



GRAMMARS & PARSING

Lecture 7
CS2110 – Fall 2013

Pointers to the textbook

2

Parse trees: Text page 592 (23.34), Figure 23-31

- ▣ Definition of Java Language, sometimes useful:
<http://docs.oracle.com/javase/specs/jls/se7/html/index.html>
- ▣ Grammar for most of Java, for those who are curious:
<http://csci.csusb.edu/dick/samples/java.syntax.html>

Homework:

- ▣ Learn to use these Java string methods:
`s.length`, `s.charAt()`, `s.indexOf()`, `s.substring()`, `s.toCharArray()`,
`s = new string(char[] array)`.
- ▣ Hint: These methods will be useful on prelim1 (Oct 10)!
(They can be useful for parsing too...)

Application of Recursion

3

- So far, we have discussed recursion on integers
 - ▣ Factorial, fibonacci, a^n , combinatorials
- Let us now consider a new application that shows off the full power of recursion: *parsing*
- Parsing has numerous applications: compilers, data retrieval, data mining,...

Motivation

4

- **The cat ate the rat.**
 - **The cat ate the rat slowly.**
 - **The small cat ate the big rat slowly.**
 - **The small cat ate the big rat on the mat slowly.**
 - **The small cat that sat in the hat ate the big rat on the mat slowly.**
 - **The small cat that sat in the hat ate the big rat on the mat slowly, then got sick.**
 - ...
- Not all sequences of words are legal sentences
 - The ate cat rat the
 - How many legal sentences are there?
 - How many legal programs are there?
 - Are all Java programs that compile legal programs?
 - How do we know what programs are legal?

<http://docs.oracle.com/javase/specs/jls/se7/html/index.html>

A Grammar

5

□ **Sentence** → **Noun Verb Noun**

□ **Noun** → **boys**

□ **Noun** → **girls**

□ **Noun** → **bunnies**

□ **Verb** → **like**

□ **Verb** → **see**

□ **Our sample grammar has these rules:**

□ **A Sentence can be a Noun followed by a Verb followed by a Noun**

□ **A Noun can be 'boys' or 'girls' or 'bunnies'**

□ **A Verb can be 'like' or 'see'**

• **Grammar:** set of rules for generating sentences in a language

• **Examples of Sentence:**

▪ boys see bunnies

▪ bunnies like girls

▪ ...

• White space between words does not matter

• The words **boys, girls, bunnies, like, see** are called *tokens* or *terminals*

• The words **Sentence, Noun, Verb** are called *nonterminals*

• This is a very boring grammar because the set of Sentences is finite (exactly 18 sentences)

A Recursive Grammar

6

- **Sentence** → **Sentence and Sentence**
 - **Sentence** → **Sentence or Sentence**
 - **Sentence** → **Noun Verb Noun**
 - **Noun** → **boys**
 - **Noun** → **girls**
 - **Noun** → **bunnies**
 - **Verb** → **like**
 - **Verb** → **see**

 - **This grammar is more interesting than the last one because the set of Sentences is infinite**
- Examples of Sentences in this language:
 - boys like girls
 - boys like girls and girls like bunnies
 - boys like girls and girls like bunnies and girls like bunnies
 - boys like girls and girls like bunnies and girls like bunnies and girls like bunnies
 -
 - What makes this set infinite?
Answer:
 - Recursive definition of Sentence

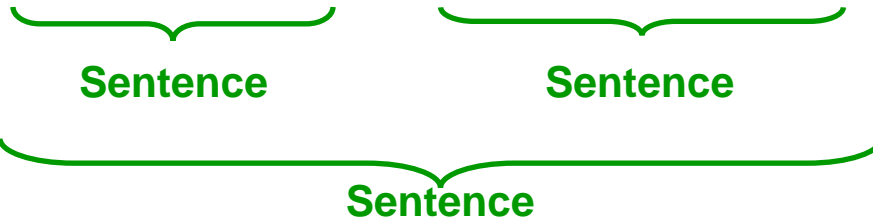
Detour

7

- What if we want to add a period at the end of every sentence?
- Sentence → Sentence and Sentence .
- Sentence → Sentence or Sentence .
- Sentence → Noun Verb Noun .
- Noun → ...

- Does this work?
- No! This produces sentences like:

□ girls like boys . and boys like bunnies . .



Sentences with Periods

8

- **PunctuatedSentence** → **Sentence .**
 - **Sentence** → **Sentence and Sentence**
 - **Sentence** → **Sentence or Sentence**
 - **Sentence** → **Noun Verb Noun**
 - **Noun** → **boys**
 - **Noun** → **girls**
 - **Noun** → **bunnies**
 - **Verb** → **like**
 - **Verb** → **see**
- Add a new rule that adds a period only at the end of the sentence.
 - The tokens here are the 7 words plus the period (.)
 - This grammar is ambiguous:
boys like girls
and girls like boys
or girls like bunnies

Uses of Grammars

- Grammar describes every possible legal expression
 - ▣ You could use the grammar for Java to list every possible Java program. (It would take forever)
- Grammar tells the Java compiler how to understand a Java program

Grammar for Simple Expressions

10

- $E \rightarrow \text{integer}$
 - $E \rightarrow (E + E)$

 - **Simple expressions:**
 - An E can be an integer.
 - An E can be '(' followed by an E followed by '+' followed by an E followed by ')'

 - **Set of expressions defined by this grammar is a recursively-defined set**
 - Is language finite or infinite?
 - Do recursive grammars always yield infinite languages?
- Here are some legal expressions:
 - 2
 - (3 + 34)
 - ((4+23) + 89)
 - ((89 + 23) + (23 + (34+12)))

 - Here are some illegal expressions:
 - (3
 - 3 + 4

 - The *tokens* in this grammar are (, +,), and any integer

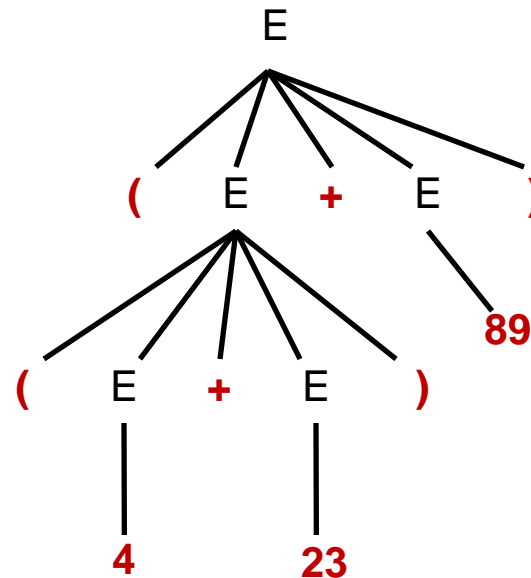
Parsing

11

- Grammars can be used in two ways
 - ▣ A grammar defines a *language* (i.e., the set of properly structured sentences)
 - ▣ A grammar can be used to *parse* a sentence (thus, checking if the sentence is in the *language*)

- To *parse* a sentence is to build a *parse tree*
 - ▣ This is much like *diagramming a sentence*

- Example: Show that $((4+23) + 89)$ is a valid expression E by building a *parse tree*



Recursive Descent Parsing

12

- Idea: Use the grammar to design a *recursive program* to check if a sentence is in the language
- To parse an expression E, for instance
 - ▣ We look for each terminal (i.e., each *token*)
 - ▣ Each nonterminal (e.g., E) can handle itself by using a *recursive call*
- The grammar tells how to write the program!

```
boolean parseE() {
    if (first token is an integer) return true;
    if (first token is '(' ) {
        parseE();
        Make sure there is a '+' token;
        parseE( );
        Make sure there is a ')' token;
        return true;
    }
    return false;
}
```

Java Code for Parsing E

13

```
public static Node parseE(Scanner scanner) {
    if (scanner.hasNextInt()) {
        int data = scanner.nextInt();
        return new Node(data);
    }
    check(scanner, '(');
    left = parseE(scanner);
    check(scanner, '+');
    right = parseE(scanner);
    check(scanner, ')');
    return new Node(left, right);
}
```

Detour: Error Handling with Exceptions

14

- Parsing does two things:
 - ▣ It returns useful data (a parse tree)
 - ▣ It checks for validity (i.e., is the input a valid *sentence*?)
- How should we respond to invalid input?
- *Exceptions* allow us to do this without complicating our code unnecessarily

Exceptions

15

- Exceptions are usually thrown to indicate that something bad has happened
 - **IOException** on failure to open or read a file
 - **ClassCastException** if attempted to cast an object to a type that is not a supertype of the dynamic type of the object
 - **NullPointerException** if tried to dereference null
 - **ArrayIndexOutOfBoundsException** if tried to access an array element at index $i < 0$ or ε the length of the array
- In our case (parsing), we should throw an exception when the input cannot be parsed

Handling Exceptions

16

- Exceptions can be caught by the program using a **try-catch** block
- **catch** clauses are called *exception handlers*

```
Integer x = null;
try {
    x = (Integer)y;
    System.out.println(x.intValue());
} catch (ClassCastException e) {
    System.out.println("y was not an Integer");
} catch (NullPointerException e) {
    System.out.println("y was null");
}
```


Defining Your Own Exceptions

17

- An exception is an object (like everything else in Java)
- You can define your own exceptions and throw them

```
class MyOwnException extends Exception {}  
  
...  
  
if (input == null) {  
    throw new MyOwnException();  
}
```

Declaring Exceptions

18

- In general, any exception that could be thrown must be either *declared* in the method header or *caught*

```
void foo(int input) throws MyOwnException {  
    if (input == null) {  
        throw new MyOwnException();  
    }  
    ...  
}
```

-
- Note: **throws** means “can throw”, not “does throw”
- Subtypes of **RuntimeException** do not have to be declared (e.g., **NullPointerException**, **ClassCastException**)
 - These represent exceptions that can occur during “normal operation of the Java Virtual Machine”

How Exceptions are Handled

19

- If the exception is thrown from *inside* the **try** clause of a **try-catch** block with a handler for that exception (or a superclass of the exception), then that handler is executed
 - ▣ Otherwise, the method terminates abruptly and control is passed back to the calling method
- If the calling method can handle the exception (i.e., if the call occurred within a **try-catch** block with a handler for that exception) then that handler is executed
 - ▣ Otherwise, the calling method terminates abruptly, etc.
- If *none* of the calling methods handle the exception, the entire program terminates with an error message

Using a Parser to Generate Code

20

- We can modify the parser so that it generates stack code to evaluate arithmetic expressions:

2 PUSH 2
 STOP

(2 + 3) PUSH 2
 PUSH 3
 ADD
 STOP

- Goal: Method `parseE` should return a string containing stack code for expression it has parsed

- Method `parseE` can generate code in a recursive way:
 - For integer i , it returns string “PUSH” + i + “\n”
 - For $(E1 + E2)$,
 - ◆ Recursive calls for $E1$ and $E2$ return code strings $c1$ and $c2$, respectively
 - ◆ Then to compile $(E1 + E2)$, return $c1 + c2 + “ADD\n”$
 - Top-level method should tack on a **STOP** command after code received from `parseE`

Does Recursive Descent Always Work?

21

- There are some grammars that cannot be used as the basis for recursive descent
 - A trivial example (causes infinite recursion):
 - $S \rightarrow b$
 - $S \rightarrow Sa$

- Can rewrite grammar
 - $S \rightarrow b$
 - $S \rightarrow bA$
 - $A \rightarrow a$
 - $A \rightarrow aA$

- For some constructs, recursive descent is hard to use
- Can use a more powerful parsing technique (there are several, but not in this course)

Syntactic Ambiguity

22

□ Sometimes a sentence has more than one parse tree

- $S \rightarrow A \mid aaxB$
- $A \rightarrow x \mid aAb$
- $B \rightarrow b \mid bB$

□ The string $aaxbb$ can be parsed in two ways

□ This kind of ambiguity sometimes shows up in programming languages

□ if E1 then if E2 then S1 else S2

□ Which then does the else go with?

- This ambiguity actually affects the program's meaning
- How do we resolve this?
 - Provide an extra non-grammar rule (e.g., the *else* goes with the closest *if*)
 - Modify the language (e.g., an if-statement must end with a 'fi')
 - Operator precedence (e.g.
 $1 + 2 * 3$ should be parsed as $1 + (2 * 3)$, not $(1 + 2) * 3$)
 - Other methods (e.g., Python uses amount of indentation)

Conclusion

23

- Recursion is a very powerful technique for writing compact programs that do complex things
- Common mistakes:
 - ▣ Incorrect or missing base cases
 - ▣ Subproblems must be simpler than top-level problem
- Try to write description of recursive algorithm and reason about base cases before writing code
 - ▣ Why?
 - Syntactic junk such as type declarations, etc. can create mental fog that obscures the underlying recursive algorithm
 - ▣ Best to separate the logic of the program from coding details

Exercises

24

- Think about recursive calls made to parse and generate code for simple expressions
 - 2
 - $(2 + 3)$
 - $((2 + 45) + (34 + -9))$

- Derive an expression for the total number of calls made to parse E for parsing an expression
 - Hint: think inductively

- Derive an expression for the maximum number of recursive calls that are active at any time during the parsing of an expression (i.e. max depth of call stack)

Exercises

25

- Write a grammar and recursive program for sentence palindromes that ignores white spaces & punctuation
 - ▣ **Was it Eliot's toilet I saw?**
 - ▣ **No trace; not one carton**
 - ▣ **Go deliver a dare, vile dog!**
 - ▣ **Madam, in Eden I'm Adam**
- Write a grammar and recursive program for strings A^nB^n
 - ▣ **AB**
 - ▣ **AABB**
 - ▣ **AAAAAABBBBBBB**
- Write a grammar and recursive program for Java identifiers
 - ▣ **<letter> [<letter> or <digit>]^{0...N}**
 - ▣ **j27, but not 2j7**