

- Previous topics:
  - Branching
  - Boolean expressions
- Now:
  - Introduction to `for`-loop

Question

A stick of unit length is split into two pieces. The breakpoint is randomly selected. On average, how long is the shorter piece?

Physical experiment? ♦  
 Thought experiment? → analysis  
 Computational experiment! → simulation ♦

♦ Need to repeat many trials!

```
% one trial of the experiment
breakPt= rand;
if breakPt<0.5
    shortPiece= breakPt;
else
    shortPiece= 1-breakPt;
end
```

```
% one trial of the experiment
breakPt= rand;
shortPiece= min(breakPt, 1-breakPt);
```

Want to do many trials, add up the lengths of the short pieces, and then divide by the number of trials to get the average length.

Repeat n times

```
% one trial of the experiment
breakPt= rand;
shortPiece= min(breakPt, 1-breakPt);
```

Take average

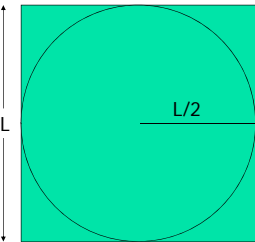
Print result

```
n= 10000; % number of trials
total= 0; % accumulated length so far

for k= 1:n
    % one trial of the experiment
    breakPt= rand;
    shortPiece= min(breakPt, 1-breakPt);
    total= total + shortPiece;
end

aveLength= total/n
fprintf('Average length is %f\n', ...
        aveLength)
```

### Monte Carlo Estimation of $\pi$



Throw  $N$  darts

Sq. area =  $N = L \times L$

Circle area =  $N_{in}$   
 $= \pi L^2 / 4$

$\pi = 4 N_{in} / N$

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### Monte Carlo Approximation of Pi

For each of  $N$  trials  
 Throw a dart  
 If it lands in circle  
 add 1 to total # of hits

Pi is  $4 \cdot \text{hits} / N$

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### Monte Carlo Pi with $N$ darts on $L$ -by- $L$ board

```

hits = 0;
for k = 1:N
    % Throw kth dart
    x = rand*L - L/2;
    y = rand*L - L/2;
    % Is it in the circle?
    if sqrt(x^2+y^2) <= L/2
        hits = hits + 1;
    end
end
myPi = 4*hits/N;
    
```

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### Syntax of the for loop

```

for <var>= <start value>:<incr>:<end bound>
    statements to be executed repeatedly
end
    
```

Loop body

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### Syntax of the for loop

```

for <var>= <start value>:<incr>:<end bound>
    statements to be executed repeatedly
end
    
```

Loop header specifies all the values that the index variable will take on, one for each pass of the loop.

Eg,  $k = 3:1:7$  means  $k$  will take on the values 3, 4, 5, 6, 7, one at a time.

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### Pattern for doing something $n$ times

```

n= _____
for k= 1:n
    % code to do
    % that something
end
    
```

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**for** loop examples

```

for k= 2:0.5:3
    disp(k)
end
for k= 1:4
    disp(k)
end
for k= 0:-2:-6
    disp(k)
end
for k= 0:-2:-7
    disp(k)
end
for k= 5:2:1
    disp(k)
end
    
```

**k** takes on the values \_\_\_\_\_  
 Non-integer increment is OK

**k** takes on the values \_\_\_\_\_  
 Default increment is 1

**k** takes on the values \_\_\_\_\_  
 "Increment" may be negative

**k** takes on the values \_\_\_\_\_  
 Colon expression specifies a bound

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Example: count down to blast off

- Write a script `countDown` that produces this screen output after asking user to input starting value (4 in this example):

```

T = 4 seconds
T = 3 seconds
T = 2 seconds
T = 1 second
Blast off!!!!
    
```

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```

% What will be printed?
for k= 1:2:6
    fprintf('%d ', k)
end
    
```

A: 1 2 3 4 5 6  
 B: 1 3 5 6  
 C: 1 3 5  
 D: error (incorrect bounds)

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```

% What will be printed?
for k= 10:-1:14
    fprintf('%d ', k)
end
fprintf('!')
    
```

A: error (incorrect bounds)  
 B: 10 (then error)  
 C: 10 !  
 D: 14 !  
 E: !

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