## CS1112 Discussion Exercise 9

## Two-dimensional interpolation

When you enlarge an image, you are actually adding data points among the existing data (pixels). How do you get the additional data points? One way is to interpolate from the neighboring points-take the average value. First, consider a simple case of one-dimensional interpolation, we add a data point between neighboring pairs of existing data points by taking the simple average. For example,

```
2.0 1.0 1.0 2.0 becomes 2.0 1.5 1.0 1.0 1.0 1.5 2.0.
```

In 2-d interpolation, work with one dimension at a time. For example, given a matrix

```
2.0}1.0\quad1.0 2.
6.0
5.0 5.0 5.0 4.0
```

First we can add a column between two neighboring columns, so the matrix becomes $3 \times 7$ :

| 2.0 | 1.5 | 1.0 | 1.0 | 1.0 | 1.5 | 2.0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6.0 | 5.5 | 5.0 | 4.5 | 4.0 | 3.5 | 3.0 |
| 5.0 | 5.0 | 5.0 | 5.0 | 5.0 | 4.5 | 4.0 |

Then add a row between neighboring rows, so the final matrix will be $5 \times 7$ :

| 2.0 | 1.5 | 1.0 | 1.0 | 1.0 | 1.5 | 2.0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4.0 | 3.5 | 3.0 | 2.8 | 2.5 | 2.5 | 2.5 |
| 6.0 | 5.5 | 5.0 | 4.5 | 4.0 | 3.5 | 3.0 |
| 5.5 | 5.2 | 5.0 | 4.8 | 4.5 | 4.0 | 3.5 |
| 5.0 | 5.0 | 5.0 | 5.0 | 5.0 | 4.5 | 4.0 |

Write two versions of the following function Interpolate2D: (a) use non-vectorized code; (b) use vectorized code (work with whole rows, or whole columns, one at a time). Do not use built-in function linspace.

```
function newM = Interpolate2D(M)
% Perform 2-d interpolation on the real-valued data in nr-by-nc matrix M.
% The interpolated data are added between existing data points so newM is
% (2*nr-1)-by-(2*nc-1). Use the simple average as the interpolated value.
```

If you haven't completed the exercise from last week, be sure to do it now!

