Check that your exam has six (6) pages including this one.
1. Complete the following function so that it performs as specified

```matlab
function [alfa,i,j] = MaxOfAll(C)
% C is a cell array of vectors C{1},...,C{n}
% alfa is the largest numerical value that can be found in C.
% i and j are indices with the property that alfa is the value of C{i}(j)

Thus, if

C = { [ 10 -50 20], [13 5], [40 10 18 6]}
[alfa,i,j] = MaxOfAll(C)

then the value of alfa, i, and j would be 40, 3, and 1 respectively. For full credit your solution should make effective use of the max function\(^1\).

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\(^1\)For your information, if [beta,idx] = max([-20 30 10 15]), then the value of beta is 30 and the value of idx is 2.
2. Assume the availability of the following functions

```matlab
function P = MakePoint(x,y)
% P is a point structure.
% P.x and P.y are assigned the coordinate values x and y.

function d = Dist(P1,P2)
% P1 and P2 are points and d is the distance between them

function E = MakeOrbit(P,A,phi,N)
% P, A, and phi are the perihelion, aphelion, and tilt (degrees) of
% a rotated Kepler Orbit
% N is a positive integer (>=2) that specifies the number of points that
% will make up the discrete rotated orbit.
% E is a 4-field structure that represents a discrete version of the orbit
% E.Q is a length N structure array whose components are points on the orbit
% E.s is the string-value of the orbit.
% E.F1 is a point that identifies the location of the Sun, i.e., (0,0)
% E.F2 is a point that identifies the location of the phantom focus.

Recall that a point is inside an ellipse if the sum of its distances to the two ellipse foci is less than the ellipse string value. Complete the following function so that it performs as specified

```matlab
function alfa = Inside(E1,E2)
% E1 and E2 are discrete orbits
% alfa is 1 if all points on E1 are inside the rotated Kepler orbit associated with E2.
% Otherwise, alfa is 0.

Efficiency matters.
3. The `uint8` range can be broken into four **quartile intervals**: $Q_1 = [0, 63]$, $Q_2 = [64, 127]$, $Q_3 = [128, 191]$, and $Q_4 = [192, 255]$. (Note that it is easy to determine the quartile interval of a `uint8` value by using `ceil`.) Complete the following function so that it performs as specified.

```matlab
function V = Profile(fName)
    % fName is the name of a .jpg file in the current directory that encodes an image.
    % V is a 4-by-4-by-4 array with the property that V(i,j,k) is the
    % number of pixels in the image with the property that
    % its red value is in the i-th quartile (1<=i<=4)
    % its green value is in the j-th quartile (1<=j<=4)
    % its blue value is in the k-th quartile (1<=k<=4)

    A = imread([fName '.jpg']);

    : ;
```
4. The `sort` function\(^2\) can be used to identify the median value in a vector:

\[
[y, \text{idx}] = \text{sort}(x);
\]
\[
n = \text{length}(x);
\]
\[
\text{medIndex} = \text{idx(ceil(n/2))};
\]
\[
\text{medianValue} = x(\text{medIndex});
\]

We assume here and throughout this problem that \(n\) is odd. Complete the following function so that it performs as specified:

```matlab
function [xBelow, xAbove] = Split(x)
    % x is a length-n column vector with distinct values.
    % n is odd and n>=3.
    % xBelow is a sorted column vector of all values in x that are strictly less
    % than the median of x.
    % xAbove is a sorted column vector of all values in x that are strictly larger
    % than the median of x.

    y = sort(x);
    n = length(x);
    medIndex = idx(ceil(n/2));
    medianValue = x(medIndex);

    % xBelow
    for i = 1:n/2
        xBelow = [xBelow; x(i)];
    end
    % xAbove
    for i = n/2+1:n
        xAbove = [xAbove; x(i)];
    end
```

Thus, if \(x = [30; 70; 10; 20; 40; 60; 50]\), then \(xBelow = [10; 20; 30]\) and \(xAbove = [50; 60; 70]\). For full credit, your solution must NOT be vectorized.

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\(^2\)For your information, if \([y, \text{idx}] = \text{sort}([20 40 10 30])\) then \(y = [10 20 30 40]\) and \(\text{idx} = [3 1 4 2]\).
5. (a) Assume that $n$ is a positive integer and that we have the following length-60 string of amino acid mnemonics:

$$\text{Names} = \text{'AlaArgAsnAspCysGluGlnGlyHisIleLeuLysMetPheProSerThrTrpTyrVal'};$$

(a) Write a fragment that generates a random length-$n$ protein. Represent the protein in a length-$n$ cell array $C$. Make effective use of strcmp\(^3\).

(b) Write a fragment that generates a random length-$n$ protein with the property that adjacent amino acids are different. Represent the protein in a length-$n$ cell array. Thus, if $n = 4$ then

$$C = \{ \text{'Cys'}, \text{'Phe'}, \text{'Cys'}, \text{'Met'} \}$$

is OK but

$$C = \{ \text{'Cys'}, \text{'Phe'}, \text{'Phe'}, \text{'Met'} \}$$

is not.

\(^3\text{Recall that strcmp(s1,s2) is 1 if the strings s1 and s2 are identical and is 0 otherwise.}\)