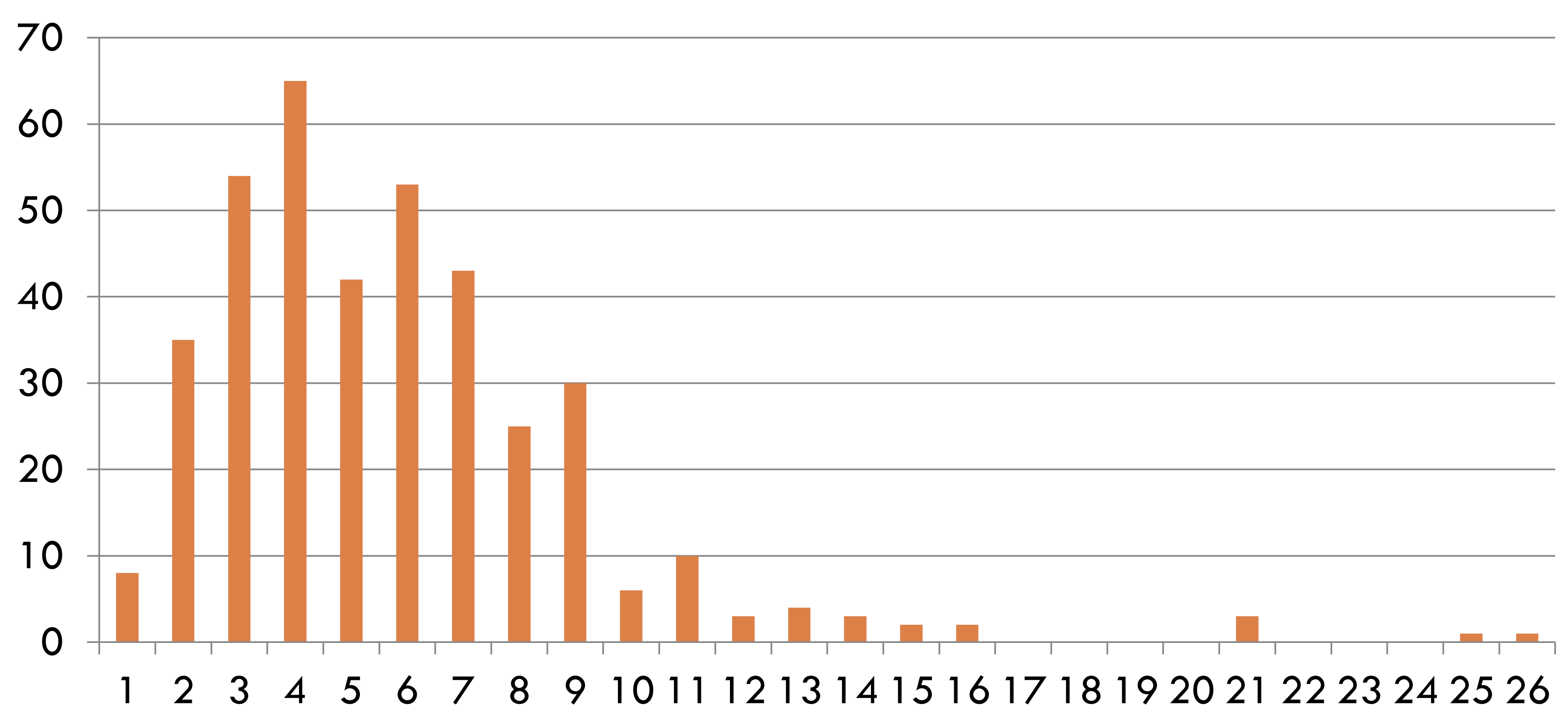
LISTS

Lecture 9

CS2110 – Fall 2013

Time spent on A2

- max: 25.4; avg: 5.2 hours, mean: 4.5 hours, min: 0.57 hours



References and Homework

- Text:
  - Chapters 10, 11 and 12
- Homework: Learn these List methods, from **http://docs.oracle.com/javase/7/docs/api/java/util/List.html**
  - add, addAll, contains, containsAll, get, indexOf, isEmpty, lastIndexOf, remove, size, toArray
  - myList = new List(someOtherList)
  - myList = new List(Collection<T>)
  - Also useful: Arrays.asList()

Understanding assignment A3

(1,4)	(2,4)	(3,4)	(4,4)
(1,3)	(2,3)	(3,3)	(4,3)
(1,2)	(2,2)	(3,2)	(4,2)
(1,1)	(2,1)	(3,1)	(4,1)

- A 4x4 park with the butterfly in position (1,1), a flower and a cliff.

Understanding assignment A3

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(3,2)	(4,2)	(1,2)	(2,2)
(3,1)	(4,1)	(1,1)	(2,1)
(3,4)	(4,4)	(1,4)	(2,4)
(3,3)	(4,3)	(1,3)	(2,3)

- A 4x4 park with the butterfly in position (1,1), a flower and a cliff.
- The same park! The map "wraps" as if the park lives on a torus!

Mapping Park coordinates to Java

- In the Park we use a column,row notation to identify cells, and have HEIGHT columns and WIDTH rows.
- Inside Java, we use 2-D arrays that index from 0
  - TileCell[][] myMap = new TileCell[Height][Width]
  - But one issue is that a (column,row) coordinate in the Park has to be "swapped" and adjusted to access the corresponding cell of myMap
- Rule:
  - Save the Park Cell from **Park location (r,c)** at **myMap[HEIGHT-c][r-1]**
  - **myMap**[**x**][**y**] tells you about **Park location (y+1, HEIGHT-x)**

Mapping Park coordinates to Java

- Rule:
  - Save the Park Cell from **Park location (r,c)** at **myMap[HEIGHT-c][r-1]**
  - **myMap[x][y]** tells you about **Park location (y+1, HEIGHT-x)**

- **Examples: assume HEIGHT=3, WIDTH=3**
  - **Location (1,3) = top left corner. Stored in myMap[HEIGHT-3][1-1], which is myMap[0][0]. Converts back to (1,3)**
  - **Location (1,1) = bottom left corner. Store in myMap[2][0].**
  - **Location (2,2) = middle of the 3x3 Park. Store in myMap[1][1]**
  - **Location (2,3) = top row, middle: Store in myMap[0][1]**

Mapping Park coordinates to Java

Park (Height=3, Width=3)

(1,3)	(2,3)	(3,3)
(1,2)	(2,2)	(3,2)
(1,1)	(2,1)	(3,1)

myMap (Height=3, Width=3)

[0][0]	[0][1]	[0][2]
[1][0]	[1][1]	[1][2]
[2][0]	[2][1]	[2][2]

Mapping Park coordinates to Java

HEIGHT=3, WIDTH=3

Park uses (column, row) notation

(1,3)	(2,3)	(3,3)
(1,2)	(2,2)	(3,2)
(1,1)	(2,1)	(3,1)

myMap uses [row][column] indexing

[0][0]	[0][1]	[0][2]
[1][0]	[1][1]	[1][2]
[2][0]	[2][1]	[2][2]

Example: Park (2,1) => myMap[HEIGHT-r][c-1]
. . . myMap[3-1][2-1]: myMap[2][1]

List Overview

- Purpose
  - Maintain an ordered collection of elements (with possible duplication)
- Common operations
  - Create a list
  - Access elements of a list sequentially
  - Insert elements into a list
  - Delete elements from a list
- Arrays
  - Random access ☺
  - Fixed size: cannot grow or shrink after creation ☹ (Sometimes simulated using copying)
- Linked Lists
  - No random access ☹ (Sometimes random-access is "simulated" but cost is linear)
  - Can grow and shrink dynamically ☺

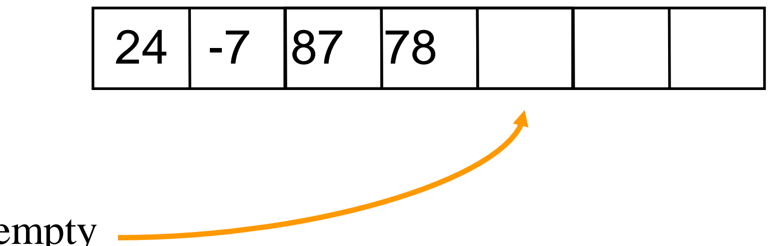
A Simple List Interface


```
public interface List<T> {
    public void insert(T element);
    public void delete(T element);
    public boolean contains(T element);
    public int size();
}
```

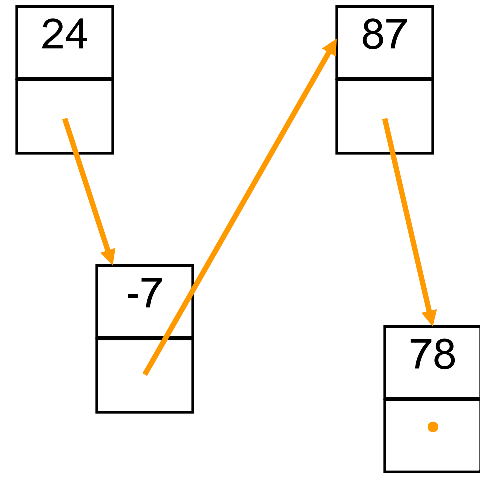
- Note that Java has a more complete interface and we do expect you to be proficient with it!

List Data Structures

- Array
  - Must specify array size at creation
  - Insert, delete require moving elements
  - Must copy array to a larger array when it gets full

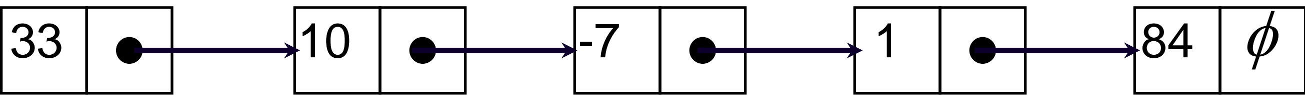


- Linked list
- uses a sequence of linked cells
- we will define a class ListCell from which we build lists



List Terminology

- Head = first element of the list
- Tail = rest of the list



Class ListCell

Each list element "points" to the next one!

End of list: `next==null`

```
class ListCell<T> {
    private T datum;
    private ListCell<T> next;

    public ListCell(T datum, ListCell<T> next){
        this.datum = datum;
        this.next = next;
    }

    public T getDatum() { return datum; }
    public ListCell<T> getNext() { return next; }
    public void setDatum(T obj) { datum = obj; }
    public void setNext(ListCell<T> c) { next = c; }
}
```

Ways of building a Linked List


```
ListCell<Integer> c =
    new ListCell<Integer>(new Integer(24),null);
```

c ListCell:

24

```
Integer t = new Integer(24);
Integer s = new Integer(-7);
Integer e = new Integer(87);

ListCell<Integer> p =
   new ListCell<Integer>(t,
      new ListCell<Integer>(s,
         new ListCell<Integer>(e, null)));
```

p ListCell:

24

–7

87

Building a Linked List (cont'd)

Another way:

```
Integer t = new Integer(24);
Integer s = new Integer(-7);
Integer e = new Integer(87);
//Can also use "autoboxing"
```

p ListCell:

24

-7

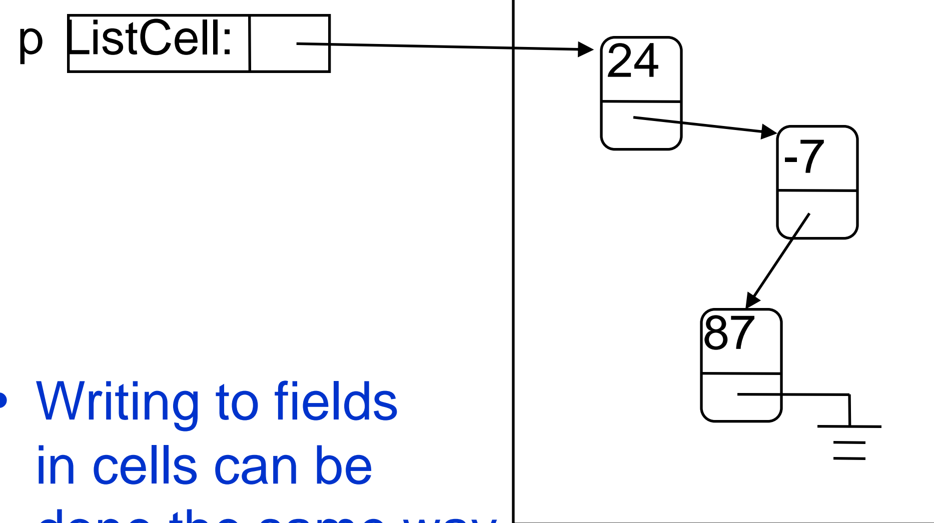
87

```
ListCell<Integer> p = new ListCell<Integer>(e, null);
p = new ListCell<Integer>(s, p);
p = new ListCell<Integer>(t, p);
```

Note: `p = new ListCell<Integer>(s,p);`
does *not* create a circular list!

Accessing List Elements

- Linked Lists are *sequential-access* data structures.
  - To access contents of cell n in sequence, you must access cells 0 ... n-1
- Accessing data in first cell: `p.getDatum()`
- Accessing data in second cell: `p.getNext().getDatum()`
- Accessing **next** field in second cell: `p.getNext().getNext()`



- Writing to fields in cells can be done the same way
  - Update data in first cell: `p.setDatum(new Integer(53));`
  - Update data in second cell: `p.getNext().setDatum(new Integer(53));`
  - Chop off third cell: `p.getNext().setNext(null);`

Access Example: Linear Search


```
// Here is another version. Why does this work?
public static boolean search(T x, ListCell c) {
    while(c != null) {
        if (c.getDatum().equals(x)) return true;
        c = c.getNext();
    }
    return false;
}
```

```
// Scan list looking for x, return true if found
public static boolean search(T x, ListCell c) {
    for (ListCell lc = c; lc != null; lc = lc.getNext()) {
        if (lc.getDatum().equals(x)) return true;
    }
    return false;
}
```

Why would we need to write code for search? It already exists in Java utils!

- Good question! In practice you should always use indexOf(), contains(), etc
- But by understanding how to code search, you gain skills you'll need when working with data structures that are more complex and that don't match predefined things in Java utils
- General rule: *If it already exists, use it.* But for anything you use, know how you would code it!

Recursion on Lists

- Recursion can be done on lists
  - Similar to recursion on integers

- Almost always
  - Base case: empty list
  - Recursive case: Assume you can solve problem on the tail, use that in the solution for the whole list

- Many list operations can be implemented very simply by using this idea
  - Although some are easier to implement using iteration

Recursive Search

- Base case: empty list
  - return false

- Recursive case: non-empty list
  - if data in first cell equals object x, return true
  - else return the result of doing linear search on the tail

Recursive Search: Static method


```java
public static boolean search(T x, ListCell c) {
    if (c == null) return false;
    if (c.getDatum().equals(x)) return true;
    return search(x, c.getNext());
}
```

```java
public static boolean search(T x, ListCell c) {
    return c != null &&
        (c.getDatum().equals(x) || search(x, c.getNext()));
}
```

Recursive Search: Instance method


```
public boolean search(T x) {
    if (datum.equals(x)) return true;
    if (next == null) return false
    return next.search(x);
}
```

```
public boolean search(T x) {
    return datum.equals(x) ||
        (next!= null && next.search(x));
}
```

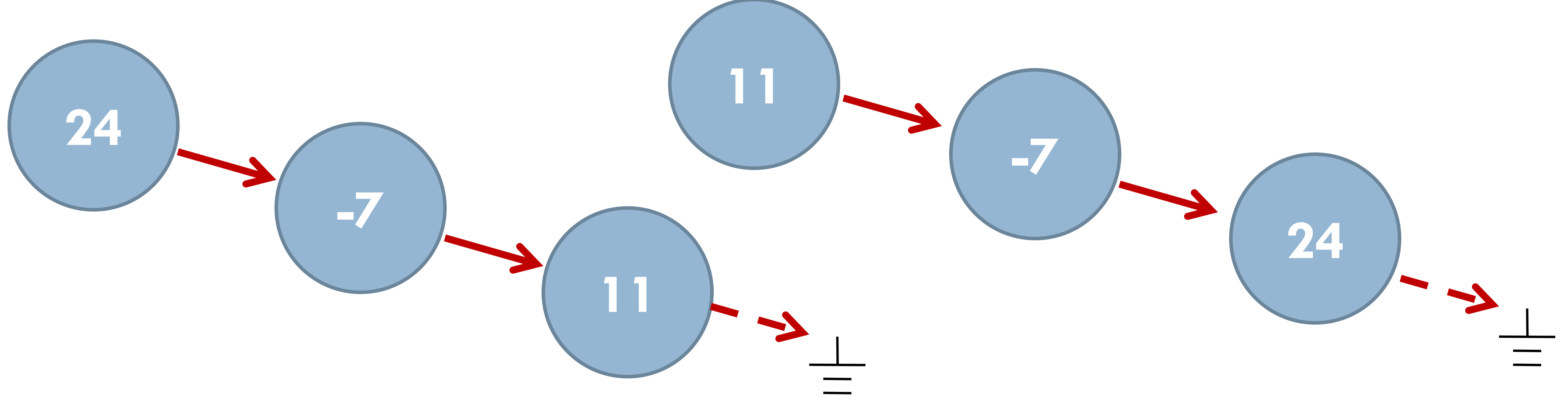
Reversing a List

- Given a list, create a new list with elements in reverse order
- Intuition: think of reversing a pile of coins

```
public static ListCell reverse(ListCell c) {
   ListCell rev = null;
   while(c != null) {
      rev = new ListCell(c.getDatum(), rev);
      c = c.getNext();
   }
   return rev;
}
```

- It may not be obvious how to write this recursively...

Reversing a list: Animation



- Approach: One by one, remove the first element of the given list and make it the first element of "rev"
- By the time we are done, the last element from the given list will be the first element of the finished "rev"

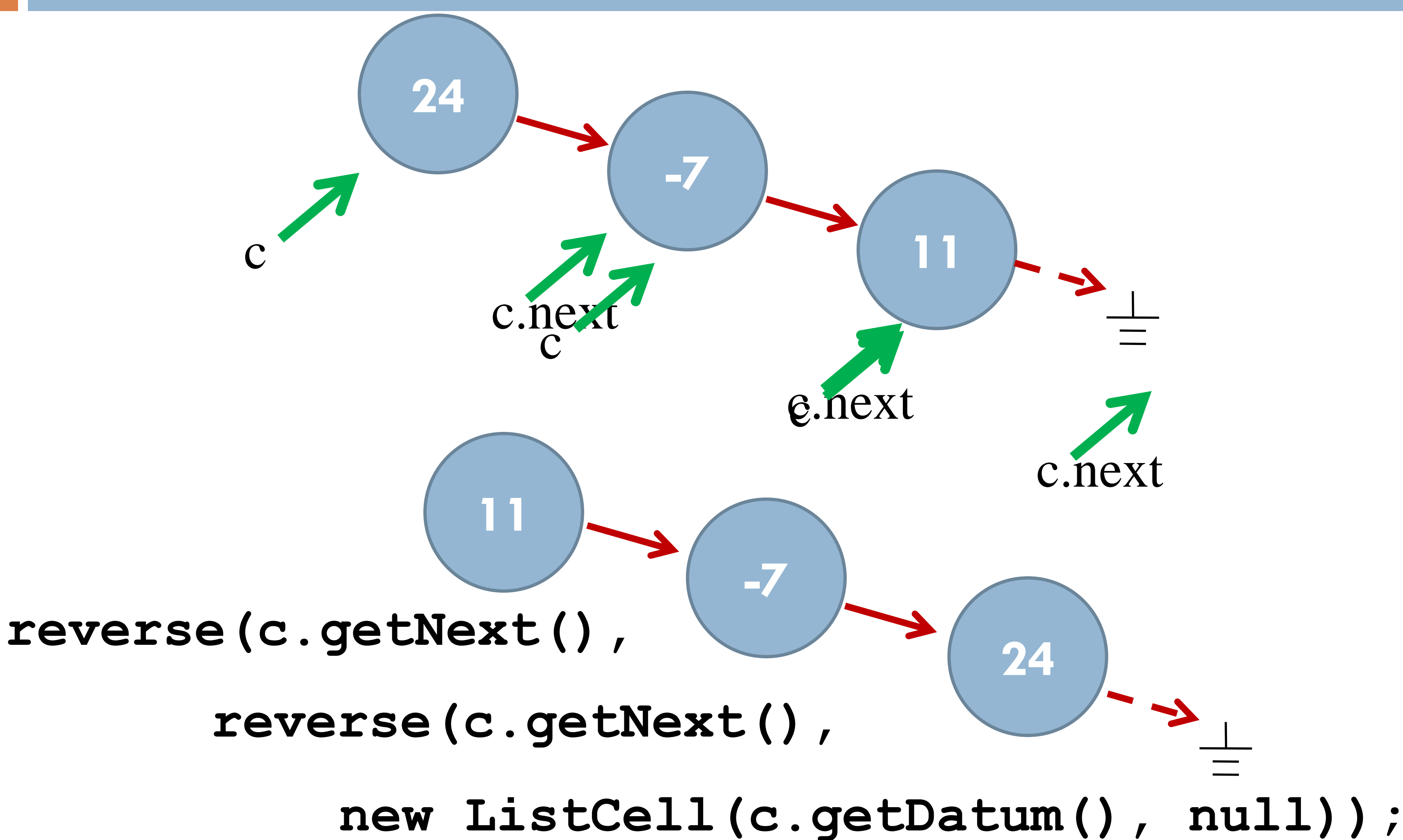
Recursive Reverse


```
public static ListCell reverse(ListCell c) {
   return reverse(c, null);
}

private static ListCell reverse(ListCell c, ListCell r) {
   if (c == null) return r;
   return reverse(c.getNext(),
                  new ListCell(c.getDatum(), r));
}
```

- Exercise: Turn this into an instance method

Reversing a list: Animation



List with Header

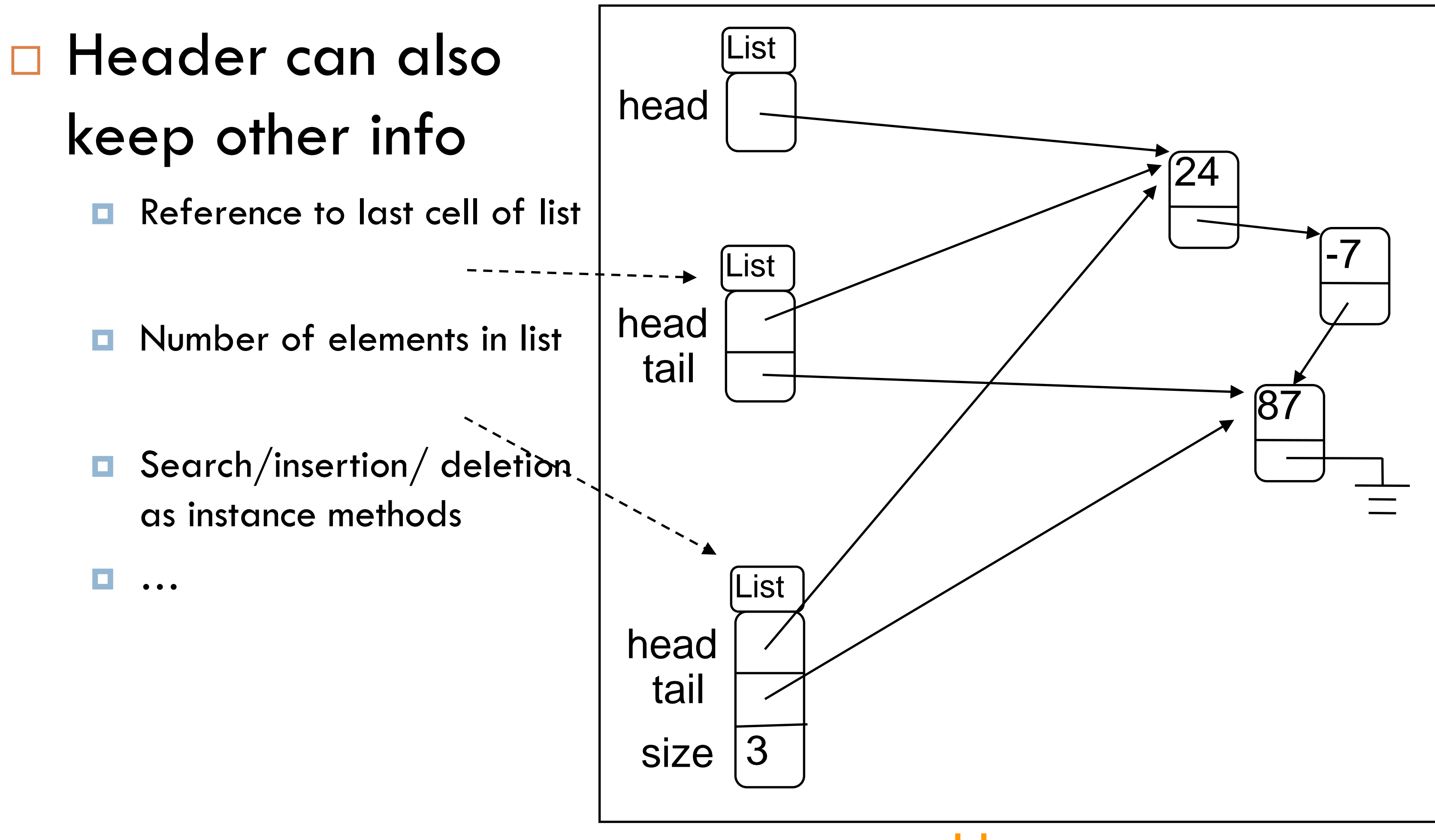
- Sometimes it is preferable to have a List class distinct from the ListCell class
- The List object is like a head element that always exists even if list itself is empty

```
class List {
   protected ListCell head;
   public List(ListCell c) {
      head = c;
   }
   public ListCell getHead()
   .........
   public void setHead(ListCell c)
   .........
}
```

List
head
24
-7
87
Heap

Variations on List with Header

- Header can also keep other info
  - Reference to last cell of list
  - Number of elements in list
  - Search/insertion/ deletion as instance methods
  - …



Special Cases to Worry About

- Empty list
  - add
  - find
  - delete
- Front of list
  - insert
- End of list
  - find
  - delete
- Lists with just one element

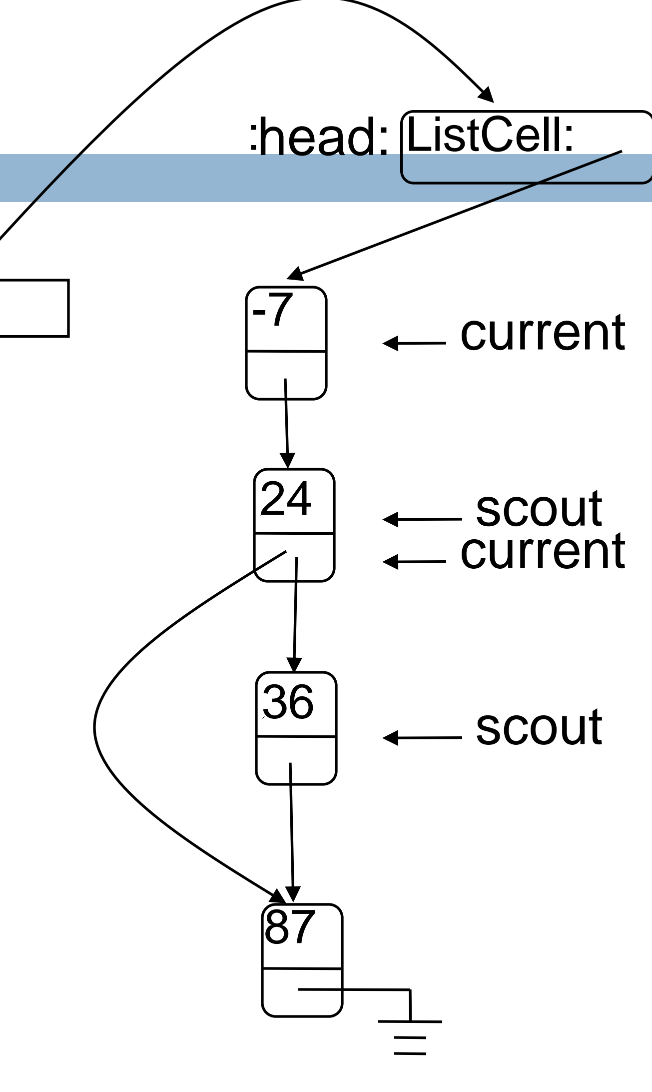
Example: Delete from a List

- Delete *first occurrence* of x from a list
- Intuitive idea of recursive code:
  - If list is empty, return null
  - If datum at head is x, return tail
  - Otherwise, return list consisting of

```
// recursive delete
public static ListCell delete(Object x, ListCell c) {
   if (c == null) return null;
   if (c.getDatum().equals(x)) return c.getNext();
   c.setNext(delete(x, c.getNext()));
   return c;
}
```

Iterative Delete

- Two steps:
  - Locate cell that is the *predecessor* of cell to be deleted (i.e., the cell containing x)
    - Keep two cursors, *scout* and *current*
    - *scout* is always one cell ahead of *current*
    - Stop when *scout* finds cell containing x, or falls off end of list
  - If *scout* finds cell, update *next* field of *current* cell to splice out object x from list
- Note: Need special case for x in first cell



delete 36 from list

Iterative Code for Delete


```
public void delete (Object x) {
    if (head == null) return;
    if (head.getDatum().equals(x)) { //x in first cell?
        head = head.getNext();
        return;
    }
    ListCell current = head;
    ListCell scout = head.getNext();
    while ((scout != null) && !scout.getDatum().equals(x)) {
        current = scout;
        scout = scout.getNext();
    }
    if (scout != null) current.setNext(scout.getNext());
    return;
}
```

Doubly-Linked Lists

- In some applications, it is convenient to have a **`ListCell`** that has references to both its predecessor and its successor in the list.

```
class DLLCell {
   private Object datum;
   private DLLCell next;
   private DLLCell prev;
   …
}
```

prev

6

45

8

-9

next

Doubly-Linked vs Singly-Linked

- Advantages of doubly-linked over singly-linked lists
  - some things are easier – e.g., reversing a doubly-linked list can be done simply by swapping the previous and next fields of each cell
  - don't need the scout to delete
- Disadvantages
  - doubly-linked lists require twice as much space
  - insert and delete take more time

Java ArrayList

- "Extensible array"
- Starts with an initial capacity = size of underlying array
- If you try to insert an element beyond the end of the array, it will allocate a new (larger) array, copy everything over invisibly
  - Appears infinitely extensible

- Advantages:
  - random access in constant time
  - dynamically extensible

- Disadvantages:
  - Allocation, copying overhead