1 : \text{type} \quad \Delta \vdash \tau_2 : \text{type} \\ \hline \Delta \vdash \tau_1 \rightarrow \tau_2 : \text{type} \end{array}$$

$$\Delta \vdash b : \text{type}$$

$$\frac{}{\tau \equiv \tau}$$

$$\frac{\tau_1 \equiv \tau_2}{\tau_2 \equiv \tau_1}$$

$$\frac{\tau_1 \equiv \tau_2 \quad \tau_2 \equiv \tau_3}{\tau_1 \equiv \tau_3}$$

$$\frac{\tau_1 \equiv \tau'_1 \quad \tau_2 \equiv \tau'_2}{\tau_1 \rightarrow \tau_2 \equiv \tau'_1 \rightarrow \tau'_2}$$

$$\frac{\tau \equiv \tau'}{\lambda x : \kappa. \tau \equiv \lambda x : \kappa. \tau'}$$

$$\frac{\tau_1 \equiv \tau'_1 \quad \tau_2 \equiv \tau'_2}{\tau_1 \tau_2 \equiv \tau'_1 \tau'_2}$$

$$\frac{}{(\lambda \alpha : \kappa. \tau_1) \tau_2 \equiv \tau_1 \{ \tau_2 / \alpha \}}$$

List

List <Integer>

List < $\tau$ > := Array List < $\tau$ >

