

## 1 String Methods

(a) Implement the following function so that it performs as specified:

```
def Q1(s):
    """ Returns True if the first half of s is exactly same as the
        second half of s.

        PreCondition: s is a non-empty string with even length.
    """
```

(b) What can you say about a string `s` if the boolean expression `s.count(s[0]) == len(s)-1` is True? Assume that `s` has length 2 or greater.

(c) Give an example of a string `s` for which the boolean expression `s.find('xx') > s.find('x') >= 0` is True.

## 2 Loops

(a) Consider the following script:

```
N = input('Enter a positive integer: ')
s1=0
s2=0
for k in range(1,N+1):
    if k%2==0:
        s1 = s1+k
    else:
        s2 = s2+k
print s2-s1
```

What is the output if the value of `N` is 4? What is the output if the value of `N` is 99?

(b) Consider the following script:

```
k = 0
while k<=100:
    print k
    k=k+5
```

Write an equivalent script that makes effective use of a for-loop.

(c) Describe in English what the following function returns:

```
def F(s):
    """ PreCondition: s is a non empty string
    """
    t = '' # Empty string
    for c in s:
        if s.count(c)==1:
            t = t+c
    return t
```

### 3 Random Walk

A *travel string* for a robot journey is made up of the characters N, E, S, and W. If  $T$  is a travel string then  $T[k]$  specifies the direction of travel at step  $k$ . (Indexing steps from zero.) Assume that 'N' means that the  $y$ -value of the robot's location is increased by 1. Assume that 'E' means that the  $x$ -value of the robot's location is increased by 1. Assume that 'S' means that the  $y$ -value of the robot's location is decreased by 1. Assume that 'W' means that the  $x$ -value of the robot's location is decreased by 1. We assume that the robot starts at  $(0,0)$ .

(a) Complete the following function so that it performs as specified:

```
def FarAway(T,r,k):
    """ Returns true if and only if the robot's distance to (0,0)
        is greater than r just after it takes step k.
    PreC: T is a travel string, k is an int that satisfies  $0 \leq k < \text{len}(T)$ , r is a positive float.
```

(b) We say a step is *good* if after it is completed the robot's distance to the origin is greater than  $r$ . Complete the following function so that it performs as specified. Make effective use of `FarAway`.

```
def NotFarAway(T,r):
    """ Returns an int that is the total number of good steps.
    PreC: T is a travel string.
```

## 4 Short Answer

(a) Assign a value to  $x$  so that the following code prints ‘‘A’’:

```
x = _____  
  
if x == x-(x/d)*d+7:  
    print 'A'
```

(b) Assume that  $x$ ,  $y$ , and  $z$  are initialized integers. Can the Boolean expression  $(x*y)/z != x*(y/z)$  ever be True? Explain.

(c) Indicate the output if the following application script is run:

```
def F(x,y):  
    u = x+2*y  
    print x,y,u  
    return x  
  
if __name__ == '__main__':  
    x = 1  
    y = 10  
    u = 0  
    print x,y,u  
    y = F(y,x)+F(2*x,y)  
    print x,y,u
```

(d) A function can have local variables and parameters. Explain using as an example the function  $F$  in part (c).

## 5 A Graphics Computation

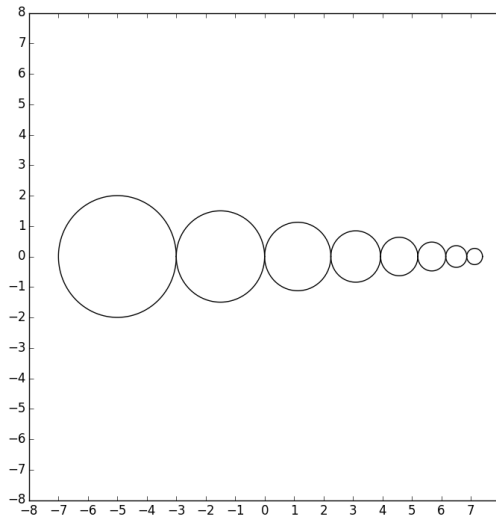
By adding code in between the two comments, produce a script that draws the figure below

```
x = -5
y = 0
r = 2
alfa = .75
DrawDisk(x,y,r)

for k in range(7):
#####

#####
DrawDisk(x,y,r)
```

Assume (a) all the circles have their centers on the x-axis, (b) the radius of a given circle is .75 times the radius of the circle to its left, (c) the circles are tangent to each other, and (d) the leftmost circle has radius 2 and center (-5,0)



## 6 Leading Zeros

Complete the following function so that it performs as specified

```
def ThreeDigit(n):  
    """Returns a length-three string that encodes the integer n.  
  
    Leading zeros are included if necessary, e.g., '000', '001', '012'.  
  
    Precondition: n is an integer that satisfies  $0 \leq n \leq 999$ .  
  
    """
```

Function	What It Does
<code>len(s)</code>	returns an <code>int</code> that is the length of string <code>s</code>
<code>s.count(t)</code>	returns an <code>int</code> that is the number of occurrences of string <code>t</code> in string <code>s</code>
<code>s.find(t)</code>	returns an <code>int</code> that is the index of the first occurrence of string <code>t</code> in the string <code>s</code> . Returns -1 if no occurrence.
<code>s.replace(t1,t2)</code>	returns a string that is obtained from <code>s</code> by replacing all occurrences of <code>t1</code> with <code>t2</code> .
<code>floor(x)</code>	returns a float whose value is the largest integer less than or equal to the value of <code>x</code> .
<code>ceil(x)</code>	returns a float whose value is the smallest integer greater than or equal to the value of <code>x</code>
<code>int(x)</code>	If <code>x</code> has type <code>float</code> , converts its value into an <code>int</code> . If <code>x</code> is a string like <code>'-123'</code> , converts it into an <code>int</code> like <code>-123</code>
<code>float(x)</code>	If <code>x</code> has type <code>int</code> , converts its value into a <code>float</code> . If <code>x</code> is a string like <code>'1.23'</code> , converts it into a <code>float</code> like <code>1.23</code> .
<code>str(x)</code>	Converts the value of <code>x</code> into a string.
<code>DrawRect(x,y,L,W)</code>	Draws a rectangle with center $(x, y)$ , horizontal dimension <code>L</code> , and vertical dimension <code>W</code> .
<code>DrawDisk(x,y,r)</code>	Draws a circle with center $(x, y)$ and radius <code>r</code> .
<code>DrawStar(x,y,r)</code>	Draws a star with center $(x, y)$ and radius <code>r</code> .
<code>DrawLineSeg(x,y,L,d)</code>	Draws a length <code>L</code> line segment that starts at $(x, y)$ and makes counterclockwise angle of <code>d</code> degrees with the positive x-axis.