# L11. User-Defined Functions 

Input parameters
Local Variables
Output Values

## Why?

# 1. Elevates reasoning by hiding details. 

2. Facilitates top-down design.
3. Software management.

## Elevates Reasoning

Nice to have sqrt function when designing a quadratic equation solver.

You get to think at the level of $a x^{2}+b x+c=0$

## Elevates Reasoning

Easier to understand the finished quadratic equation solving code:

$$
\begin{aligned}
& \text { r1 }=\left(-b+\operatorname{sqrt}\left(b^{\wedge} 2-4^{*} a^{*} c\right)\right) /\left(2^{*} a\right) ; \\
& \text { r2 }=\left(-b-\operatorname{sqrt}\left(b^{\wedge} 2-4^{*} a^{*} c\right)\right) /\left(2^{*} a\right) ;
\end{aligned}
$$

## Facilitates Top-Down Design



## Facilitates Top-Down Design

1. Focus on how to draw the flag given just a specification of what the functions DrawRect and DrawStar do.
2. Figure out how to implement DrawRect and DrawStar.

## To Specify a Function...

You describe how to use it, e.g.,
function DrawRect(a,b,L,W,c)
\% Adds rectangle to current window.
\% Assumes hold is on. Vertices are
\% ( $a, b),(a+L, b),(a+L, b+W), \&(a, b+W)$
\% The color $c$ is one of 'r','g',
\%'y','b','w','k','c',or 'm'.

## To Implement a Function...

You write the code so that the function works. I.e., code that "lives up to" the specification. E.g.,

$$
\begin{aligned}
& x=[a \operatorname{a+L} a+L a \operatorname{a}] ; \\
& y=[b \text { b b+W b+W b]; } \\
& \text { fill }(x, y, c) ;
\end{aligned}
$$

Not to worry. You will understand this soon.

## Software Management

Today:
I write a function
EPerimeter (a,b)
that computes the perimeter of the ellipse

$$
\left(\frac{x}{a}\right)^{2}+\left(\frac{y}{b}\right)^{2}=1
$$

## Software Management

## During the Next 10 years :

You write software that makes extensive use of

EPerimeter(a,b)

Imagine 100's of programs each with several lines that reference EPerimeter

## Software Management

After 10 years :
I discover a more efficient way to approximate ellipse perimeters. I change the implementation of

EPerimeter (a,b)

You do not have to change your software at all.

## Example 1. MySqrt(A)

Recall that we can approximate square roots through the process of ractangle averaging

$$
\begin{aligned}
& \mathrm{L}=\mathrm{A} ; \mathrm{W}=\mathrm{A} / \mathrm{L} ; \\
& \mathrm{L}=(\mathrm{L}+\mathrm{W}) / 2 ; \mathrm{W}=\mathrm{A} / \mathrm{L} ; \\
& \mathrm{L}=(\mathrm{L}+\mathrm{W}) / 2 ; \mathrm{W}=\mathrm{A} / \mathrm{L} ; \\
& \text { etc }
\end{aligned}
$$

## Package this Idea...

$$
L=A ; W=A / L ;
$$

for $k=1: 10$
$L=(L+W) / 2 ; W=A / L ;$
end
$s=(L+W) / 2 ;$

## A User-Defined Function...

function $s=\operatorname{MySqrt}(A)$
L = A; W = A/L;
for $k=1: 10$

$$
L=(L+W) / 2 ; W=A / L ;
$$

end
s = (L+W)/2;

## A Function Begins with a Header

function s = MySqrt(A)
L = A; W = A/L;
for $k=1: 10$

$$
L=(L+W) / 2 ; W=A / L ;
$$

end

$$
s=(L+W) / 2 ;
$$

## A Function Has a Name

function $s=$ MySqrt $A$ )
L = A; W = A/L;
for $k=1: 10$

$$
L=(L+W) / 2 ; W=A / L ;
$$

end

$$
s=(L+W) / 2 ;
$$

## Input Arguments

function $s=\operatorname{MySqrt(A)}$
L = A; W = A/L;
for $k=1: 10$

$$
L=(L+W) / 2 ; W=A / L ;
$$

end
s = (L+W)/2;

## Output Arguments

function $s=\operatorname{MySqrt}(A)$
L = A; W = A/L;
for $k=1: 10$

$$
L=(L+W) / 2 ; W=A / L ;
$$

end

$$
s=(L+W) / 2 ;
$$

## Think of MySqrt as a Factory


$=$ Our method for approximating sqrt(A)

## Hidden Inner Workings



Can use MySqrt w/o knowing how it works.

## Practical Matters

The code sits in a separate file.
MySqrt.m
function s = MySqrt(A)
L = A; W = A/L;
for $k=1: 10$

$$
L=(L+W) / 2 ; W=A / L ;
$$

end

$$
s=(L+W) / 2 ;
$$

## Practical Matters

The .m file has the same name as the function.

Thus, in MySqrt.m you will find an implementation of MySqrt.

## Practical Matters

The first non-comment in the file must be the function header statement.
E.9.,
function $s=\operatorname{MySqrt}(A)$

## Syntax

## function <br> 



Name. Same rules as variable names


List of input parameters.

List of output parameters.

## Practical Matters

For now*, scripts and other Functions that reference MySqrt must be in the same directory. MyDirectory

Script1.m
MySqrt.m
Script2.m
Script3.m

OtherF.m

*The path function gives greater flexibility. More later.

## Using MySqr $\dagger$

r1 = (-b+MySqrt(b^2-4*a*c))/(2*a);
$r 2=\left(-b-M y S q r t\left(b^{\wedge} 2-4^{*} a^{*} c\right)\right) /(2 * a) ;$

## Understanding Function Calls

There is a substitution mechanism.

Local variables are used to carry out the computations.

## Script

 functionfunction $y=f(x)$
$z=2 * x$
$y=z+1$

Let's execute the script line-by-line and see what happens during the call to $f$.

## Script

## function

$$
\begin{aligned}
& a=1 \\
& b=f(2) \\
& c=3
\end{aligned}
$$

function $y=f(x)$
z = 2*x
$y=z+1$

$x, y, z$ serve as local variables during the process. $x$ is referred to as an input parameter.

- $\mathbf{a}=1$

$$
b=f(2)
$$

function $y=f(x)$
$z=2 * x$

$$
c=3
$$

$y=z+1$

Green dot tells us what the computer is currently doing.

## Control passes to the function.

$$
\begin{aligned}
a & =1 \\
b & =f(2) \\
c & =3
\end{aligned}
$$

- function $y=f(x)$

$$
\begin{aligned}
& z=2^{*} x \\
& y=z+1
\end{aligned}
$$



## x: 2

The input
value is assigned to $x$

## Control passes to the function.

$$
\begin{aligned}
a & =1 \\
b & =f(2) \\
c & =3
\end{aligned}
$$



The input value is assigned to $x$

$$
\begin{aligned}
a & =1 \\
b & =f(2) \\
c & =3
\end{aligned}
$$

function $y=f(x)$

$$
\begin{aligned}
z & =2^{*} x \\
y & =z+1
\end{aligned}
$$

x: 2
z: 4

$$
\begin{aligned}
a & =1 \\
b & =f(2) \\
c & =3
\end{aligned}
$$


function $y=f(x)$
$z=2 * x$

- $y=z+1$


Control passes back to the calling program

$$
\begin{aligned}
a & =1 \\
b & =f(2) \\
c & =3
\end{aligned}
$$

a: 1
b: 5

## function $y=f(x)$ <br> z = 2*x <br> y = $\mathrm{z}+1$

After the the value is passed back, the call to the function ends and the local variables disappear.

$$
\begin{aligned}
a & =1 \\
b & =f(2) \\
c & =3
\end{aligned}
$$

function $y=f(x)$
z = 2*x
$y=z+1$
a: 1
b: 5
c: 3

## Repeat to Stress the distinction between local variables and

variables in the calling program.

## Script

 function$$
\begin{aligned}
& z=1 \\
& x=f(2) \\
& y=3
\end{aligned}
$$

function $y=f(x)$
$z=2 * x$
$y=z+1$

Let's execute the script line-by-line and see what happens during the call to $f$.

- $z=1$
$x=f(2)$
$y=3$
function $y=f(x)$
$z=2 * x$
$y=z+1$
z: 1
Green dot tells us what the computer does next.


## Control passes to the function.

$$
\begin{aligned}
z & =1 \\
x & =f(2) \\
y & =3
\end{aligned}
$$

- function $y=f(x)$

$$
\begin{aligned}
& z=2^{*} x \\
& y=z+1
\end{aligned}
$$



## x: 2

The input
value is assigned to $x$

$$
\begin{aligned}
z & =1 \\
x & =f(2) \\
y & =3
\end{aligned}
$$

function $y=f(x)$

$$
\begin{aligned}
z & =2 * x \\
y & =z+1
\end{aligned}
$$

z: 4

This does NOT change

function $y=f(x)$
oz $=2 * x$
$y=z+1$


## Because this is the current context

$$
\begin{aligned}
z & =1 \\
x & =f(2) \\
y & =3
\end{aligned}
$$

function $y=f(x)$
z = 2*x

- $y=z+1$



## Control passes back to the calling program

$$
\begin{aligned}
z & =1 \\
x & =f(2) \\
y & =3
\end{aligned}
$$

z: 1
x: 5

$$
\begin{aligned}
& \text { function } y=f(x) \\
& z=2^{*} x \\
& y=z+1
\end{aligned}
$$

After the the value is passed back, the function "shuts down"

$$
\begin{aligned}
z & =1 \\
x & =f(2) \\
y & =3
\end{aligned}
$$

function $y=f(x)$
$z=2 * x$
$y=z+1$
z: 1
x: 5
y: 3

## Question Time

$$
\begin{array}{ll}
x=1 ; & \text { function } y=f(x) \\
x=f(x+1) ; & x=x+1 ; \\
y=x+1 & y=x+1 ;
\end{array}
$$

What is the output?

$$
\begin{array}{lllll}
\text { A. } 1 & \text { B. } 2 & \text { C. } 3 & \text { D. } 4 & \text { E. } 5
\end{array}
$$

## Question Time

$$
\begin{array}{ll}
x=1 ; & \text { function } y=f(x) \\
x=f(x+1) ; & x=x+1 ; \\
y=x+1 & y=x+1 ;
\end{array}
$$

What is the output?
A. 1
B. 2
C. 3
D. 4
E. 5

## Back to MySqr $\dagger$

function s = MySqrt(A)
\% $A$ is a positive real number $\%$ and s is an approximation \% to its square root.

The specification is given in the form of comments just after the header statement.

## Back to MySqrt

function s = MySqrt(A)
\% $A$ is a positive real number $\%$ and $s$ is an approximation \% to its square root.

It must be clear, complete, and concise.

## Back to MySqrt

function s = MySqrt(A)
\% $A$ is a positive real number $\%$ and s is an approximation \% to its square root.
$-\infty$ If ever you write a function with no specification!!!

