| Recitation 10 |
| :--- |
|  |
|  |
| Prelim Review |

## Big O

See the Study Habits Note @282 on the course Piazza. There is a 2-page pdf file that says how to learn what you need to know for O-notation.

Big O definition


| Review: Informal Big O rules |  |
| :---: | :---: |
| 1. Usually: $O(f(n)) \times O(g(n))=O(f(n) \times g(n))$ <br> - Such as if something that takes $g(n)$ time for each of $f(n)$ repetitions ... (loop within a loop) |  |
| 2. Usually: $O(f(n))+O(g(n))=O(\max (f(n), g(n)))$ <br> - "max" is whatever's dominant as $n$ approaches infinity $\text { - Example: } O\left(\left(n^{2}-n\right) / 2\right)=O\left((1 / 2) n^{2}+(-1 / 2) n\right)=O\left((1 / 2) n^{2}\right)$ $=O\left(n^{2}\right)$ |  |
| 3. Why don't logarithm bases matter? <br> -For constants $\mathrm{x}, \mathrm{y}: \mathrm{O}\left(\log _{\mathrm{x}} \mathrm{n}\right)=\mathrm{O}\left(\left(\log _{\mathrm{x}} \mathrm{y}\right)\left(\log _{\mathrm{y}} \mathrm{n}\right)\right)$ <br> -Since $\left(\log _{x} y\right)$ is a constant, $O\left(\log _{x} n\right)=O\left(\log _{y} n\right)$ <br> Test will not require understanding such rules for logarithms |  |
|  |  |


| Review: Big |  |  |  | i 0 |
| :---: | :---: | :---: | :---: | :---: |
| 1. $\log (n)+20$ | is | $\mathrm{O}(\log (\mathrm{n})$ ) | (logarithmic) |  |
| 2. $n+\log (\mathrm{n})$ | is | $\mathrm{O}(\mathrm{n})$ | (linear) |  |
| 3. $n / 2$ and $3^{*} n$ | are | $\mathrm{O}(\mathrm{n})$ |  |  |
| 4. $n * \log (\mathrm{n})+\mathrm{n}$ | is | $\mathrm{O}(\mathrm{n}$ * $\log (\mathrm{n})$ ) |  |  |
| 5. $n^{2}+2^{*} n+6$ | is | $\mathrm{O}\left(\mathrm{n}^{2}\right)$ | (quadratic) |  |
| 6. $\mathrm{n}^{3}+\mathrm{n}^{2}$ | is | $\mathrm{O}\left(\mathrm{n}^{3}\right)$ | (cubic) |  |
| 7. $2^{n}+n 5$ | is | $\mathrm{O}\left(2^{\mathrm{n}}\right)$ | (exponential) |  |




## Review: Hashing



| Method | Expected <br> Runtime | Worst <br> Case |
| :--- | :--- | :--- |
| add | $O(1)$ | $O(n)$ |
| contains | $O(1)$ | $O(n)$ |
| remove | $O(1)$ | $O(n)$ |

HashMap<String, Integer>

| to | 2 |
| :---: | :---: |
| be | 2 |
| or | 1 |
| not | 1 |
| that | 1 |
| is | 1 |
| the | 1 |
| question | 1 |




## Question: Hashing

Using linear probing to resolve collisions,

1. Add element SC (hashes to 9).
2. Remove VA (hashes to 3).
3. Check to see if MA (hashes to 21) is in the set.
4. What should we do if we override equals()?


Question: What is BFS and DFS?


1. Starting from node A, run BFS and DFS to find node $Z$. What is the order that the nodes were processed in? Visit neighbors in alphabetical order.
2. What is the difference between DFS and BFS ?
3. What algorithm would be better to use if our graph were near infinite and a node was nearby?
4. Is Dijkstra's more like DFS or BFS? Why?
5. Can you run topological sort on this graph?

Topological ordering


All edges go from a smaller-numbered node to a larger-numbered node.
How can this be useful?

## Dijkstra's Algorithm



The nodes are numbered in the order they are visitied if we start at 1 . Why are they visited in this order?

