CS/ENGRD 2110 Object-Oriented Programming and Data Structures Spring 2011





Recursion Overview

- Recursion is a powerful technique for specifying functions, sets, and programs
- · Example recursively-defined functions and programs
 - factorial
 - combinations
 - exponentiation (raising to an integer power)
 solution of combinatorial problems (i.e. search)
- Example recursively-defined sets
 - grammars
 - expressions
 data structures (lists to
 - data structures (lists, trees, ...)

The Factorial Function (n!) fine: $n! = n \cdot (n-1) \cdot (n-2) \cdots 3 \cdot 2 \cdot 1$

- Define: n! = n·(n-1)·(n-2)···3·2·1

 read: "n factorial"
 - − E.g., 3! = 3·2·1 = 6
- The function int → int that gives n! on input n is called the factorial function
- n! is the number of permutations of n distinct objects
 - There is just one permutation of one object. 1! = 1
 There are two permutations of two objects: 2! = 2
 - 12 21 - There are six permutations of three objects: 3! = 6
 - 123 132 213 231 312 321





General Approach to Writing Recursive Functions

- Try to find a parameter, say n, such that the solution for n can be obtained by combining solutions to the same problem using smaller values of n (e.g., (n-1)!) (i.e. recursion)
- Find base case(s) small values of n for which you can just write down the solution (e.g., 0! = 1)
- Verify that, for any valid value of n, applying the reduction of step 1 repeatedly will ultimately hit one of the base cases













- Determine argument values for which recursive case does not apply
- Introduce a base case for each one of these

Recursive Program for Combinations $\binom{n}{r} = \binom{n-1}{r} + \binom{n-1}{r-1}, \quad n > r > 0$ $\binom{n}{n} = 1$ $\binom{n}{0} = 1$ static int combs(int n, int r) { //assume n>=r>=0 if (r == 0 || r == n) return 1; //base cases else return combs(n-1,r) + combs(n-1,r-1); }





















Conclusion

- Recursion is a convenient and powerful way to define functions
- Problems that seem insurmountable can often be solved in a "divide-and-conquer" fashion:
 - Reduce a big problem to smaller problems of the same kind, solve the smaller problems
 - Recombine the solutions to smaller problems to form solution for big problem
- Important application: parsing