

Prelim 1

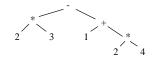
- □ Where: Kennedy Auditorium
- □ When:
 - □ A-Lib: 5:30-7
 - □ Lie-Z: 7:30-9
 - (unless we explicitly notified you otherwise)

Pointers to material

- □ Parse trees: text, section 23.36
- Definition of Java Language, sometimes useful: docs.oracle.com/javase/specs/jls/se8/html/index.html
- Grammar for most of Java, for those who are curious: docs.oracle.com/javase/specs/jls/se8/html/jls-18.html
- Tree traversals –preorder, inorder, postorder: text, sections 23.13 .. 23.15.

Expression trees

Can draw a tree for 2 * 3 - (1 + 2 * 4)



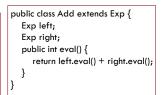
public abstract class Exp {
 /* return the value of this Exp */
 public abstract int eval();

Expression trees

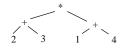
public abstract class Exp {
 /* return the value of this Exp */
 public abstract int eval();
}



public class Int extends Exp {
 int v;
 public int eval() {
 return v;
 }
}



tree for (2 + 3) * (1 + 4)



Preorder traversal:

- 1. Visit the root
- 2. Visit left subtree, in preorder
- 3. Visit right subtree, in preorder

* + 23 + 14

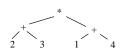
prefix and postfix notation proposed by Jan Lukasiewicz in 1951

Postfix (we see it later) is often called RPN for Reverse Polish Notation

see it.

In about 1974, Gries paid \$300 for an HP calculator, which had some memory and used postfix notation! Still works. Come up to

tree for (2 + 3) * (1 + 4)



Postorder traversal:

- 1. Visit left subtree, in postorder
- 2. Visit right subtree, in postorder
- 3. Visit the root

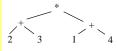
23+14+* Postfix notation tree for (2 + 3) * (1 + 4)

Postfix is easy to compute. Process elements left to right.

Number? Push it on a stack

Binary operator? Remove two top stack elements, apply operator to it, push result on stack

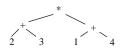
Unary operator? Remove top stack element, apply operator to it, push result on stack



Postfix notation

23+14+ *

tree for (2 + 3) * (1 + 4)



Inorder traversal:

- 1. Visit left subtree, in inorder
- 2. Visit the root
- 3. Visit right subtree, in inorder

To help out, put parens around expressions with

operators

(2+3) *(1 + 4) **Expression trees**

public class Add extends Exp {

Exp left; Exp right; public abstract class Exp { public abstract int eval(); public abstract String pre(); public abstract String post();

/** Return the value of this exp. * public int eval() {return left.eval() + right.eval();}

/** Return the preorder.*/ public String pre() {return "+ " + left.pre() + right.pre(); }

/** Return the postorder.*/ public String post() {return left.post() + right.post() + "+ "; }

Motivation for grammars

- ☐ The cat ate the rat.
- ☐ The cat ate the rat slowly.
- □ The small cat ate the big rat slowly.
- □ The small cat ate the big rat on the mat slowly.
- □ The small cat that sat in the hat ate the big rat on the mat slowly, then got sick.
- ...

· Not all sequences of words are legal sentences

The ate cat rat the

- · How many legal sentences are there?
- How many legal Java programs?
- How do we know what programs are legal?

http://docs.oracle.com/javase/specs/jls/se8/html/index.html

A Grammar

Sentence → Noun Verb Noun

Noun \rightarrow boys

Noun \rightarrow girls

Noun Verb

→ bunnies

 \rightarrow like see

• White space between words does not matter

• A very boring grammar because the set of Sentences is finite (exactly 18 sentences)

Our sample grammar has these rules:

A Sentence can be a Noun followed by a Verb followed by a Noun

A Noun can be boys or girls or bunnies

A Verb can be like or see

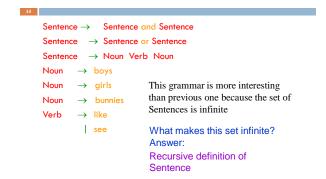
A Grammar

bunnies like boys

Sentence → Noun Verb Noun Noun → boys Noun → girls Noun → bunnies Verb → like Verb → see Sentence → Noun Verb Noun Grammar: set of rules for generating sentences of a language. Examples of Sentence: girls see bunnies

- The words boys, girls, bunnies, like, see are called *tokens* or *terminals*
- The words Sentence, Noun, Verb are called nonterminals

A recursive grammar



Detour

What if we want to add a period at the end of every sentence? Sentence → Sentence and Sentence. Sentence → Sentence or Sentence. Sentence → Noun Verb Noun. Noun → ... Does this work? No! This produces sentences like: girls like boys. and boys like bunnies.. Sentence Sentence

Sentence

Sentences with periods



Grammars for programming languages

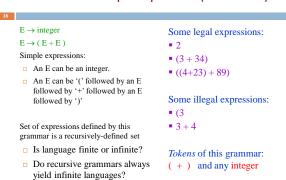
Grammar describes every possible legal expression

You could use the grammar for Java to list every possible Java
program. (It would take forever.)

Grammar tells the Java compiler how to "parse" a Java program

docs.oracle.com/javase/specs/jls/se8/html/jls-2.html#jls-2.3

Grammar for simple expressions (not the best)



Parsing

 $E \rightarrow integer$ $E \rightarrow (E + E)$

Use a grammar in two ways:

- ☐ A grammar defines a language (i.e. the set of properly structured sentences)
- ☐ A grammar can be used to parse a sentence (thus, checking if a string is asentence is in the language)

To *parse* a sentence is to build a *parse tree*: much like diagramming a sentence

• Example: Show that ((4+23) + 89) is a valid expression E by building a *parse tree*

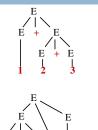


Ambiguity

Grammar is ambiguous if it allows two parse trees for a sentence. The grammar below, using no parentheses, is ambiguous. The two parse trees to right show this. We don't know which + to evaluate first in the expression 1+2+3

$$E \rightarrow integer$$

 $E \rightarrow E + E$



Recursive descent parsing

Write a set of mutually recursive methods to check if a sentence is in the language (show how to generate parse tree later).

One method for each nonterminal of the grammar. The method is completely determined by the rules for that nonterminal. On the next pages, we give a high-level version of the method for nonterminal E:

$$E \rightarrow integer$$

 $E \rightarrow (E + E)$

Parsing an E

 $E \rightarrow integer$ $E \rightarrow (E + E)$

/** Unprocessed input starts an E. Recognize that E, throwing away each piece from the input as it is recognized.

Return false if error is detected and true if no errors.

Upon return, processed tokens have been removed from input. */ public boolean parseE()

before call: already processed unprocessed

(2 + (4 + 8) + 9)

after call: already processed unprocessed
(call returns true) (2 + (4 + 8) + 9)

Specification: /** Unprocessed input starts an $E.\ \dots */$

 $E \rightarrow integer$ $E \rightarrow (E + E)$

public boolean parseE() {

if (first token is an integer) remove it from input and return true;

if (!parseE()) return false;

if (first token is not '+') return false else remove it from input;

 $if\ (!parseE())\ return\ false;$

if (first token is not ')') return false ${\it else}$ remove it from input; return true;

}

Illustration of parsing to check syntax

 $E \xrightarrow{E \rightarrow \text{integer}} E \xrightarrow{E \rightarrow (E+E)}$ $E \xrightarrow{E \rightarrow (E+E)}$ $E \xrightarrow{E \rightarrow (E+E)}$

The scanner constructs tokens

25

An object scanner of class Scanner is in charge of the input String. It constructs the tokens from the String as necessary. e.g. from the string "1464+634" build the token "1464", the token "+", and the token "634".

It is ready to work with the part of the input string that has not yet been processed and has thrown away the part that is already processed, in left-to-right fashion.

```
\frac{\text{already processed}}{(2 + (4 + 8) + 9)} \frac{\text{unprocessed}}{+ 9}
```

Change parser to generate a tree

```
E → integer

| ** ... Return a Tree for the E if no error.
| Return null if there was an error*/
| public Tree parseE() {
| if (first token is an integer) remove it from input and return true;
| if (first token is an integer) {
| Tree t = new Tree(the integer);
| Remove token from input;
| return t;
| }
```

Change parser to generate a tree

```
public '
```

```
/** ... Return a Tree for the E if no error.

Return null if there was an error*/

E \rightarrow integer
E \rightarrow (E + E)
```

public Tree parseE() {

if (first token is an integer) ...;

if (first token is not '(') return null else remove it from input;

Tree t1 = parse(E); **if** (t1 == null) **return null**;

if (first token is not '+') return null else remove it from input;

Tree t2= parse(E); **if** (t2 == null) **return null**;

if (first token is not ')' return false else remove it from input; return new Tree(t1, '+', t2);

r

Code for a stack machine

```
Code for 2 + (3 + 4)

PUSH 2

PUSH 3

PUSH 4

ADD

ADD

ADD

ADD: remove two top values from stack, add them, and place result on stack

It's postfix notation! 2 3 4 + +
```

Code for a stack machine

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Code for 2 + (3 + 4)

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PUSH 4

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ADD: remove two top values from stack, add them, and place result on stack

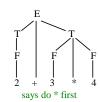
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```

Use parser to generate code for a stack machine

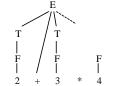
```
Code for 2 + (3 + 4)
                             parseE can generate code
                             as follows:
   PUSH 2
   PUSH 3
                             ■For integer i, return string
   PUSH 4
                               "PUSH" + i + "\n"
  ADD
                             •For (E1 + E2), return a
  ADD
                              string containing
ADD: remove two top values
                                 ◆Code for E1
from stack, add them, and
                                 ◆Code for E2
place result on stack
                                 •"ADD\n"
 It's postfix notation! 2 3 4 + +
```

Grammar that gives precedence to * over +

E-> T {+T} T->F{*F} F-> integer F->(E)



Notation: { xxx } means
0 or more occurrences of xxx.
E: Expression T: Term
F: Factor



Try to do + first, can't complete tree

Does recursive descent always work?

Some grammars cannot be used for recursive descent Trivial example (causes infinite recursion):

 $S \rightarrow b$

 $S \rightarrow Sa$

Can rewrite grammar

 $S \rightarrow b$

 $S \rightarrow bA$

 $A \rightarrow a$

 $A \rightarrow aA$

For some constructs, recursive descent is hard to use

Other parsing techniques exist – take the compiler writing course