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GRAMMARS & PARSING

Lecture 7
CS2110 – Fall 2013

Pointers to the textbook

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Parse trees: [Text page 592 \(23.34\), Figure 23-31](#)

- Definition of Java Language, sometimes useful: <http://docs.oracle.com/javase/specs/jls/se7/html/index.html>
- Grammar for most of Java, for those who are curious: <http://csci.csusb.edu/dick/samples/java.syntax.html>

Homework:

- Learn to use these Java string methods: `s.length`, `s.charAt()`, `s.indexOf()`, `s.substring()`, `s.toCharArray()`, `s = new string(char[] array)`.
- Hint: These methods will be useful on prelim1 (Oct 10)! (They can be useful for parsing too...)

Application of Recursion

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- So far, we have discussed recursion on integers
 - Factorial, fibonacci, a^n , combinatorials
- Let us now consider a new application that shows off the full power of recursion: *parsing*
- Parsing has numerous applications: compilers, data retrieval, data mining,...

Motivation

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- The cat ate the rat.
- The cat ate the rat slowly.
- The small cat ate the big rat slowly.
- The small cat ate the big rat on the mat slowly.
- The small cat that sat in the hat ate the big rat on the mat slowly.
- The small cat that sat in the hat ate the big rat on the mat slowly, then got sick.
- ...

- Not all sequences of words are legal sentences
- The ate cat rat the
- How many legal sentences are there?
- How many legal programs are there?
- Are all Java programs that compile legal programs?
- How do we know what programs are legal?

<http://docs.oracle.com/javase/specs/jls/se7/html/index.html>

A Grammar

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- Sentence → Noun Verb Noun
- Noun → boys
- Noun → girls
- Noun → bunnies
- Verb → like
- Verb → see

- Grammar: set of rules for generating sentences in a language
- Examples of Sentence:
 - boys see bunnies
 - bunnies like girls
 - ...
- White space between words does not matter
- The words *boys*, *girls*, *bunnies*, *like*, *see* are called *tokens* or *terminals*
- The words *Sentence*, *Noun*, *Verb* are called *nonterminals*
- This is a very boring grammar because the set of Sentences is finite (exactly 18 sentences)

- Our sample grammar has these rules:
 - A Sentence can be a Noun followed by a Verb followed by a Noun
 - A Noun can be 'boys' or 'girls' or 'bunnies'
 - A Verb can be 'like' or 'see'

A Recursive Grammar

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- Sentence → Sentence and Sentence
- Sentence → Sentence or Sentence
- Sentence → Noun Verb Noun
- Noun → boys
- Noun → girls
- Noun → bunnies
- Verb → like
- Verb → see

- Examples of Sentences in this language:
 - boys like girls
 - boys like girls and girls like bunnies
 - boys like girls and girls like bunnies and girls like bunnies
 - boys like girls and girls like bunnies and girls like bunnies and girls like bunnies
 -
- What makes this set infinite? Answer: Recursive definition of Sentence

- This grammar is more interesting than the last one because the set of Sentences is infinite

Detour

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- What if we want to add a period at the end of every sentence?
- Sentence → Sentence and Sentence .
- Sentence → Sentence or Sentence .
- Sentence → Noun Verb Noun .
- Noun → ...

Does this work?

No! This produces sentences like:

girls like boys . and boys like bunnies . .

Sentences with Periods

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- PunctuatedSentence → Sentence .
- Sentence → Sentence and Sentence
- Sentence → Sentence or Sentence
- Sentence → Noun Verb Noun
- Noun → boys
- Noun → girls
- Noun → bunnies
- Verb → like
- Verb → see

- Add a new rule that adds a period only at the end of the sentence.
- The tokens here are the 7 words plus the period (.)
- This grammar is ambiguous:
girls like girls
and girls like boys
or girls like bunnies

Uses of Grammars

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- Grammar describes every possible legal expression
 - You could use the grammar for Java to list every possible Java program. (It would take forever)
- Grammar tells the Java compiler how to understand a Java program

Grammar for Simple Expressions

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- E → integer
- E → (E + E)

- Simple expressions:
 - An E can be an integer.
 - An E can be '(' followed by an E followed by '+' followed by an E followed by ')'.
- Set of expressions defined by this grammar is a recursively-defined set
 - Is language finite or infinite?
 - Do recursive grammars always yield infinite languages?

- Here are some legal expressions:
 - 2
 - (3 + 34)
 - ((4+23) + 89)
 - ((89 + 23) + (23 + (34+12)))
- Here are some illegal expressions:
 - (3
 - 3 + 4
- The tokens in this grammar are (, +,), and any integer

Parsing

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- Grammars can be used in two ways
 - A grammar defines a language (i.e., the set of properly structured sentences)
 - A grammar can be used to parse a sentence (thus, checking if the sentence is in the language)
- To parse a sentence is to build a parse tree
 - This is much like diagramming a sentence

Example: Show that ((4+23) + 89) is a valid expression E by building a parse tree

Recursive Descent Parsing

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- Idea: Use the grammar to design a recursive program to check if a sentence is in the language
- To parse an expression E, for instance
 - We look for each terminal (i.e., each token)
 - Each nonterminal (e.g., E) can handle itself by using a recursive call
- The grammar tells how to write the program!

```
boolean parseE() {
    if (first token is an integer) return true;
    if (first token is '(') {
        parseE();
        Make sure there is a '+' token;
        parseE();
        Make sure there is a ')' token;
        return true;
    }
    return false;
}
```

Java Code for Parsing E

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```
public static Node parseE(Scanner scanner) {
    if (scanner.hasNextInt()) {
        int data = scanner.nextInt();
        return new Node(data);
    }
    check(scanner, '(');
    left = parseE(scanner);
    check(scanner, '+');
    right = parseE(scanner);
    check(scanner, ')');
    return new Node(left, right);
}
```

Detour: Error Handling with Exceptions

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- Parsing does two things:
 - It returns useful data (a parse tree)
 - It checks for validity (i.e., is the input a valid sentence?)
- How should we respond to invalid input?
- **Exceptions** allow us to do this without complicating our code unnecessarily

Exceptions

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- Exceptions are usually thrown to indicate that something bad has happened
 - **IOException** on failure to open or read a file
 - **ClassCastException** if attempted to cast an object to a type that is not a supertype of the dynamic type of the object
 - **NullPointerException** if tried to dereference null
 - **ArrayIndexOutOfBoundsException** if tried to access an array element at index $i < 0$ or ε : the length of the array
- In our case (parsing), we should throw an exception when the input cannot be parsed

Handling Exceptions

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- Exceptions can be caught by the program using a **try-catch** block
- **catch** clauses are called **exception handlers**

```
Integer x = null;
try {
    x = (Integer)y;
    System.out.println(x.intValue());
} catch (ClassCastException e) {
    System.out.println("y was not an Integer");
} catch (NullPointerException e) {
    System.out.println("y was null");
}
```

Defining Your Own Exceptions

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- An exception is an object (like everything else in Java)
- You can define your own exceptions and throw them

```
class MyOwnException extends Exception {}
...
if (input == null) {
    throw new MyOwnException();
}
```

Declaring Exceptions

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- In general, any exception that could be thrown must be either declared in the method header or *caught*

```
void foo(int input) throws MyOwnException {
    if (input == null) {
        throw new MyOwnException();
    }
    ...
}
```

- Note: **throws** means "can throw", not "does throw"
- Subtypes of **RuntimeException** do not have to be declared (e.g., **NullPointerException**, **ClassCastException**)
 - These represent exceptions that can occur during "normal operation of the Java Virtual Machine"

How Exceptions are Handled

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- If the exception is thrown from *inside* the **try** clause of a **try-catch** block with a handler for that exception (or a superclass of the exception), then that handler is executed
 - Otherwise, the method terminates abruptly and control is passed back to the calling method
- If the calling method can handle the exception (i.e., if the call occurred within a **try-catch** block with a handler for that exception) then that handler is executed
 - Otherwise, the calling method terminates abruptly, etc.
- If *none* of the calling methods handle the exception, the entire program terminates with an error message

Using a Parser to Generate Code

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- We can modify the parser so that it generates stack code to evaluate arithmetic expressions:
 - 2 PUSH 2
 STOP
 - (2 + 3) PUSH 2
 PUSH 3
 ADD
 STOP
- Goal: Method `parseE` should return a string containing stack code for expression it has parsed
- Method `parseE` can generate code in a recursive way:
 - For integer `i`, it returns string "PUSH" + `i` + "\n"
 - For `(E1 + E2)`,
 - Recursive calls for `E1` and `E2` return code strings `c1` and `c2`, respectively
 - Then to compile `(E1 + E2)`, return `c1 + c2 + "ADD\n"`
 - Top-level method should tack on a `STOP` command after code received from `parseE`

Does Recursive Descent Always Work?

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- There are some grammars that cannot be used as the basis for recursive descent
 - A trivial example (causes infinite recursion):
 - $S \rightarrow b$
 - $S \rightarrow Sa$
- For some constructs, recursive descent is hard to use
- Can use a more powerful parsing technique (there are several, but not in this course)
- Can rewrite grammar
 - $S \rightarrow b$
 - $S \rightarrow bA$
 - $A \rightarrow a$
 - $A \rightarrow aA$

Syntactic Ambiguity

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- Sometimes a sentence has more than one parse tree
 - $S \rightarrow A \mid aaxb$
 - $A \rightarrow a \mid aAb$
 - $B \rightarrow b \mid bB$
 - The string `aaxbb` can be parsed in two ways
- This kind of ambiguity sometimes shows up in programming languages
- if `E1` then if `E2` then `S1` else `S2`
- Which then does the else go with?
- This ambiguity actually affects the program's meaning
- How do we resolve this?
 - Provide an extra non-grammar rule (e.g., the `else` goes with the closest `#`)
 - Modify the language (e.g., an if-statement must end with a 'fi')
 - Operator precedence (e.g., $1 + 2 * 3$ should be parsed as $1 + (2 * 3)$, not $(1 + 2) * 3$)
 - Other methods (e.g., Python uses amount of indentation)

Conclusion

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- Recursion is a very powerful technique for writing compact programs that do complex things
- Common mistakes:
 - Incorrect or missing base cases
 - Subproblems must be simpler than top-level problem
- Try to write description of recursive algorithm and reason about base cases before writing code
 - Why?
 - Syntactic junk such as type declarations, etc. can create mental fog that obscures the underlying recursive algorithm
 - Best to separate the logic of the program from coding details

Exercises

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- Think about recursive calls made to parse and generate code for simple expressions
 - 2
 - (2 + 3)
 - ((2 + 45) + (34 + -9))
- Derive an expression for the total number of calls made to `parseE` for parsing an expression
 - Hint: think inductively
- Derive an expression for the maximum number of recursive calls that are active at any time during the parsing of an expression (i.e. max depth of call stack)

Exercises

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- Write a grammar and recursive program for sentence palindromes that ignores white spaces & punctuation
 - **Was it Eliot's toilet I saw?**
 - **No trace; not one carton**
 - **Go deliver a dare, vile dog!**
 - **Madam, in Eden I'm Adam**
- Write a grammar and recursive program for strings A^nB^n
 - **AB**
 - **AABB**
 - **AAAAAABBBBBB**
- Write a grammar and recursive program for Java identifiers
 - **<letter> [<letter> or <digit>]^{0..N}**
 - **!27, but not 2j7**