







Variable Definitions

- x: the x-value of the left tangent point for a given circle.
- d : the diameter of a given circle







| F | Refineme | ent | |
|------------------------|-------------------------|------------------------|----|
| U | pdate x and | d? | |
| Dis | s <mark>k x</mark> | d | |
| 1 2 3 | 0 0+1 0+1+1/ | 1 1/2 2 1/4 | |
| Next x is Next d is | current x one-half c | + current urrent d. | d. |





```
DrawDisk(x+d/2,0,d/2,'y')
   x = x+d;
   d = d/2;
end
```

 $\mathbf{x} = 0;$ d = 1;







The Discrete Display of Sine

```
N = 100;
X_spacing = 4*pi/N;
Dot_radius = X_spacing/3;
for k=0:N
    x = k*X_spacing;
    y = sin(x);
    DrawDisk(x,y,Dot_Radius,'r')
end
```

The Moral

To produce <u>realistic</u> plots/renderings you must <u>appreciate</u> <u>screen granularity</u>.

Similar Finite "Behavior" with Computer Arithmetic

Memory Hardware is finite.

Computer cannot store never-ending decimals like pi, sqrt(2), 1/3.

Question Time

Does this script print anything?
k = 0;
while 1 + 1/2^k > 1
k = k+1;
end
k = k
A. Yes B. No E. None of these

















The 1991 Patriot Missile Disaster



Elementary misperceptions about the finiteness of computer arithmetic. 30+ died.

The Setting External clock counts time in tenths of seconds. Targeting software needs time to compute trajectories. The method: Time = (# external clock ticks) × (1/10)

One-Tenth in Binary

Exact:

.0001100110011001100110011...

Patriot System used:

.0001100110011001100110011...

Error = .00000095sec every clock tick

Error

Time = (# external clock ticks) \times (1/10)

Error = (# external clock ticks) x (.000000095)

After 100 hours...

Error = (100×60×60*10)*.00000095 = .34 secs

Missed target by 500 meters.