

#### Probabilistic Programming

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It's not about writing software.

#### Probabilistic Programming

Probabilistic programming is a tool for statistical modeling.

#### OR

A probabilistic programming language is a plain old programming language with rand(3) and a suite of fancy analysis tools for understanding its probabilistic behavior.

### An Example Model









 $\Pr[A_{\text{NIPS}}|I_{\text{stats}} \wedge B] = 0.3$  $\Pr[A_{\text{NIPS}}|I_{\text{stats}} \land \neg B] = 0.8$  $\Pr[A_{\rm NIPS} | \neg I_{\rm stats}] = 0.1$ Whither reuse?  $\Pr[A_{\text{Dagstuhl}}|I_{\text{stats}} \wedge I_{\text{PL}}] = 0.3$  $\Pr[A_{\text{Dagstuhl}}|I_{\text{stats}} \wedge I_{\text{PL}} \wedge \neg B] = 0.8$  $\Pr[A_{\text{Dagstuhl}} | \neg (I_{\text{stats}} \lor I_{\text{PL}})] = 0.1$  $R_1 \sim I_{\rm PL} \wedge I_{\rm stats}$ Whither Whither  $R_2 \sim I_{\rm PL}$ abstraction? intermediate  $R_3 \sim I_{\rm stats}$ variables?

## Writing even this tiny model feels like **drudgery.**

(and we haven't even gotten to the hard part yet)

- What and Why
- The Basics and Examples
- Applications
- Current Problems

### webppl.org



webppl

**On Github** 

webppl is a small but feature-rich probabilistic programming language embedded in Javascript.



#### Our First Probabilistic Program

## var b = flip(0.5); b ? "yes" : "no"

#### Enumeration

# var roll = function () { var die1 = randomInteger(6) + 1; var die2 = randomInteger(6) + 1; return die1 + die2;

Enumerate(roll)

#### Our Basic Model in webppl

```
model.wppl (~/science/ppl-intro/code) - VIM
// Class attendance model.
var attendance = function(i_pl, i_stats, busy) {
 var attendance = function (interest, busy) {
   if (interest) {
      return busy ? flip(0.3) : flip(0.8);
   } else {
      return flip(0.1);
   - }-
  }
  var a_4110 = attendance(i_pl, busy);
 var a_4780 = attendance(i_stats, busy);
 var a_4242 = attendance(i_pl && i_stats, busy);
 return {cs4110: a_4110, cs4780: a_4780, cs4242: a_4242};
// Relevance of our three papers.
var relevance = function(i_pl, i_stats) {
 var rel1 = i_pl && i_stats;
 var rel2 = i_pl;
  var rel3 = i_stats;
  return {paper1: rel1, paper2: rel2, paper3: rel3};
// A combined model.
var model = function() {
 // Some even random priors for our "student profile."
 var i_pl = flip(0.5);
 var i_stats = flip(0.5);
 var busy = flip(0.5);
  return [relevance(i_pl, i_stats), attendance(i_pl, i_stats, busy)];
var dist = Enumerate(model);
viz.auto(dist);
```

### Conditioning

var roll = function () {
 var die1 = randomInteger(6) + 1;
 var die2 = randomInteger(6) + 1;
 if (!(die1 === 4 || die2 === 4)) {
 factor(-Infinity);
 }
 return die1 + die2;

Enumerate (roll)

#### Conditioning on Observations

// Discard any executions that
// don't sum to 10.
var out = die1 + die2;
if (out !== 10) {
 factor(-Infinity);
}

// Return the values on the dice.
return [die1, die2];

### **Recommending Papers**

require(att.cs4110 && att.cs4242 && !att.cs4780);

return relevance(i\_pl, i\_stats);

### Inference Algorithms

Enumerate is the simplest possible *inference* strategy.

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#### TrueSkill

Measure Transformer Semantics for Bayesian Machine Learning

Johannes Borgström Andrew D. Gordon Michael Greenberg James Margetson Jurgen Van Gael

// prior distributions, the hypothesis
let skill() = random (Gaussian(10.0,20.0))
let Alice,Bob,Cyd = skill(),skill(),skill()
// observe the evidence
let performance player = random (Gaussian(player,1.0))
observe (performance Alice > performance Bob) //Alice beats Bob
observe (performance Bob > performance Cyd) //Bob beats Cyd
observe (performance Alice > performance Cyd) //Alice beats Cyd
// return the skills
Alice,Bob,Cyd

### webppl Vision Demo



### Forestdb.org

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Forest						
	Models					
	Concept Learning					
	Inducing Arithmetic	Functions			<ul> <li>Image: A second s</li></ul>	
	Causal Support					
	Rational Rules					
	Word Learning as B	ayesian Inference				
	Bayes Net Structure	Learning			*	

- What and Why
- The Basics and Examples
- Applications
- Current Research

**R2** 3 C ŋ research.microsoft.com Ι >>Microsoft Microsoft Research Search Microsoft Research Connections Our research Careers About us All Downloads People Projects Publications Videos Events Groups News f The R2 Probabilistic Programming Tool The R2 Probabilistic Programming Tool is a research project within the Programming Languages and Tools group at Microsoft Research on probabilistic programming. Our goal is to build a user friendly and scalable probabilistic programming system by employing powerful techniques from language in design, program analysis and verification. Details Download Download Type

File Name

r2-0.0.1.zip

Note By installing conving or otherwise

#### R2's weakest preconditions

var die1 = randomInteger(7) + 1; var die2 = randomInteger(7) + 1;

// Discard any executions that
// don't sum to 10.
var out = die1 + die2; wasted work!
require(out === 10);

#### R2's weakest preconditions

var die1 = randomInteger(7) + 1; var die2 = randomInteger(7) + 1;

require(
 (die1 == 3 && die2 == 7) || ...);
var out = die1 + die2;
require(out === 10);

#### R2's weakest preconditions

var die1 = randomInteger(7) + 1; var die2 = randomInteger(7) + 1; require( (die1 == 3 && die2 == 7) || ...); var out = die1 + die2;

# Probabilistic assertions: design goals

Work on a messy, mainstream language (C and C++)

Efficiently check statistical properties of the output

We don't care about conditioning

#### passert e, p, c

#### e must hold with probability p at confidence c

#### distribution extraction via symbolic execution statistical optimizations float average\_salary(float\* salaries) { total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT;

Bayesian network IR



Bayesian network IR

#### **Distribution extraction:** random draws are symbolic





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#### distribution extraction via symbolic execution statistical optimizations flot obfuscated(flot n) { return n + gaussian(0.0, 1000.0); ff ot it = 0; i < COUNT; ++i) total + cobfuscated(salaries) { total + cobfuscated(salaries); p\_avg = ...; passert e, p, c

Bayesian network IR

 $X \sim G(\mu_X, \sigma_X^2)$  $Y \sim G(\mu_Y, \sigma_Y^2)$ Z = X + Y $\Rightarrow Z \sim G(\mu_X + \mu_Y, \sigma_X^2 + \sigma_Y^2)$ 

 $X \sim U(a, b)$ Y = cX $\Rightarrow Y \sim U(ca, cb)$ 



 $X \sim U(a, b)$  $Y \sim X \le c$  $a \le c < b$  $\Rightarrow Y \sim B\left(\frac{c-a}{b-a}\right)$ 

 $X_1, X_2, \dots, X_n \sim D$  $Y = \mathbf{\Sigma}$  $Y = \sum_{i} X_{i}$   $\Rightarrow Y \sim G(n\mu_{D}, n\sigma_{D}^{2})$ 

#### distribution extraction via symbolic execution statistical optimizations float average\_salary(float\* salaries) { total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT; +i) total = 0.0; for (int = 0; i < COUNT;

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