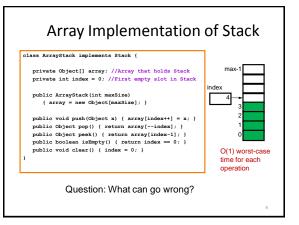
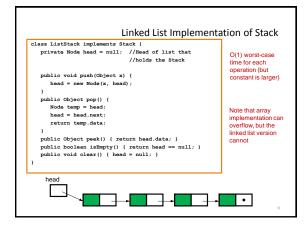
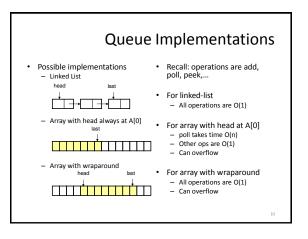


Data Structure Building Blocks

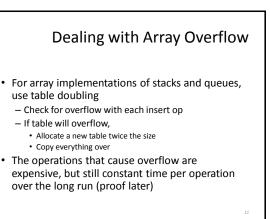
- These are *implementation* "building blocks" that are often used to build more-complicated data structures
 - Arrays
 - Linked Lists (singly linked, doubly linked)
 - Binary Trees
 - Graphs (adjacency matrix, adjacency list)







A Queue From 2 Stacks • Algorithm - Add pushes onto stack A - Poll pops from stack B - If B is empty, move all elements from stack A to stack B • Some individual operations are costly, but still O(1) time per operations over the long run • Check for • Allocat • Copy e • The operative, over the long



Goal: Implement a Dictionary (aka Map) Operations • Array implementation: Using an array of (key,value) pairs - void insert(key, value) void update(key, value) Object find(key) Unsorted Sorted - void remove(key) O(1) O(n) - insert boolean isEmpty() update O(n) O(log n) - void clear() - find O(n) O(log n) remove O(n) O(n) n is the number of items currently held in the dictionary

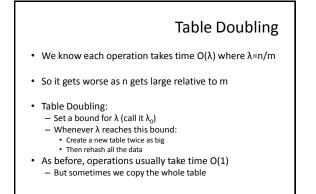
Hashing

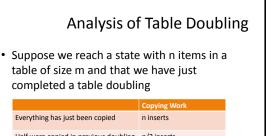
- Idea: compute an array index via a hash function h
 - − U is the universe of keys (e.g. all legal identifiers) − h: U \rightarrow [0,...,m-1]
 - where m = hash table size
- Usually |U| is much bigger than m, so collisions are possible (two elements with the same hash code)
- Hash function h should
 - be easy to compute
 - avoid collisions
 - have roughly equal probability for each table position

	A Hashing Example
 Suppose each word below has the following hash-code jan feb mar mar apr may jun jul aug sep oct sep oct sep 	 How do we resolve collisions? use chaining: each table position is the head of a list for any particular problem, this might work terribly In practice, using a good hash function, we can assume each position is equally likely

Analysis for Hashing with Chaining

- Analyzed in terms of load factor λ = n/m = (items in table)/(table size)
- We count the expected number of probes (i.e. key comparisons)
- Goal: Determine expected number of probes for an unsuccessful search
- Expected number of probes for a successful search = $1 + \lambda/2 = O(\lambda)$
- Worst case is O(n)





Analysis of Table Doubling, Cont'd

- Total number of insert operations needed to reach current table
 = copying work + initial insertions of items
 = 2n + n = 3n inserts
- Each insert takes expected time $O(\lambda_0)$ or O(1), so total expected time to build entire table is O(n)
- Thus, expected time per operation is O(1)
- Disadvantages of table doubling:
 Worst-case insertion time of O(n) is definitely
 - achieved (but rarely) - Thus, not appropriate for time critical operations

Java Hash Functions

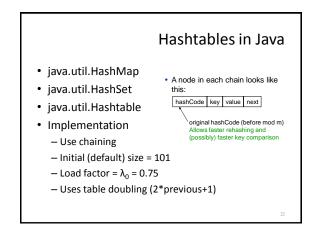
- Most Java classes implement the hashCode () method – hashCode () returns int
- Java's HashMap class uses h(X) = X.hashCode() mod m
- h(X) in detail: int hash = X.hashCode(); int index = (hash & 0x7FFFFFFF) % m;

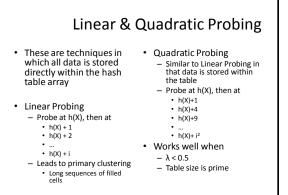
What hashCode () returns for

- Integer:
 - uses the int value
 Float:
 - converts to a bit representation and treats it as an int
 - Short Strings:
 37*previous + value of next character
- Long Strings:
 sample of 8
 - sample of 8 characters; 39*previous + next value

hashCode() Requirements

- Contract for hashCode () method:
 - Whenever it is invoked in the same object, it must return the same result
 - Two objects that are equal (in the sense of equals (...)) must have the same hash code
 - Two objects that are not equal should return different hash codes, but are not required to do so (i.e., collisions are allowed)





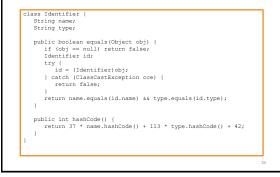
Universal Hashing

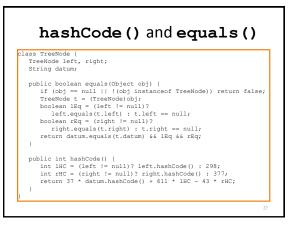
- Choose a hash function at random from a large parameterized family of hash functions (e.g., h(x) = ax + b, where a and b are chosen at random)
- With high probability, it will be just as good as any custom-designed hash function you can come up with

hashCode() and equals()

- We mentioned that the hash codes of two equal objects must be equal — this is necessary for hashtable-based data structures such as HashMap and HashSet to work correctly
- In Java, this means if you override
 Object.equals(), you had better also override Object.hashCode()
- But how???

hashCode() and equals()





Dictionary Implementations

- Ordered Array
 - Better than unordered array because Binary Search can be used
- Unordered Linked List

 Ordering doesn't help
- Hashtables

 O(1) expected time for Dictionary operations