| Discrete Structures | Homework 9 |
|---------------------|------------|
| CS2800 Spring 2015  | RSA        |

1. Suppose we wish to transmit the message "cs2800 rocks" using RSA. Suppose the public key has m = pq = 3403 and the exponent k = 17.

Note: for this problem, I used a spreadsheet to do the calculations. If you use calculators or spreadsheets to manipulate very large numbers, you can cause overflow, so make sure you reduce mod m as necessary to keep the numbers small. To compute  $a^k$  for large k, it helps to write k in binary, and then use repeated squaring to find a to a power-of-two power. For example, to compute  $a^{52}$ , I write 52 = 32 + 16 + 4, so  $a^{52} = a^{32} \cdot a^{16} \cdot a^4$ .

(a) Use the mapping

| · ?         | 01 |
|-------------|----|
| a           | 01 |
| 'b'         | 02 |
| :           | ÷  |
| 'y'         | 25 |
| 'z'         | 26 |
| ، ،         | 27 |
| '0'         | 28 |
| '1'         | 29 |
| '2'         | 30 |
| :           | ÷  |
| <b>'</b> 9' | 37 |

convert the message into a string of digits, and break the digits up into groups of threes.

- (b) By separately encrypting each block of 3 digits, produce the RSA cyphertext. Add leading zeros to each encrypted block so that each block of cyphertext is 4 digits long.
- (c) You have managed to intercept the private key: p = 41, q = 83. Use these factors to compute  $\phi(m)$  and  $k^{-1}$ . Use the algorithm you derived in question 2 of homework 8 to compute  $k^{-1} \mod \phi(m)$ .
- (d) Using these values, decrypt the message "0948 3332 1850 2898 2002 2692 0377 1398".