









■Basic step:

- input or output of a scalar value
 accessing the value of a scalar variable, array element, or field of an object
- an object assignment to a variable, array element, or field of an object
- a single arithmetic or logical operation
- method invocation (not counting
- argument evaluation and execution of the method body)

For a conditional, count number of basic steps on the branch that is executed

For a loop, count number of basic steps in loop body times the number of iterations

For a method, count number of basic steps in method body (including steps needed to prepare stack-frame)











Problem-	Size Exar	nples	
 Suppose we execute 10 problem ca 	e have a comp 00 operations n we solve?	uting device per second;	that can how large a
	1 second	1 minute	1 hour
n	1000	60,000	3,600,000
n log n	140	4893	200,000
n ²	31	244	1897
3n ²	18	144	1096
n ³	10	39	153
2 ⁿ	9	15	21

O(1)	constant	excellent
O(log n)	logarithmic	excellent
O(n)	linear	good
O(n log n)	n log n	pretty good
O(n ²)	quadratic	OK
O(n ³)	cubic	maybe OK
O(2 ⁿ)	exponential	too slow



Our Simplifying Assumptions

 \Box Use the size of the input rather than the input itself – n

 $\hfill\square\ensuremath{\mathsf{Count}}$ the number of "basic steps" rather than computing exact times

□ Multiplicative constants and small inputs ignored (order-of, big-O)

Determine number of steps for either
worst-case
expected-case

15

□These assumptions allow us to analyze algorithms effectively

















Summary

25

- Asymptotic complexity
- Asymptotic complexity
 Used to measure of time (or space) required by an algorithm
 Measure of the algorithm, not the problem
 Searching a sorted array

 - Linear search: O(n) worst-case time
 Binary search: O(log n) worst-case time
- Matrix operations:
 - Note: n = number-of-rows = number-of-columns
 Matrix-vector product: O(n²) worst-case time
 Matrix-matrix multiplication: O(n³) worst-case time
- More later with sorting and graph algorithms