

Name: \_\_\_\_\_  
 (Legibly print last name, first name, middle name)

NetID: \_\_\_\_\_

Statement of integrity:

I did not, and will not, violate the rules of academic integrity on this exam.

\_\_\_\_\_ (Signature)

Q1: (20)	_____	_____
Q2: (10)	_____	_____
Q3: (20)	_____	_____
Q4: (20)	_____	_____
Q5: (30)	_____	_____
Total: (100)	_____	_____

Circle your lecture time: 9:05 or 11:15

Circle your section instructor's name:

	<i>Tuesday</i>	<i>Wednesday</i>
10:10		Utkarsh Prateek
11:15		Tim Condon
12:20	Stefan Ragnarsson	Tim Condon
1:25	Stefan Ragnarsson	Myle Ott
2:30	Josef Broder	Myle Ott
3:35	Josef Broder	Myle Ott
7:30		Vivek Maharajh
8:35		Vivek Maharajh

Instructions:

- This is a 90-minute, closed-book exam; no calculators are allowed.
- The exam is worth a total of 100 points, so it's about one point per minute!
- Read each problem completely, including any provided code, before starting it.
- Raise your hand if you have any questions.
- Use the backs of pages or ask for additional sheets of paper as necessary.
- Clarity, conciseness, and good programming style count for credit.
- If you supply multiple answers, we will grade only *one*.
- Use only MATLAB code. No credit for code written in other programming languages.
- Assume there will be no input errors.
- **Do not use arrays. Do not write user-defined functions.**
- Do not use `switch`, `try`, `catch`, or `break` statements.
- You may find the following MATLAB predefined functions useful:  
`abs`, `sqrt`, `rem`, `rand`, `floor`, `ceil`, `input`, `fprintf`, `disp`

Examples: `rem(5,2)` → 1, the remainder of 5 divided by 2  
`rand(1)` → a random real value in the interval (0,1)  
`floor(6.9)`, `floor(6)` → 6, rounds down to the nearest integer  
`ceil(8.1)`, `ceil(9)` → 9, rounds up to the nearest integer

## Question 1: (20 points)

### Part (a): (12 points)

Suppose the following fragment has been executed:

```
% The first interval [a1,b1] has these endpoints:  
a1 = rand(1); b1 = a1+rand(1);  
% The second interval [a2,b2] has these endpoints:  
a2 = rand(1); b2 = a2+rand(1);  
% Assume a1, b1, a2, and b2 are unique.
```

(i) Complete the following fragment so that it prints 'Yes' if the second interval is inside the first interval and 'No' otherwise.

```
if -----  
    disp('Yes')  
else  
    disp('No')  
end
```

(ii) Complete the following fragment so that it prints 'No' if the the intervals fail to intersect and 'Yes' otherwise.

```
if -----  
    disp('No')  
else  
    disp('Yes')  
end
```

### Part (b): (8 points)

Write the loop condition below so that the fragment keeps prompting the user to enter a number until the value entered is positive and is a multiple of 3 or 5.

```
n = input('Enter a number: ');  
  
while -----  
  
    n = input('Enter a number: ');  
  
end
```

## Question 2: (10 points)

### Part (a): (3 points)

What is the last line of output after executing the following fragment?

```
x = 2;
y = x*3;
while x<=6 && y<=6
    x = x + 2;
    disp(x)
end
```

*Answer:*

### Part (b): (7 points)

The following fragment calculates and displays the first few Fibonacci numbers. When the fragment finishes execution, which Fibonacci numbers are stored in variables `f_old`, `f_cur`, and `f_new`? You can, but don't have to, evaluate the Fibonacci numbers. For example, you can write  $f_4$  instead of its value 3.

```
n = 2;
f_old = 1    % f(1)
f_cur = 1    % f(2)
for n = 3:5
    f_new = f_old + f_cur
    f_old = f_cur;
    f_cur = f_new;
end
```

f_old:	f_cur:	f_new:
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### Question 3: (20 points)

A certain bacteria has a growth rate that is dependent on the ambient temperature. At or below 32°F, there is no growth. Above 32°F the growth rate follows the formula

$$aT^2 + b$$

where  $T$  is ambient temperature in °F, and  $a = 0.01$  and  $b = -10$  are model parameters. When the temperature is very high, above 90°F, the rate estimated by the above formula must be corrected by a reduction of 10%.

Complete the fragment below to compute and display the growth rate.

```
T = input('What is the temperature? ');  
  
% Calculate and display the growth rate of the bacteria
```

### Question 4: (20 points)

A *unit hexagon* centered at  $(a, b)$  has vertices

$$P_1 : (a + \Delta_x, b + \Delta_y)$$

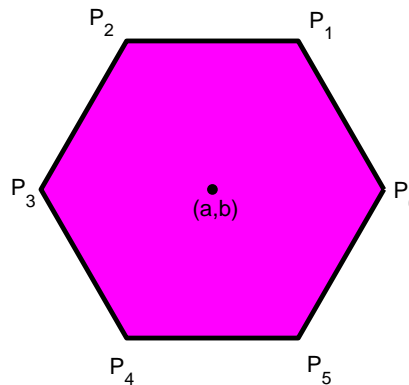
$$P_2 : (a - \Delta_x, b + \Delta_y)$$

$$P_3 : (a - 1, b)$$

$$P_4 : (a - \Delta_x, b - \Delta_y)$$

$$P_5 : (a + \Delta_x, b - \Delta_y)$$

$$P_6 : (a + 1, b)$$



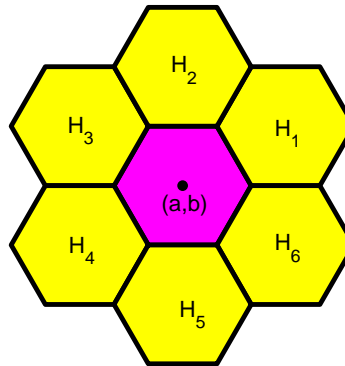
where  $\Delta_x = 1/2$  and  $\Delta_y = \sqrt{3}/2$ . Assume that the function `DrawHex(a, b)` adds to the figure window a unit hexagon with center at  $(a, b)$ .

We say that a unit hexagon is “good” if it is entirely inside a square with vertices  $(0,0)$ ,  $(10,0)$ ,  $(10,10)$ , and  $(0,10)$ . Write a program fragment to randomly choose points from a square with vertices  $(0,0)$ ,  $(10,0)$ ,  $(10,10)$ , and  $(0,10)$ —each coordinate is uniformly random in the interval  $(0,10)$ . Whenever there is a point that can be the center of a *good* hexagon, draw the hexagon. Your fragment should draw exactly 100 good hexagons. Do not write code to set up the figure window and axes.

## Question 5: (30 points)

A unit hexagon has six unit hexagon neighbors with these centers

$$\begin{aligned} H_1 & : (a + 3\Delta_x, b + \Delta_y) \\ H_2 & : (a, b + 2\Delta_y) \\ H_3 & : (a - 3\Delta_x, b + \Delta_y) \\ H_4 & : (a - 3\Delta_x, b - \Delta_y) \\ H_5 & : (a, b - 2\Delta_y) \\ H_6 & : (a + 3\Delta_x, b - \Delta_y) \end{aligned}$$



where  $\Delta_x = 1/2$  and  $\Delta_y = \sqrt{3}/2$ . Assume that the function `DrawHex(a,b)` adds to the figure window a unit hexagon with center at  $(a,b)$ .

Complete the fragment below to draw  $K$  columns of a “slanted” bee hive. Each column is made up of  $n$  unit hexagons. Center the top left hexagon on the origin  $(0,0)$ . An example with 5 hexagons in each of 3 columns is shown below. Do not write code to set up the figure window and axes.

```
n = input('How many hexagons in each column? ');
K = input('How many columns? ');

% Draw a slanted bee hive with n hexagons in each
% of K columns
```

