Previous Lecture:

- Vectors
- Color computation
- Linear interpolation

Today's Lecture:

- Vectorized operations
- 2-d array—matrix

Announcements:

- Discussion this week in classrooms as listed in Student Center
- Prelim I on 10/16 (Thursday) at 7:30pm

Initialize arrays if dimensions are known

... instead of "building" the array one component at a time

```
% Initialize y
x=linspace(a,b,n);
y=zeros(1,n);
for k=1:n
    y(k)=myF(x(k));
end
```

```
% Build y on the fly
x=linspace(a,b,n);

for k=1:n
   y(k)=myF(x(k));
end
```



Lecture 13

Drawing a polygon (multiple line segments)

Fill in the missing vector values!

Drawing a polygon (multiple line segments)

```
% Draw a rectangle with the lower-left
% corner at (a,b), width w, height h.
x= [a a+w a+w a a]; % x data
y= [b b b+h b+h b]; % y data
plot(x, y)
```

Coloring a polygon (fill)

```
% Draw a rectangle with the lower-left
% corner at (a,b), width w, height h,
% and fill it with a color named by c.
x=[a a+w a+w a a]; % x data
y=[b b b+h b+h b]; % y data
fill(x, y, c)
         A built-in function
```

Coloring a polygon (fill)

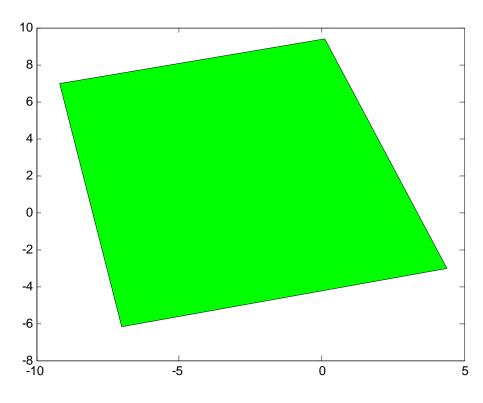
```
% Draw a rectangle with the lower-left
% corner at (a,b), width w, height h,
% and fill it with a color named by c.
x= [a a+w a+w a a]; % x data
y= [b b b+h b+h b]; % y data
fill(x, y, c)
```

Built-in function **fill** actually does the "wrap-around" automatically.

Coloring a polygon (fill)

$$x = [0.1 - 9.2 - 7 4.4];$$
 $y = [9.4 7 -6.2 -3];$
 $fill(x,y,'g')$

Can be a vector (RGB values)



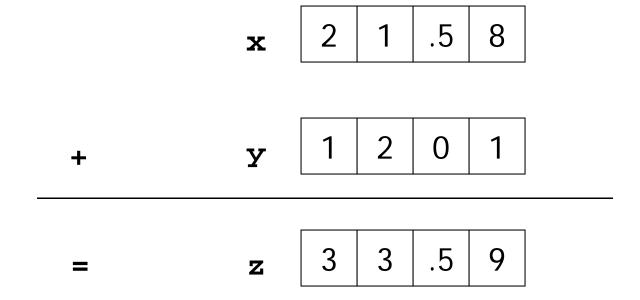
Vectorized code

—a Matlab-specific feature

See Sec 4.1 for list of vectorized arithmetic operations

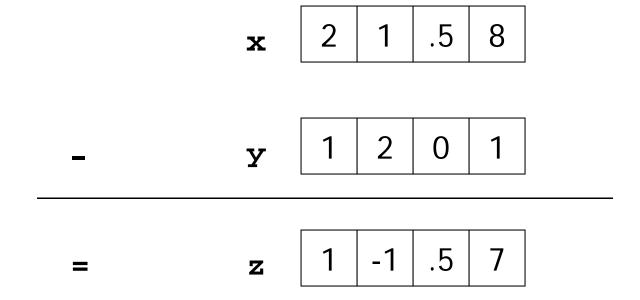
- Code that performs element-by-element arithmetic/relational/logical operations on array operands in one step
- Scalar operation: x + y
 where x, y are scalar variables
- Vectorized code: x + y where x and/or y are vectors. If x and y are both vectors, they must be of the same shape and length

Vectorized addition



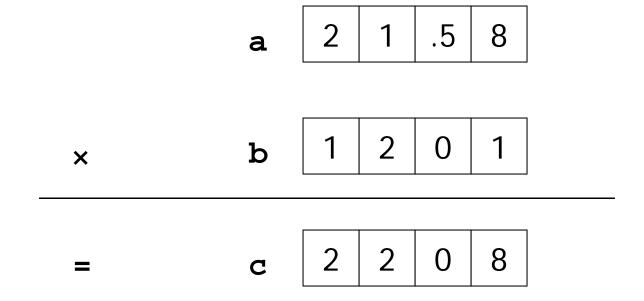
Matlab code: z = x + y

Vectorized subtraction



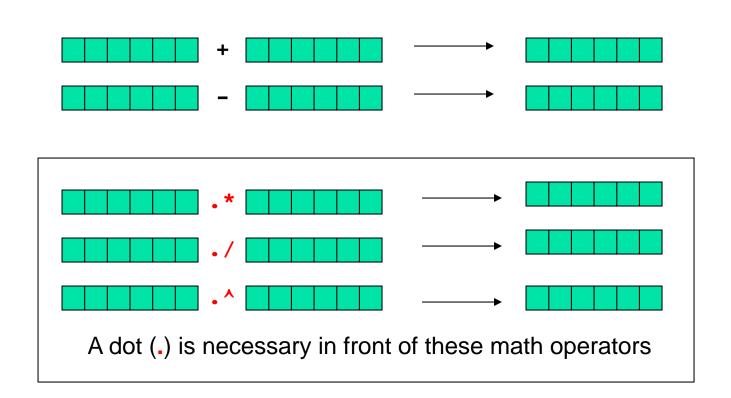
Matlab code: z = x - y

Vectorized multiplication



See full list of ops in §4.1

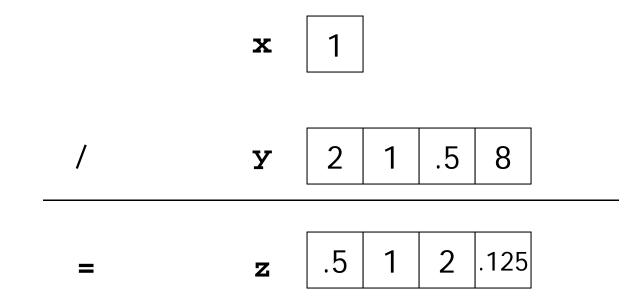
Vectorized element-by-element arithmetic operations on arrays



Shift

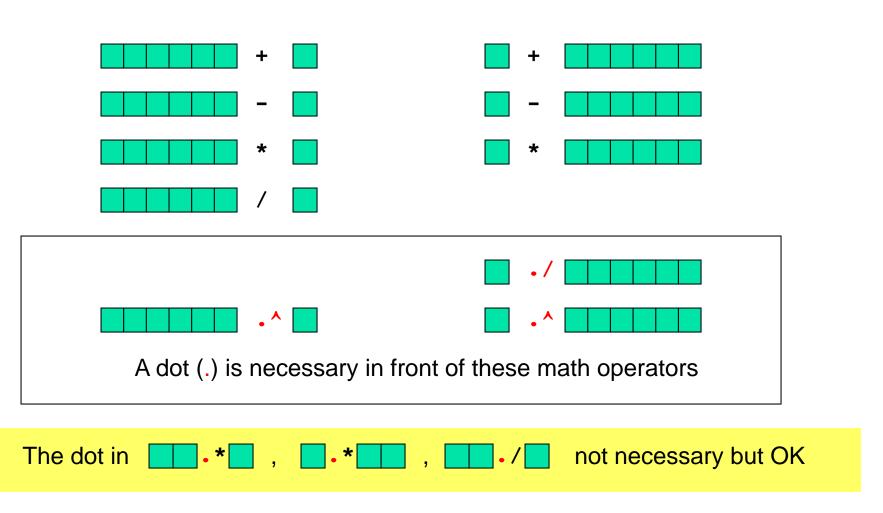
Matlab code:
$$z = x + y$$

Reciprocate



Vectorized

element-by-element arithmetic operations between an array and a scalar



See plotComparison.m

Can we plot this?

$$f(x) = \frac{\sin(5x)\exp(-x/2)}{1+x^2}$$
 for
$$-2 <= x <= 3$$

Yes!

operations on arrays

Element-by-element arithmetic operations on arrays... Also called "vectorized code"

$$x = linspace(-2,3,200);$$

 $y = sin(5*x).*exp(-x/2)./(1 + x.^2);$

Contrast with scalar operations that we've used previously...

a and b are scalars

The operators are (mostly) the same; the operands may be scalars or vectors.

When an operand is a vector, you have "vectorized code."

Concatenating 2 vectors—copy 2 vectors into a new one % given row vectors x and y

```
% given row vectors x and y
v= zeros(1,length(x)+length(y));
```

```
% given row vectors x and y
v= zeros(1,length(x)+length(y));
for k=1:length(x)
   v(k)= x(k);
end
```

```
% given row vectors x and y
v= zeros(1,length(x)+length(y));
for k=1:length(x)
   v(k) = x(k);
end
for k=1:length(y)
   v(length(x)+k)=y(k);
end
```

This is **non-vectorized code**—operations are performed on one component (scalar) at a time

```
% given row vectors x and y
v= zeros(1,length(x)+length(y));
for k=1:length(x)
   v(k) = x(k);
end
for k=1:length(y)
   v(length(x)+k) = y(k);
    Below is vectorized code—ops are performed on
    multiple components (a vector) at the same time:
end
                    v = [x \ y];
```

% given row vector v

```
% given row vector v
s= ceil(rand*length(v)); % split pt
x= zeros(1,s);
y= zeros(1,length(v)-s);
```

```
% given row vector v
s= ceil(rand*length(v)); % split pt
x= zeros(1,s);
y= zeros(1,length(v)-s);
for k=1:s
    x(k)= v(k);
end
```

```
% given row vector v
s= ceil(rand*length(v)); % split pt
x = zeros(1,s);
y= zeros(1,length(v)-s);
for k=1:s
                      This is non-vectorized
   x(k) = v(k);
                      code—operations are
                      performed on one
end
                      component (scalar) at a
for k=1:length(y)
   y(k) = v(s+k);
                       time
end
```

```
% given row vector v
s= ceil(rand*length(v)); % split pt
x = zeros(1,s);
y= zeros(1,length(v)-s);
for k=1:s
                      Below is vectorized code:
   x(k) = v(k);
                      multiple components
                      (subvectors) are
end
                       affected/accessed at the same
for k=1:length(y)
                       time:
   y(k) = v(s+k);
                       x= v(1:s);
y= v(s+1:length(v));
end
```

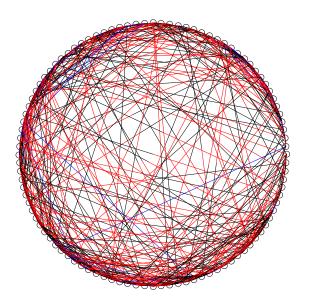
End of Prelim 1 material

Storing and using data in tables

A company has 3 factories that make 5 products with these costs:

	10	36	22	15	62
С	12	35	20	12	66
	13	37	21	16	59

What is the best way to fill a given purchase order?



Connections between webpages

```
      0
      0
      1
      0
      1
      0
      0

      1
      0
      0
      1
      1
      1
      0

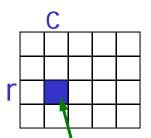
      0
      1
      0
      1
      1
      1
      1
      1

      1
      0
      1
      1
      0
      1
      1
      1

      0
      0
      1
      0
      1
      0
      1
      1
      0

      0
      1
      1
      0
      1
      1
      0
      1
      0
```

2-d array: matrix

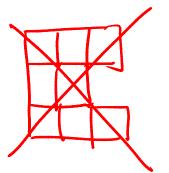


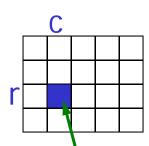
- An array is a named collection of like data organized into rows and columns
- A 2-d array is a table, called a matrix
- Two indices identify the position of a value in a matrix, e.g.,

refers to component in row r, column c of matrix mat

- Array index starts at 1
- Rectangular: all rows have the same #of columns

2-d array: matrix





- An array is a named collection of like data organized into rows and columns
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- Rectangular: all rows have the same #of columns

Creating a matrix

- Built-in functions: ones, zeros, rand
 - E.g., zeros(2,3) gives a 2-by-3 matrix of 0s
- "Build" a matrix using square brackets, [], but the dimension must match up:
 - [x y] puts y to the right of x
 - [x; y] puts y below x
 - [4 0 3; 5 | 9] creates the matrix 5 | 1
 - [4 0 3; ones(1,3)] gives
 - [4 0 3; ones(3,1)] doesn't work

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0

Working with a matrix: size and individual components

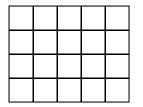
Given a matrix M

2	-1	.5	0	-3
3	8	6	7	7
5	-3	8.5	9	10
52	81	.5	7	2

Example: minimum value in a matrix

function val = minInMatrix(M)





Example: minimum value in a matrix

function val = minInMatrix(M)

% val is the smallest value in matrix M

[nr, nc] =
$$SiZe(M)$$
;
 $Val = M(I,I)$;
for $r = 1:nr$
% At row r
for $c = 1:nc$
% At col c (at row r)
if $M(r,c) < val$
 $val = M(r,c)$;
end
end

Pattern for traversing a matrix M

```
[nr, nc] = size(M)
for r= 1:nr
    % At row r
    for c= 1:nc
         % At column c (in row r)
         %
         % Do something with M(r,c) ...
    end
end
```