

### Announcements

- Prelim 2 conflicts due by midnight *tonight*
- Lab 11 is out
  - Due in 2 weeks because of Prelim 2
- Review Prelim 2 announcements from previous lecture
- A4 is due Thursday at midnight
- There will only be 5 assignments.
  - Can look at webpage for redistributed weights

### Recall: Important Terminology

- **assertion**: true-false statement placed in a program to *assert* that it is true at that point
  - Can either be a comment, or an **assert** command
- **invariant**: assertion supposed to "always" be true
  - If temporarily invalidated, must make it true again
  - **Example**: class invariants and class methods
- **loop invariant**: assertion supposed to be true before and after each iteration of the loop
- **iteration of a loop**: one execution of its body

### Preconditions & Postconditions

precondition

```
# x = sum of 1..n-1
x = x + n
n = n + 1
# x = sum of 1..n-1
```

postcondition

$n$

1 2 3 4 5 6 7 8

x contains the sum of these (6)

$n$

1 2 3 4 5 6 7 8

x contains the sum of these (10)

**Relationship Between Two**

If **precondition** is true, then **postcondition** will be true

- **Precondition**: assertion placed before a segment
- **Postcondition**: assertion placed after a segment

### Solving a Problem

precondition

```
# x = sum of 1..n
n = n + 1
# x = sum of 1..n
```

postcondition

What statement do you put here to make the postcondition true?

A:  $x = x + 1$

B:  $x = x + n$

C:  $x = x + n + 1$

D: None of the above

E: I don't know

### Invariants: Assertions That Do Not Change

- **Loop Invariant**: an assertion that is true before and after each iteration (execution of repetend)

```
x = 0; i = 2
while i <= 5:
    x = x + i*i
    i = i + 1
# x = sum of squares of 2..5
```

i = 2

# invariant

i <= 5

true

x = x + i\*i

i = i + 1

false

The loop processes the range 2..5

Invariant:

x = sum of squares of 2..i-1

in terms of the range of integers that have been processed so far

### Invariants: Assertions That Do Not Change

```
x = 0; i = 2
# Inv: x = sum of squares of 2..i-1
while i <= 5:
    x = x + i*i
    i = i + 1
# Post: x = sum of squares of 2..5
```

x = 0; i = 2

x

# Inv: x = sum of squares of 2..i-1

i

while i <= 5:

x = x + i\*i

i = i + 1

# Post: x = sum of squares of 2..5

Integers that have been processed: 2, 3, 4, 5

Range 2..i-1: 2..5

Invariant was always true just before test of loop condition. So it's true when loop terminates

x

i

i = 2

# invariant

i <= 5

true

x = x + i\*i

i = i + 1

false

The loop processes the range 2..5

### Designing Integer while-loops

```

# Process integers in a..b
# inv: integers in a..k-1 have been processed
k = a
while k <= b:
  process integer k
  k = k + 1
# post: integers in a..b have been processed
    
```

**Command to do something**  
**Equivalent postcondition**

### Designing Integer while-loops

1. Recognize that a range of integers b..c has to be processed
2. Write the command and equivalent postcondition
3. Write the basic part of the while-loop
4. Write loop invariant
5. Figure out any initialization
6. Implement the repetend (process k)

```

# Process b..c
Initialize variables (if necessary) to make invariant true
# Invariant: range b..k-1 has been processed
while k <= c:
  # Process k
  k = k + 1
# Postcondition: range b..c has been processed
    
```

### Finding an Invariant

```

# Make b True if n is prime, False otherwise
b = True
k = 2
# invariant: b is True if no int in 2..k-1 divides n, False otherwise
while k < n:
  # Process k;
  if n % k == 0:
    b = False
  k = k + 1
# b is True if no int in 2..n-1 divides n, False otherwise
    
```

**Command to do something**  
**Equivalent postcondition**

What is the invariant?     1 2 3 ... k-1 k k+1 ... n

### Finding an Invariant

```

# set x to # adjacent equal pairs in s
for s = 'ebee', x = 2

while k < len(s):
  # Process k
  k = k + 1
# x = # adjacent equal pairs in s[0..len(s)-1]
k: next integer to process.
Which have been processed?
    
```

**Command to do something**  
**Equivalent postcondition**

A: 0..k  
B: 1..k  
C: 0..k-1  
D: 1..k-1  
E: I don't know

### Finding an Invariant

```

# set x to # adjacent equal pairs in s
x = 0
# inv: x = # adjacent equal pairs in s[0..k-1]
while k < len(s):
  # Process k
  k = k + 1
# x = # adjacent equal pairs in s[0..len(s)-1]
k: next integer to process.
What is initialization for k?
    
```

**Command to do something**  
**Equivalent postcondition**

A: k = 0  
B: k = 1  
C: k = -1  
D: I don't know

### Reason carefully about initialization

```

# s is a string; len(s) >= 1
# Set c to largest element in s
c = ??
# inv: c is largest element in s[0..k-1]
while k < len(s):
  # Process k
  k = k + 1
# c = largest char in s[0..len(s)-1]
    
```

**Command to do something**  
**Equivalent postcondition**

1. What is the invariant?
2. How do we initialize c and k?

A: k = 0; c = s[0]  
B: k = 1; c = s[0]  
C: k = 1; c = s[1]  
D: k = 0; c = s[1]  
E: None of the above